AN EFFICIENT PARALLEL GPU EVALUATION OF SMALL ANGLE X-RAY SCATTERING PROFILES

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Abstract: The inference of protein structure from experimental data is of crucial interest in science, medicine and biotechnology. Unfortunately, high-resolution experimental methods can not yet provide a detailed analysis of the ensemble of conformations adopted under physiological conditions. Low resolution techniques are often better suited for this task. Small angle X-ray scattering (SAXS) plays a major role in investigating important biological questions regarding the structure of multidomain proteins connected by flexible linkers or the aggregation processes that underlie several major diseases in humans.

In silico simulations can bridge the gap between low resolution information and models derived from high-resolution techniques. For that, it is necessary to be able to calculate the low resolution information from a given detailed model using a so-called *forward model*. These calculations need to be performed many times during a conformational search, and therefore need to be computationally efficient.

We present an efficient implementation of the forward model for SAXS experiments with full hardware utilization of General Purpose Graphical Processor Units (GPGPUs). The proposed algorithm is orders of magnitude faster than an efficient CPU implementation, and implements a caching procedure ready to be employed in the partial SAXS evaluations required by *in silico* simulations.

1 INTRODUCTION

Proteins play a crucial role in science, medicine and biotechnology: without them, cellular activities such as catalysis, signaling and regulation would be impossible. Protein function is determined by protein structure, which is in term determined by the amino acid sequence (Anfinsen, 1973).

Despite encouraging improvements, determining the ensemble of possible conformations in solution is far from an accomplished goal. High resolution experimental methods, notably X-ray crystallography and Nuclear Magnetic Resonance (NMR), can only partially provide information on such ensembles, and encounter several limitations in fully describing the flexibility of large systems in physiological conditions (Zheng and Doniach, 2005).

Low resolution methods, on the other hand, can more easily provide information on such ensembles. In particular, Small Angle X-ray Scattering (SAXS) provides information on the excess electron density of the sample versus the surrounding environment. Recently, with the advent of automated high-throughput SAXS analysis of biomolecules (Toft et al., 2008; Hura et al., 2009), high-throughput data acquisition is within reach. Since SAXS data only describes the spherical averaging of the electron density of the average conformation of the ensemble, additional information is needed to assist structural interpretation.

Usual *in silico* methods propose plausible structural conformations, and calculate their associated scattering profile by means of a forward model. Then, the proposed and the experimental profiles are compared using an error model of the experiment. For this procedure to be successful, an efficient procedure for both sampling protein structures and calculating the SAXS profile is required. We focus on the latter problem.

Early approaches for the evaluation comprise *ab initio* shape determinations using spherical harmonics expansions (Svergun and Stuhrmann, 1991). Here, computational feasibility is attained at the cost of limiting the possible shapes of the sample, for instance excluding internal cavities (Koch et al., 2003). Other modeling approaches compute and fit the scattering curve from a condensation of a gas of "dummy beads" to an experimental SAXS curve. This has been done using conformational searches by a genetic al-

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gorithm in DALAI_GA (Chacon et al., 1998) or simulated annealing in DAMMIN (Svergun, 1999) and DAMMIF (Franke and Svergun, 2009).

Higher resolution models impose further constraints to the proposals. In the GASBOR program (Svergun et al., 2001), a SAXS profile is calculated for a packed assembly of spheres placed according to a pseudo- C_{α} chain. The scattering intensity is calculated using the Debye formula, while simulated annealing is used for searching the conformational space. Other recent structure prediction methods, such as the ORNL (Tjioe and Heller, 2007) and IMP (Förster et al., 2008) programs, utilize the SAXS curve as an energy term in combination with other energy contributions from physical force fields. Since these descriptors are non-probabilistic in nature, the weights used for scaling the SAXS energy to other conformational constraints must be chosen heuristically (Habeck et al., 2006).

In recent publications, our group developed probabilistic models for the proposal of protein-like conformations, in full atomic detail, for both backbone and side chains (Boomsma et al., 2008; Harder et al., 2010). We also developed a forward model of the scattering profile evaluation, that includes the experimental error associated with SAXS data (Stovgaard et al., 2010). The forward model consists of a coarse-grained computation based on the Debye formula (Debye, 1915). Our main aim is the study of proteins consisting of multiple domains connected by flexible linkers. Such proteins play a major role in the regulation of gene expression, cell growth, cell cycle, metabolic pathways, signal transduction, protein folding and transport (Levitt, 2009; Madl et al., 2010). With this aim, a computationally efficient forward model for the calculation of SAXS curves is paramount.

