

EPILEPTIC ELECTROENCEPHALOGRAM SIGNAL CLASSIFICATION BASED ON SPARSE REPRESENTATION

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Abstract: Epilepsy seizure detection in Electroencephalogram (EEG) is a major issue in the diagnosis of epilepsy and it can be considered as a classification problem. According to the particular property of EEG, a novel method based on sparse representation is proposed for epilepsy detection in this paper. Classification accuracy, robustness on noisy data and parameters (the size of dictionary and the number of features) of proposed method are tested and analysed on the public available data. The proposed method can obtain the highest classification accuracy among the discussed methods when the suitable parameters are set, and the proposed method based on sparse representations for classification is robust to noise. This is consistent with the theory that sparse representations can capture the inherent structure of signal. Furthermore, it is shown by experiments that the optimal selection of the parameters is critical to the performance of epilepsy detection.

1 INTRODUCTION

Epilepsy is a chronic neurological disorder that plagues about 50 million people worldwide at one time. It is characterized by recurrent unprovoked seizures that disturb the nervous system. However who has a seizure does not necessarily have epilepsy, for example many diseases might cause seizure-like activity such as stroke, life-threatening dehydration or high temperature. And sometimes there authentically are epileptic even absence of seizures. Due to that non-epileptic seizures are difficult to differentiate from epileptic ones, misdiagnosis might happen. A significant way for identifying and analyzing epileptic seizure activity in humans is by using Electroencephalogram (EEG) signals, which record the electrical potentials produced by the brain, and are the basis of epilepsy clinical diagnosis and treatment. In the past, interpretation of the EEG was limited to visual inspection by a neurophysiologist, an individual trained to make qualitatively a distinction between normal EEG activity and abnormalities contained within EEG records. Unfortunately, prediction of epilepsy which needs visual inspection of long recordings of EEG is usually a time-consuming and high-cost process. Therefore,

several diagnostic aid approaches for automated detecting epileptic seizures from EEG signals were proposed in recent years.

Nigam and Graupe employed a multistage nonlinear pre-processing filter for extracting two features: relative spike amplitude and spike occurrence frequency, then which were fed to a diagnostic artificial neural network for automatically detecting of epileptic seizures from EEG signals and obtained 97.2% accuracy (Nigam, 2004). Srinivasan obtained 99.6% classification accuracy by using Time & Frequency domain features and recurrent neural network (Srinivasan, 2005). Güler *et al* obtained 96.79% classification accuracy by using recurrent neural networks to detect the epileptic seizure from EEG signals (Güler, 2005). Subasi decomposed the EEG signals using discrete wavelet transform. Some statistical information were extracted from the wavelet coefficients, and applied for different classifiers for epileptic EEG classification, such as feed-forward error back-propagation artificial neural network (FEBANN) (Subasi, 2005-A), dynamic wavelet network (DWN) (Subasi, 2005-B), dynamic fuzzy neural network (DFNN) (Subasi, 2006), an adaptive neuron-fuzzy inference system (ANFIS) (Subasi, 2007-A) and

mixture of expert system (ME) (Subasi, 2007-B), and separately obtained accuracies of 91%, 93%, 93%, 94% and 95%, respectively.

Übeyli employed wavelet analysis with combined neural network model to discriminate EEG signals (Übeyli, 2009). The EEGs were decomposed into time–frequency representations using discrete wavelet transform (DWT) and then statistical feature were calculated. Then a two-level neural network model was used to classify three types of EEG signals. classification accuracy of 94.83% was achieved. Ocak detected epileptic seizures based on approximate entropy (ApEn) and discrete wavelet transform. EEG signals were firstly decomposed into approximate and detailed coefficients by DWT, and then ApEn values for each set of coefficients were computed. Finally, surrogate data analysis was used to classify the ApEn values (Ocak, 2009).

EEG is a non-stationary and extremely sensitive signal, even a small movement from eyes or body can contaminate it. Most of researches extract features for classification from signals in which the polluted signal segments or contaminated channels have been removed by visual inspection and the noise influences from EOG, EMG and other channels have been reducing by preprocessing, and don't consider the influence of noise to classification accuracies.