We ported our original implementation of the Debye formula to General Purpose Graphics Processing Units (GPGPUs), parallel computing engines that can offer great advantages in terms of cost-efficiency and low power consumption (Göddeke and Strzodka, 2011). One of the emerging standards of choice for their programming is the Open Computing Language (OpenCL), an open standard that provides an abstraction layer over hardware implementations of highly parallel computational engines (Stone et al., 2010).

2 METHODS

2.1 Forward SAXS Computation

The observed data in a SAXS experiment is a one-

dimensional intensity curve, I(q), measured at discretized scattering momenta $q = 4\pi \sin(\theta)/\lambda$, with λ the wavelength of the incoming radiation and 2 θ the scattering angle between the principal and the probing beam rays. The calculation of a theoretical SAXS profile from a given atomic structure is based on the well-known Debye formula (Debye, 1915):

$$I(q) = \sum_{i=1}^{M} \sum_{j=1}^{M} F_i(q) F_j(q) \frac{\sin(q \cdot r_{ij})}{q \cdot r_{ij}}$$
(1)

where F_i and F_j are the scattering form factors of the individual particles *i* and *j*, and r_{ij} is the Euclidean distance between them. The summations run over all the *M* scattering particles.

2.2 Coarse-grained Protein Models

If some scatterers are fixed relative to each other, they can be approximated by a single large scattering body (*dummy body*). This approximation, more precise at low q, fades with the progression of the scattering angle up to a resolution equal to the scattering diameter of the dummy body. We found that the amino acids constituent to the protein chain can be approximated by one or two large bodies (*dummy atoms*), and that this approximation holds up to scattering angles normally not measured in the current experimental standards (Stovgaard et al., 2010).

In the two body model, the amino acids are individually represented by two dummy atoms; one representing the backbone, and the other representing the side chain. Glycine and alanine, lacking a side chain, are represented by one dummy atom only. The dummy atoms are placed at the respective centers of mass (see Figure 1). A total of 21 form factors need to be estimated for the two body model: one for alanine, one for glycine, one for the generic backbone and 18 for the remaining side chains.

For the one body model, the single dummy atom is placed at the center of mass of the amino acid. Hence, 20 form factors need to be estimated; one for each amino acid type. For a given protein, the one body model allows to represent the molecule in roughly half the number of scattering bodies as compared to the two body model. If the experimental data is recorded at low resolutions only, the former is thus clearly preferable for reasons of computational efficiency.

2.3 Form Factor Descriptors

Due to the lack of publicly available high-quality experimental data needed for the estimation of the

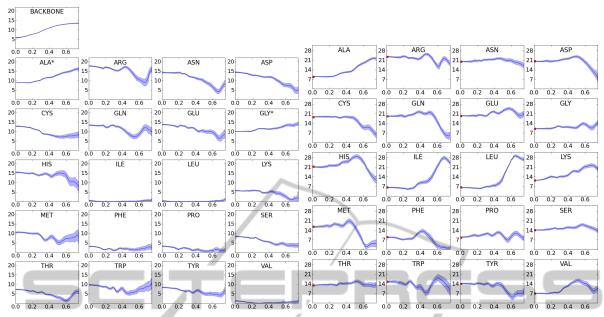


Figure 2: Form factors. Mean (dark blue curve) and standard deviations (blue areas) for the form factors (Y-axis) as a function of q (X-axis). Left: backbone and side-chains. An asterisk indicates that this form factor describes both the backbone and side chain atoms of the residue. Right: the single body form factors. Figure adapted from (Stovgaard et al., 2010).

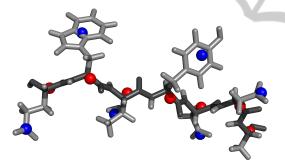


Figure 1: **Coarse-grained models of protein structure**. Example of a protein backbone stretch (dark gray) with side chain atoms (light gray). The placement of the dummy bodies for the center of mass of the backbone atoms (red spheres) and for the side chains (blue spheres) are indicated. Figure prepared with PyMOL (Schrödinger, 2010), adapted from (Stovgaard et al., 2010).

form factors, artificial data curves were generated for known high-resolution protein structures using the state-of-the-art program CRYSOL (Svergun et al., 1995). This program computes the theoretical scattering curve from a given full-atom structure using spherical harmonics expansions, therefore limiting its applications at studying compact quasi-globular proteins. We can however use this input to feed a learning protocol, and make use of the Debye formula in eq. 1 to overcome structural assumptions.

Therefore, a large scale Monte Carlo simulation has been conducted to estimate the values of the form factors of the dummy atoms (Stovgaard et al., 2010). The resulting profiles for these descriptors are shown in Figure 2.

In Figure 3 we show a SAXS curve generated with our method, and the theoretical scattering computed by CRYSOL as a reference.

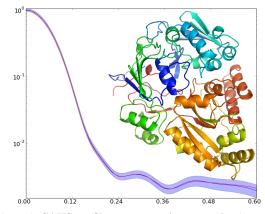


Figure 3: SAXS profile reconstruction example. Comparison of the reference profiles I(q) computed by CRYSOL from the all atom structure (blue) and by the two body model (red). Error shade indicates the simulated "experimental" error. PDB code 1JET (520 residues). Cartoon made with PyMOL (Schrödinger, 2010).

2.4 OpenCL Programming Model

An OpenCL program contains a host program that executes on the CPU, and kernels that execute on the abstracted parallel hardware. The hardware is defined as one or more compute units, which are composed of one or more processing elements and, in some cases, local memory.

The host program coordinates the execution of the kernels, and can be written in any programming language. Kernels are written in a variant of the latest released C language standard (C99) and are compiled at run time to device-specific instructions. A kernel describes the operations of a single work-item, or thread, and is run simultaneously by a set of work-items called a work-group.

The local memory of a compute unit, if present, is shared by all work-items in a work-group and provides an efficient communication channel among them. It has very low latency and is usually implemented with a full crossbar interface, but is limited in size and does not retain its state between kernel executions.

Therefore, kernels execute most efficiently when the size of the work-group matches the size of the compute unit on the OpenCL device and when all work-items in a work-group follow the same execution path.

2.5 Efficient GPU Implementation

2.5.1 Parallel Page-tile SAXS Algorithm

The computation of a SAXS profile is experimentally discretized in a set of q points, and thus naturally provides the first level of parallelization, into pages. Each page represents the computation of the intensity curve I(q) for a single value of q. A page can be visualized as a square problem matrix of side equal to the number of scattering particles M, with each cell representing the contribution of a single term of the Debye formula for particular i and j.

For performance considerations and direct mapping to the hardware, pages are partitioned into square tiles of side k, where k is set to the specific compute unit size of the OpenCL device. Since each problem matrix is symmetrical, only the tiles encompassing the lower-left triangle and the diagonal are computed and their value is simply duplicated for the mirror tiles in the upper-right triangle of the matrix. The domain decomposition is illustrated in Figure 4 for an example of 16 scattering particles and work-group size of 4.

GPUs suffer performance penalties when they have to work with data that is not aligned to their native architecture, therefore the algorithm pads the data and aligns it to the specified work-group size. The resultant dummy particles participate in the Debye calculations, but they are assigned a form factor of 0, so

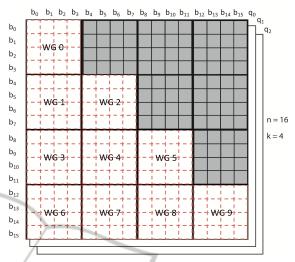


Figure 4: **Domain decomposition for the Page-Tile algorithm.** Work-groups operate on square tiles from the matrix. Only tiles in the lower-left part and the diagonal are evaluated.

their contribution to the intensity I(q) is null.

Algorithm 1 presents the pseudocode for the Page-Tile SAXS algorithm. The form factors table, supplied as input, is packed and organized by scattering momentum and particle type. The scattering particles, in addition to their position in three dimensions, have a type in the form of an index into the form factor table. The initial intensity curve calculation comprises four kernels.

Algorithm 1: Page-Tile SAXS algorithm.