Recent research suggests that sparse representation of signal over complete dictionaries is a powerful representation method for processing signal and images, and it is applied in many fields. Sparse representations have also been used for face recognition (Wright, 2009), signal classification (Huang, 2007). However, to our knowledge, there is no study related to sparse representation in epileptic EEG signal classification till now. In this paper, a new approach based on sparse representation is presented for epileptic EEG signal classification. Features for classification are extracted by sparse representation of original EEG signal directly, and this decrease the run time for data preprocessing is not needed. Since sparse representation can capture the inherent structures of signal, the proposed method is relative robust to some noise. The feasibility and efficiency of the proposed method are shown by the experiments.

This paper is structured as follows: theoretical background is introduced in section II, and in section III EEG signal classification based on sparse representation is proposed, Then Section IV presents the experimental results. Finally, conclusions and future work are discussed.

2 THEORETICAL BACKGROUND

2.1 Sparse Representations of Signals

Some natural signals have compact and condense representation in some domain, the property which is called sparsity (Richard, 2007). A real-valued, finite-length, one-dimensional, discrete-time signal x can be viewed as an $N \times 1$ column vector in \mathbb{R}^N . Any signal in \mathbb{R}^N can be represented in term of a basis of $N \times 1$ orthonormal vectors $\{D_i\}_{i=1}^N$. It can be formulated as follow:

$$x = \sum_{i=1}^N a_i D_i \text{ or } x = D\alpha. \quad (1)$$

Where, α is the $N \times 1$ column vector of weighting coefficients. Here, x and α are equivalent representations of the signal, with x is in the time domain and α is in the D domain.

The signal x is K -sparse if it is a linear combination of only K ($K \ll N$) basis vectors: that is, only K of the coefficients in equation (1) are nonzero (or large) and $(N-K)$ are zeros (or small). So the sparse representation of signal can use as little as possible amount of data to represent the original data.

2.2 Gabor Dictionary

In sparse representation, the selection of domain D is very important, only appropriate basis can ensure the sparsity of signal. Recent years, the sparse representation of signal based on overcomplete redundant dictionaries has been attracting increasing attention. That signal were decomposed with an overcomplete dictionary instead of an orthonormal basis can result in not only a higher sparsity degree, but also greater flexibility in capturing the inherent structure of the natural signals (Zhang, 2005). An overcomplete dictionary can either be chosen as a prespecified set of functions such as overcomplete wavelets, curvelets, contourlets, steerable wavelet filters, short-time-Fourier transforms, or designed by adapting its content to fit a given set of signal example (Aharon, 2006) (Mairal, 2009). The former is simple and fast, and the selection of function should base on how suitable they are to sparsely describe the signals in question; the latter usually is more suitable for the given set of signals, but it is more expensive in computational cost.

Gabor wavelets were introduced to EEG signal analysis due to their biological relevance and computational properties. Gabor functions (Mallat, 1993)

in wavelets provide optimal joint time-frequency localization.

Gabor dictionary D_g is constructed as follows:

$$D_g = \{g_r(t)\}, r \in \Gamma, \quad (2)$$

where,

$$g_r(t) = K(\gamma) e^{-\pi \left(\frac{t-\mu}{s}\right)^2} \cos(2\pi\omega(t-\mu) + \varphi) \quad (3)$$

where, $g_r(t)$ is the Gabor atom. $K(\gamma)$ is normalization factor to ensure $\|g_r(t)\|=1$. Each element in parameter set $\gamma = \{\mu, s, \omega, \varphi\}$ represents separately the position, scale, frequency and phase of Gabor atom. A series of Gabor atoms which can be created by different parameters of $\{\mu, s, \omega, \varphi\}$ compose an overcomplete dictionary $D_g = \{g_r(t)\}$, $r \in \Gamma$.

2.3 Matching Pursuit

Given an overcomplete dictionary $D = \{g_1, g_2, \dots, g_n\}$ (n is the number of atoms in dictionary D), the representation of a signal have many or infinite possible combinations. Sparse representation based on overcomplete dictionary is to find the best matched and the sparsest combination.