Input: scattering momenta, form factors table, scattering particles

Output: intensity curves for the scattering momenta /*Host program*/

Initialize the parallel algorithm

Transfer input data to GPU global memory and queue the kernels for initial profile calculation

/*Kernels executed on the GPU*/

Map form factors to scattering particles (Kernel 1) Compute the Debye sum term for each tile (Kernel 2) Perform vertical tile sum reduction for each page (Kernel 3)

Perform horizontal margin sum reduction for each page to get the intensity curve (Kernel 4)

/*Host program*/

Retrieve the results from GPU global memory

In Kernel 1 the form factor table is mapped into a form suited for hardware-efficient parallel access. The form factors are organized by scattering particle, which enables the work-groups with streaming memory access for both center coordinates and form factors.

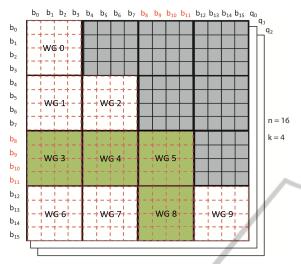


Figure 5: Problem matrix after a move. Particles b8, b9, b10 and b11 have changed positions. Blocks WG3, WG4, WG5 and WG8 will be recalculated.

The majority of execution time is spent in Kernel 2, where the Debye sum terms for the individual tiles are computed. The Debye formula is used for each term, but *i* and *j* are limited to the ranges defined by the boundaries of the tile within the global index space. The kernel uses local memory to improve performance, by pre-loading the particles and their form factors, and by performing an in-place parallel reduction to produce the partial sum for the tile. During the Debye calculation, 4x loop unrolling utilizes local registers to further optimize this stage.

Kernel 3 reduces the tile partial sums, which are stored in a global cache, to bottom margin sums that are further reduced by Kernel 4 to yield the final intensity curve.

2.5.2 Tile Recalculation

Monte Carlo Markov Chain simulations explore the conformational space of the protein structures by applying partial modifications over an accepted proposal. The average SAXS computation is therefore a partial re-evaluation of a previously computed profile, where only a subset of the bodies changed their position.

It is therefore possible to identify the subset of tiles that needs to be updated. Since the Page-Tile algorithm caches the partial contribution of each tile to the global summation, we can impose a partial recalculation of only the affected tiles (see Figure 5). This leads to a substantial reduction in the time necessary to derive an intensity curve after a move.

Algorithm 2 illustrates the pseudocode for tile recalculation. The form factor table from the initial cal-

Algorithm 2: Tile recalculation. Input: moved scattering particles Output: updated intensity curve for the scattering momenta /*Host program*/ Transfer input data to the GPU global memory and queue the kernels involved in the profile recalculation /*Kernels executed on the GPU*/ Compute the Debye sum term for the changed tiles (Kernel 5) Perform the vertical tile sum reduction for each page (Kernel 3) Perform horizontal margin sum reduction for each page to get the intensity curve (Kernel 4) /*Host program*/ Retrieve the results from the GPU global memory

culation is reused, so execution starts directly with Kernel 5, which identifies the affected tiles and invokes Kernel 2 for them. Kernel 3 and Kernel 4 perform the reductions as in the initial calculation.

2.5.3 Floating Point Precision

Floating point numbers can be stored and manipulated with single precision (SP) or double precision (DP). Mathematical operations on floating point numbers introduce errors, due to the finite precision available. Those errors tend to accumulate when a large number of operations is performed, as is the case with the double sum of the Debye formula. However, the Page-Tile algorithm significantly reduces this error growth, because its successive partitioning of the problem space results in an execution pattern resembling pairwise summation (Higham, 1993). The algorithm can be executed with SP or DP, paying a performance penalty of a factor of 2 to 4 with DP.

We measured the divergence between the SP and DP executions, and no significant differences arise between the results. Therefore, the SP implementation is used by default.

3 RESULTS AND DISCUSSION

3.1 Computational Efficiency of the SAXS Modeling

The Debye formula (Equation 1) leads to a computational complexity of $O(M^2)$, with M the number of scatterers in the structure under examination. Our coarse-grained approach reduces M by representing several atoms by one scattering body (a dummy atom), thereby lowering the complexity to $O\left(\left(\frac{M}{k}\right)^2\right)$, with *k* the number of scatterers (atoms) described by a dummy body.

The precise value of k is dependent on the primary sequence of the protein. On large datasets, the two dummy model leads to an average k of 4.24 (with a performance increase of $k^2 \simeq 18$). The single body model leads to $k \simeq 7.8$, allowing for a $k^2 \simeq 60$ times quicker execution.