The following objective function (Mallat, 1993) is minimized:

$$J(\alpha) = \left\| f(t) - \sum_{i=1}^M \alpha_i g_{\gamma_i}(t) \right\|_2^2 + \lambda \|\alpha\|_0. \quad (4)$$

where, f is the original signal, $\{\gamma_i\}_{i=1 \dots M}$ represents the indices of the chosen atoms g_{γ_i} and α_i is decomposing coefficient corresponding to g_{γ_i} . $\|\alpha\|_0$ is the \mathcal{L}_0 norm, and it is the number of nonzero components in the vector α . Minimizing the former item of the formula can find the best matched approximate, and minimizing the latter item can find the sparsest one. The parameter $\lambda > 0$ is a scalar regularization parameter that balances the tradeoff between reconstruction error and sparsity. Due to its nature of combinational optimization, it is a NP hard problem to find the solution to equation (4). Suboptimal solutions to this problem can be obtained by iterative methods such as the matching pursuit (MP) (Mallat, 1993) (Mallat, 1994). MP is a greedy algorithm that optimizes the signal approximation by iteratively selecting atoms which best match the signal structures at each step.

In the first step of MP, the atom g_{γ_0} that best matches the signal f is chosen. In each of the consecutive steps, the atom g_{γ_n} is matched to the residual signal $R^n f$.

The procedure of MP can be described by Equa-

tion (5).

$$\begin{cases} R^0 f = f \\ R^n f = \langle R^n f, g_{\gamma_n} \rangle g_{\gamma_n} + R^{n+1} f \\ g_{\gamma_n} = \arg \max_{g_{\gamma_i} \in D} |\langle R^n f, g_{\gamma_i} \rangle| \end{cases} \quad (5)$$

2.4 Bayesian Decision Rule

In Pattern Recognition, there are a variety of decision rules, but only Bayesian Decision Theory is optimal (Christopher, 2006). Bays Decision Theory is based on the popular Bays theorem, which is essentially an expression of conditional probabilities. Conditional probabilities represent the probability of an event occurring given evidence.

$$p(\omega_i | x) = \frac{p(x | \omega_i) p(\omega_i)}{p(x)} = \frac{p(x | \omega_i) p(\omega_i)}{\sum_{j=1}^k p(x | \omega_j) p(\omega_j)} \quad (6)$$

Where, $i = 1, \dots, k$, k is the number of classes. If $p(\omega_i) = p(\omega_j)$, $i \neq j$, then equation (6) was simplified as:

$$p(\omega_i | x) = \frac{p(x | \omega_i)}{\sum_{j=1}^k p(x | \omega_j)}. \quad (7)$$

The classification rule becomes:

$$x \in \omega_j, \quad (8)$$

where,

$$p(\omega_j | x) = \max p(\omega_i | x) = \max \frac{p(x | \omega_j)}{\sum_{z=1}^k p(x | \omega_z)}. \quad (9)$$

3 EEG SIGNAL CLASSIFICATION BASED ON SPARSE REPRESENTATION

3.1 Algorithm Framework

In this study, EEG signals of normal and epileptic patients are used. Epileptic seizure detection in EEG can be thought as a classification problem. It includes data acquisition, feature extraction, and classification procedure. According to the property of EEG, a novel EEG signal classification method is proposed, which based on sparse representation of signal and Bays classifier. The procedure of the proposed method can be summarized as follows:

Step 1: Divide every EEG signal sample into some sub-samples. Since in the process of sparse representation, the dimension of signal is equivalent to the dimension of the atoms of dictionary, sub-samples can greatly save the storage space and avoid tre-

mendous computation.

Step 2: Construct the overcomplete dictionary.