3.2 GPGPU Implementation

The performance of the Page-Tile algorithm was measured on a system with a Core i7-920 CPU, 12GB of DDR3 RAM and a NVIDIA GeForce GTX 560 Ti GPU with 1GB of GDDR5 RAM. The GTX 560 Ti has 8 compute units with 32 processing elements each, comprising 384 processing elements, with 32KB 32-bit registers and 48KB of local memory for each compute unit.

Performance was measured against a test protein of over a thousand amino acids, modeled with 1888 scattering bodies in the dual dummy atom representation, and a discretization of the q space in 51 scattering momenta. Protein moves were modeled by a random mutation of 40% of the particles, to approximate the asymptotic move rate in a Monte Carlo simulation. The execution times for the model test case are presented in Table 1.

Table 1: Execution times for SAXS curve calculation for a protein with 1888 bodies, 51 scattering momenta and 21 form factors per momentum. Execution times from the top are for a single processor CPU implementation, a parallel GPU full computation, and GPU partial computation, respectively. Partial computations mimic the costs in a Monte Carlo simulation, where at each step around 40% of the proposal structure is updated.

Algorithm	Time (ms)
CPU SP Time	2408
GPU full calculation	9
GPU recalculation	6.484

The performance of the algorithm was also measured for protein sizes ranging from 64 to 8192 scattering particles. Each protein was moved 1000 times, in order to obtain an average of the recalculation steps. Figure 6 shows the speed increase, relative to the CPU single precision implementation, calculated as t_{cpu}/t_{gpu} .

Figure 6 also illustrates the hardware utilization of the parallel Page-Tile algorithm. The plot shows an asymptotic behavior around problem sizes of 2000 scattering bodies. The GTX 560 Ti GPU employed in the tests is composed of 8 compute units operating on

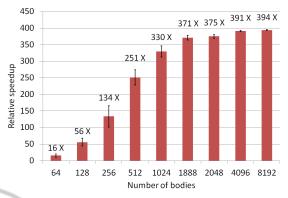


Figure 6: Algorithm performance for problem sizes ranging from 64 to 8192 scattering bodies, including the model test case of 1888, with error bars showing standard deviation. All SAXS computations involve the summations over 51 scattering momenta. The asymptotic behavior indicates hardware saturation at around 2000 bodies, which is the theoretical maximum for the GPU model used in the tests.

8 cascading work-groups, allowing for a theoretical peak of 64 active work-groups. The work-group size is 32, therefore the card would reach theoretical peak processing power at 2048 bodies. Our tests show saturation at the same level, thus indicating optimal use of the hardware.

OpenCL is thread-safe and allows access to the same device from multiple processes and threads, so by creating multiple instances of the Page-Tile algorithm, more than one calculation can be run at the same time. This is especially relevant in the case of problem sizes that would not lead to a full GPU saturation, therefore allowing for multi-threaded Monte Carlo simulations.

As a proof of concept, two instances of the algorithm were run in parallel on the test system with the model test problem of size 1888. The recorded time to complete a move recalculation was 11.962ms, or 93% of the time to complete two moves sequentially, indicating that the excess processing capacity was indeed utilized.

4 CONCLUSIONS

We have presented an efficient implementation of the forward model for the computation of Small Angle X-ray Scattering profiles. The application is multithread safe, and benchmarks show that the General Purpose Graphic Processor Units deliver the full theoretical output allowable by the hardware.

Parallelization is achieved on multiple levels by taking advantage of the structure of the Debye problem. The first level divides the SAXS evaluation in INC

multiple independent computations according to the binning of the scattering momentum. A nested level then makes full use of the work-groups in the hardware by splitting the inner summation of the Debye formula in separate partial sums. The resulting program runs orders of magnitude faster than an optimized single core CPU implementation.

A caching algorithm on the inner contributions allows for the efficient re-evaluation of SAXS profiles from partially updated structures, delivering even greater benefits to applications like Markov Chain Monte Carlo simulations of important biological and clinical targets. An open source implementation will be released shortly.

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SOURCE CODE AVAILABILITY

The source code of our implementation can be found online at: http://www.phaistos.org and http:// sourceforge.net/projects/phaistos/files.

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