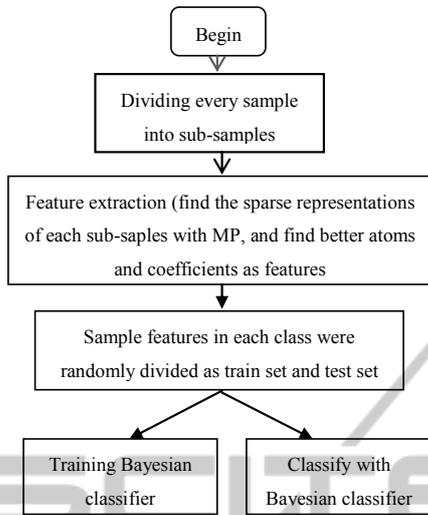


Figure 1: Flow chart of the system.

Step 3: Find the better atoms in the given dictionary and their decomposed coefficients for every sub-sample by MP, and select decomposed coefficients and atom parameters as features to formulate the training set and test set for classification.

Step 4: Train the Bayesian classifier by training set.

Step 5: Test the performance of Bayesian classifier by test set.

Fig.1. show the flow chart of the method.

In the Framework, the algorithm of feature extraction is our main contribution which will be described in the following section.

3.2 Feature Extraction based on Sparse Representation

Motivated by the compressive sensing theory that since sparse representation can recover signal without any significant information loss, can it be used as signal feature for classification? In (Huang, 2007) the coefficients of sparse representation based on the same atoms which are optimized based on all samples in average are used as features for classification. So the selected atoms for sparse representation must not be the best for single sample. In this paper, a new features for classification based on sparse representation are proposed. Different from feature extraction method in (Huang, 2007), better atoms and coefficients in sparse representation of each sample are taken as features for classification in this study.

Every EEG signals epoch x can be represented as:

$$x = \sum_{i=1}^N \alpha_i g_i. \quad (10)$$

Where, N is the number of atoms in Gabor Dictionary. The coefficients of sparse representation of one of EEG epochs are shown as Figure 2, from which it can be seen that the signal is sparse. The bigger coefficients are, the more main signal information their corresponding atoms should contain. So, the bigger coefficients and their corresponding atoms parameters are taken as features.

The features for classification are denoted as:

$$\text{Feature Vector} = \{\alpha_i, \mu_i, s_i, \omega_i, \varphi_i\}, i = 1 \cdots M \quad (11)$$

Where M is the number of selected dictionary atoms for classification. Then, the number of features used for classification will be $5 * M$. The selection of M and N which are critical for classification performance will be studied in next section.

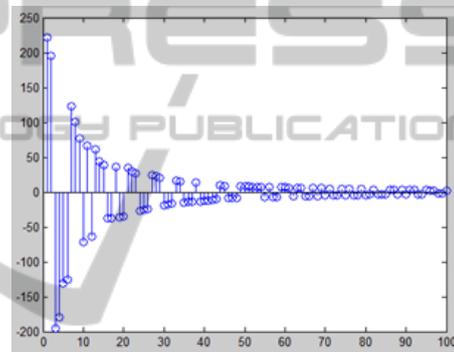


Figure 2: The coefficients of sparse representation.

4 EXPERIMENT

4.1 Data

The public available data described in (Andrzejak, 2001) is used. The complete data set consists of five sets (denoted as Z, O, N, F and S) and each contains 100 single-channel EEG segments. The dimension of the raw data set is 4096. Sets Z and O consist of segments taken from surface EEG recordings that were carried out on five healthy volunteers using a standardized electrode placement scheme. Volunteers were relaxed in an awake state with eyes open (Z) and eyes closed (O), respectively. Sets N, F and S originated from EEG archive of presurgical diagnosis. Segments in set F were recorded from the epileptogenic zone, and those in set N from the hippocampal formation of the opposite hemisphere of the brain. While set N and F contained only activity measured during seizure free intervals, set S only contained seizure activity. Here, segments are se-

lected from all recording sites exhibiting ictal activity.

The data were digitized at 173.61 samples per second using 12 bit resolution. Band-pass filter settings were 0.53 - 40 Hz (12dB/oct). Because the dataset Z included the signals from normal people and S contained signal from epileptic patient's seizure activity. In this paper, two dataset (Z and S) of the complete dataset are used.

4.2 Experiential Results

In this study, the test performance of the classifiers can be evaluated by the computation of sensitivity, specificity and total classification accuracy. The sensitivity, specificity and total classification accuracy are defined as follows:

Sensitivity (A true positive decision): number of positive decisions by computer /number of actually positive cases.

Specificity (A true negative decision): number of negative decisions by computer /number of actually negative cases.

Total classification accuracy: number of correct decisions by computer /total number of cases.

A true negative decision occurs when both the classifier and the physician suggest the absence of a positive detection. A true positive decision occurs when the positive detection of the classifier coincides with a positive detection of the physician. Accuracy, sensitivity and specificity are used as a performance measure.

4.2.1 The Performance of Proposed Algorithm

For the dimension of the raw data set is very high, every sample is divided into 17 sub-samples firstly. So the dimension d of 4096 is reduced to 241. Garber dictionary, which is constructed by equation (2) and (3), are used in sparse representation. The parameters of atoms are chosen from dyadic sequences of integers. Their sampling is governed by extra integer parameters: j ($0 \leq j \leq \log_2 N$, N is signal size), p ($0 \leq p \leq N \times 2^{-(j+1)}$), k ($0 \leq k \leq 2^{(j+1)}$) and i ($0 \leq i \leq 12$). Parameters of Gabor atoms are discretized by the following ways: $\gamma = \{\mu, s, \omega, \varphi\} = \{2^j, 1/2 \text{ ps}, (\pi k)/s, \pi i/6\}$. Every subsample is represented by sparse representation based on MP, and feature vector is formed according to equation (11). Here the number of atoms in Gabor Dictionary N and the number of features for classification which is in direct proportion to the number of selected dictionary atoms for classification M are criti-

cal for classification performance. The number of features for classification is $5 \times M$. The relationship between classification accuracy and the number of features and the size of dictionary will be discussed in 4.2.3. Here, N is set 14638, and M is set 1, so the number of features for classification is 5; 90% sample features are randomly drawn from each class as training sample to train the Bays classifier. The remaining samples are used as test sample. The number of the training samples and test samples are summarized in Table1. All experiments are repeated 1000 times, and the final results are the averaged of them. The classification results are showed in Table2. From it, we can see that the average classification accuracies, sensitivity and specificity could reach 100%, when the size is 14638 and the number of features is 5.

Table 1: The number of the training samples and test samples.

Class	Training set	Testing set	Total
Epileptic	1530	170	1700
Normal	1530	170	1700
Total	3060	340	3400

Table 2: The classification results with proposed methods.

Classification Accuracy / standard variance	Sensitivity	Specificity
100%/0	100%	100%

There are many other methods proposed for the epileptic EEG signal classification. Table 3 presents a comparison on the results between the method developed in this work and other methods. Only methods evaluated in the same dataset are included. The classification accuracies are listed in the table for comparison. From Table 3, it can be seen that the accuracy obtained from our method is the best among the comparison methods.

4.2.2 The Performance of Proposed Algorithm on Noisy Data

In our experience, these EEG segments were selected and cut out from continuous multichannel EEG recordings after visual inspection for artefacts, e.g., due to muscle activity or eye movements. To test the robustness of this method to noise, random white Gaussian noise with increasing level of energy are added to each original signal. The experiences are conducted with the same parameters, pre-processing and algorithms as with the previous subsection. The classification results are showed in Table 4, and decreasing curves of classification accuracies are showed in figure 3.

Table 3: The classification accuracy and the number of features of our method and other methods.

Researchers	Method	Accuracy	Number of input features
Srinivasan et al.	Time & Frequency domain features-recurrent neural network	99.6%	5
Polat et al.	FFT-decision tree	98.72%	129
Nigam and Graupe	Nonlinear pre-processing filter-NN	97.2%	2
Subasi	DWT-mixture of expert model	95%	16
Tzallas	Time frequency analysis-ANN	99%	13
Ling Guo(Guo2011)	GP-based feature extraction-KNN classifier GP-based feature extraction-KNN classifier	99.2%	2.32
This work	Sparse representation of signal—Bays classifier	100%	5

Table 4: The classification results with different levels of white Gaussian noise.

Noise Intensity	Classification Accuracy/ Standard Deviation	Sensitivity	Specificity
Noiseless	100%/0	100%	100%
10%	99.99%/ 0.0027	100%	99.97%
20%	99.73%/ 0.0149	99.46%	100%
30%	99.41%/ 0.0223	98.83%	100%
40%	98.46%/0.0288	96.91%	94.6%

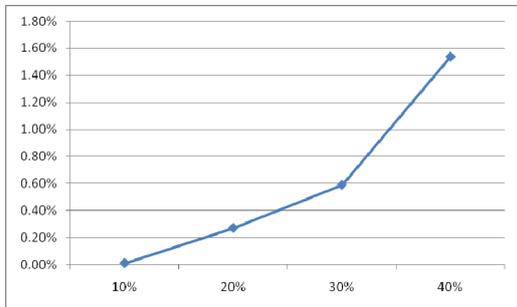


Figure 3: Classification accuracies decreasing curve.

We can see from them, the classification accuracies slightly decline with the increase of noise level. When data is polluted with 10% Gaussian noise, the classification accuracy still could reach 99.99% which decrease only 0.01%; the standard deviation is only 0.0027. Ever if when the intensity of noise reaches 40%, the performance of classifier are still relatively stable.

4.2.3 The Relationship between Classification Accuracy and the Number of Features, the Size of Dictionary

In order to studies the relationship between classification accuracy and the number of features, the size of dictionary separately. In experiences, M is set separately from 1 to 10, and N is set separately as 115804, 32305, 14638, 5889, 3861, 1495, 1001, 806, 715 and 520 which are obtained by different step-length of parameters: j , p , k and i . The classification accuracies are showed in Table 5. Form it, we can see that there are classification accuracies of 100% in every line. This demonstrates that when the size of dictionary is fixed, average classification accuracies could reach 100%, only that the number of features is properly set.

Figure 4 show the relationship between classification accuracy and the number of feature ($5 \times M$) given dictionary size. From it, we can see: (a) when dictionary sizes are 32305 and 14638, the classification accuracies maintain steadily at 100%, no matter how many the atoms are selected for classification; (b) when the size of dictionary are 1495, 1001, 806, 715, and 520, the classification accuracies grow with the number of features increasing, and all reach 100% when M are separately equal or greater than 3, 2, 6, 6 and 7; (c) when the size of dictionary are

115804, 5889 and 3861, the classification accuracies grow with the number of features increasing, and all reach 100% when M are separately 3, 4 and 5; but with the numbers of atoms selected for classification M continue to rise, the right rates decreases.

Figure 5 show the relation between classification accuracy and the size of dictionary given feature number. From it, we can see: (1) when the size of dictionary are equal or greater than 1495, all of the classification accuracy are higher than 99% whatever how many atoms are selected for classification; (2) when the size of dictionary are less than 1495, the accuracies are not stable, and is sensitive to the number of features.

4.3 Discussion

From those experience with noiseless and noise data, we see that when the noise is increased, the accuracy degrades slightly. This indicates that classification features which are constructed by coefficients and atom parameters of sparse representation are robust to noise, thus yield less performance degradation.

The results of Epilepsy Seizure Detection based on sparse representation and Bayesian classifier are

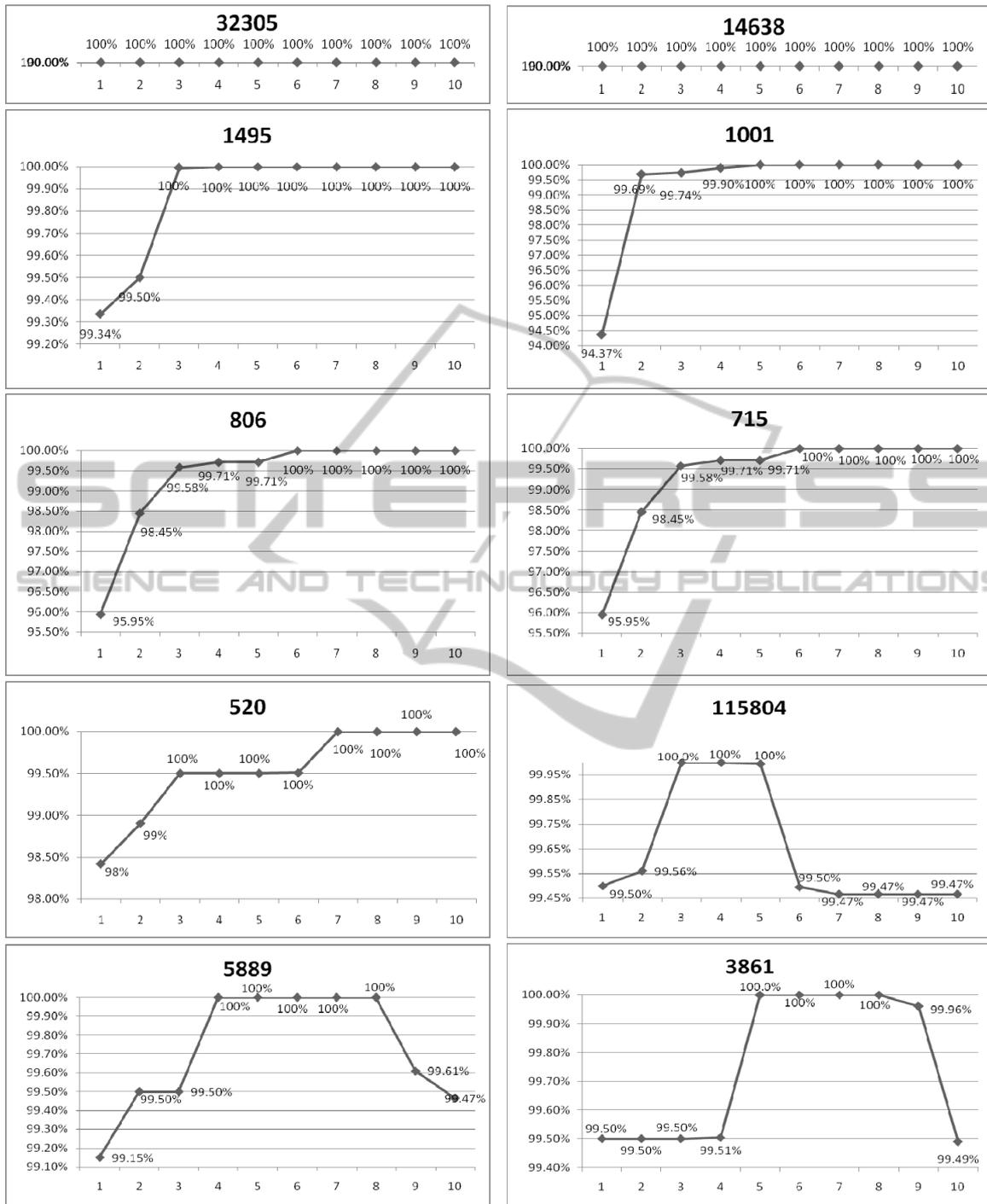


Figure 4: Classification accuracies with different number of atoms selected for classification given dictionary size.

perfect, and are robust to noise only that the proper parameters are set. This is consistent with the theory that sparse representations can capture the inherent structure of signal.

In feature selection based on sparse representation, the size of dictionary N and the number of

atoms selected for classification M are critical. From the results of section 4.2.3, we see the classification accuracies raise with the number of atoms selected for classification increases, most of them could reach accuracies of 100% when M is properly set; however, with M continue to raise, some of classifi-

Table 5: classification right rate based on different number of features and different sizes of dictionary.

Dictionary sizes N	Atom numbers selected for sparse representation M(feature Number=5*M)									
	1	2	3	4	5	6	7	8	9	10
115804	99.50%	99.56%	100%	100%	100%	99.50%	99.47%	99.47%	99.47%	99.47%
32305	100%	100%	100%	100%	100%	100.00%	100.00%	100%	100%	100%
14638	100%	100%	100%	100%	100%	100.00%	100.00%	100%	100%	100%
5889	99.15%	99.50%	99.50%	100%	100%	100.00%	100.00%	100%	99.61%	99.47%
3861	99.50%	99.50%	99.50%	99.51%	100%	100.00%	100.00%	100%	99.96%	99.49%
1495	99.34%	99.50%	100%	100%	100%	100.00%	100.00%	100%	100%	100%
1001	94.37%	99.69%	99.74%	99.90%	100%	100.00%	100.00%	100%	100%	100%
806	95.95%	98.45%	99.58%	99.71%	99.71%	100.00%	100.00%	100%	100%	100%
715	95.95%	98.45%	99.58%	99.71%	99.71%	100.00%	100.00%	100%	100%	100%
520	98.42%	98.91%	99.50%	99.50%	99.50%	99.51%	100.00%	100%	100%	100%

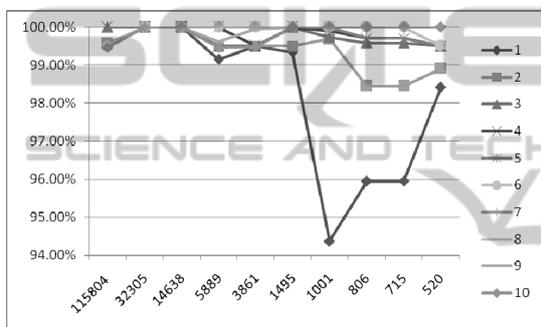


Figure 5: classification accuracies with different size of dictionary given number of features.

classification accuracies decrease. One of the possible reasons for this is that when M is small, the number of features for classification is also small, so the classification accuracies is lower; when M is big enough, the accuracies reach 100%;but when M is too larger, the noise is included into features for classification and result in degrading of the classification accuracies.

Form the results of section 4.2.3, we also can see that when the size of dictionary is large enough, the classifications accuracies are relatively stable, and are less affected by the number of features. However, the larger the size of dictionary is, the longer the time to finding the better atoms for classification in dictionary with MP is; when the size of dictionary is small, the classification accuracies are not stable, in order to obtain higher classification accuracy, the number of features must be increased. Similarly, the bigger the number of features is, the longer the time to finding the better atoms for classification in dictionary and training and testing classifier. So the select of M and N is very critical not only to classification accuracies but also the efficiency of algorithm. Only if the number of features is properly set, the

classification accuracies could be perfect.

Compare with other methods, the classification accuracies is best as illustrated in Table 3. The average accuracy of our method even for noisy data is higher than that of most other methods in Table 3 for non-noise data.

5 CONCLUSIONS

Diagnosing epilepsy is a difficult task requiring observation from the patient, EEG, and gathering additional clinical information. Different etiologies of seizures result in different treatments. In this paper, a new classifier based on sparse representation and Bays classifier is proposed for epileptic seizure detection in EEG. Since sparse representation can capture the inherent structures of signal, the proposed features are relative robust to some noise. In sparse representation, the size of dictionary is very critical to classification accuracies and the efficiency of algorithm. When the size of dictionary is bigger, the classification accuracies are relatively stable and perfect, but the time to finding the better atoms will be long. In the selection of features for classification, the number of features is also critical to classification accuracies and efficiencies of algorithm. The classification accuracies raise with the number of features increases, most of them could reach 100% of accuracies when the number of features is properly set; however, with the number of features continue to raise, some of classification accuracies decrease due to that the atoms representing the noise is included into features for classification. Comparison with the other methods, the accuracy of the proposed method is relatively high. The

classification of normal subjects and epileptic patients were done with the accuracy of 100%, only if when the number of features for classification M and the size of dictionary N are properly set.

Although the proposed method has shown good performance on the EEG signal classification, there still remain some problems to be solved. The speed is relatively slow and the selection of dictionary size and number of features is a key point to classification accuracy. So how to speed up the sparse representation calculation and how to automatically determine the size of dictionary and the number of features suitable to EEG classification are our future work.

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