BAG OF WORDS FOR LARGE SCALE OBJECT RECOGNITION

Properties and Benchmark

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Abstract: Object Recognition in a large scale collection of images has become an important application of widespread use. In this setting, the goal is to find the matching image in the collection given a probe image containing the same object. In this work we explore the different possible parameters of the bag of words (BoW) approach in terms of their recognition performance and computational cost. We make the following contributions: 1) we provide a comprehensive benchmark of the two leading methods for BoW: inverted file and min-hash; and 2) we explore the effect of the different parameters on their recognition performance and run time, using four diverse real world datasets.

1 INTRODUCTION

Object recognition in a large scale collection of images has become an important problem of widespread use. There are currently several smart phone applications that allow the user to take a photo and search a database of stored images e.g. Google Goggles\textsuperscript{1} and Barnes and Noble\textsuperscript{2} apps. These image collections typically include images of book covers, CD/DVD covers, retail products, and buildings and landmark images. Database sizes vary from $10^5$ to $10^7$ images, and they can conceivably reach billions of images. The ultimate goal is to identify the database image containing the object depicted in a probe image, e.g. an image of a book cover from a different view point and scale. The correct image can then be presented to the user, together with some revenue generating information, e.g. sponsor ads or referral links.

It has been shown that bag of words (BoW) approach provides several advantages (Philbin et al., 2007; Chum et al., 2007b; Jégou et al., 2008; Aly et al., 2009b; Chum et al., 2009; Nister and Stewenius, 2006) over the traditional approach of matching local features(Lowe, 2004): acceptable recognition performance, faster run time, and reduced storage. They have been used in image retrieval settings (Philbin et al., 2007; Jégou et al., 2008; Nister and Stewenius, 2006), near duplicate detection (Chum et al., 2007a; Chum et al., 2008), and image clustering (Aly et al., 2009b). The two leading methods for BoW are Inverted File (Zobel and Moffat, 2006) and Min-Hash (Broder et al., 1997; Broder et al., 2000). The former is an efficient exact search method to find nearest neighbors, while the latter is an efficient approximation. Both methods have a lot of parameters and settings that represent trade off between run time and performance. In this work we explore those parameters to assess their effect on the recognition performance and run time.

We make the following contributions:

1. We provide a comprehensive benchmark of the two leading methods for BoW: Inverted File (IF) and Min-Hash (MH) in the object recognition setting.

2. We explore the effect of the different parameters of these methods on the recognition performance and the run time, using four real world datasets with diverse statistics. In particular, we consider the following: IF parameters, MH parameters, dictionary size, dictionary type, and geometric consistency check.

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\textsuperscript{2}http://tinyurl.com/mstn5btinyurl.com/mstn5b
2 METHODS OVERVIEW

In this work we consider the two leading methods of the BoW approach: Inverted File and Min-Hash. They represent different levels of approximation, and differ in how they store the images histograms and in how they perform the nearest neighbor search. The basic BoW idea is described in Algorithm 1. We only provide a brief description of the methods for brevity.

Algorithm 1: Basic Bag of Words Matching Algorithm.

1. Extract features \( \{f_i\} \) from every database image \( i \)
2. Build a dictionary of “visual words”
3. For database images:
   (a) find the corresponding visual word of every feature
   (b) Build a histogram of visual words
4. Build a data structure \( D \) based on these histograms
5. Search the data structure \( D \) for “nearest neighbors”
6. Every nearest neighbor votes for the database image \( i \) it comes from, accumulating to its score \( s_i \)
7. Sort the database images based on their score \( s_i \), and report the top scoring image as the matching image
8. (Optional) Post-process the sorted list of images to enforce some geometric consistency and obtain a final list of sorted images \( s'_i \). The geometric consistency check is done using a RANSAC algorithm to fit an affine transformation between the query image \( q \) and the database image \( i \).

1. **Inverted File (IF).** The images histograms are stored in such a way to provide faster search time (Baeza-Yates and Ribeiro-Neto, 1999; Zobel and Moffat, 2006). The idea is to store for every visual word the list of images that contain it. At run time, only images with overlapping words are processed, and this saves a lot of time and provides exact search results.

2. **Min-Hash (MH).** The histograms are binarized (counts are ignored), and each image is represented as a “set” of visual words \( \{b_i\} \). Then, a number of locality sensitive hash functions (Broder et al., 1997; Broder, 1997; Broder et al., 2000; Chum et al., 2007a) are extracted from the database binary histograms \( \{b_i\} \), and are arranged in a set of tables. The hash function is defined as \( h(b) = \min \pi(b) \) where \( \pi \) is a random permutation of the numbers \( \{1, \ldots, W\} \) where \( W \) is the number of words in the dictionary. At run time, images that have the same hash value are ranked according to the amount of overlap of their binary histograms.

3 EVALUATION DETAILS

3.1 Datasets

We use the same setup as in (Aly et al., 2011). Specifically, we have two kinds of datasets:

1. **Distractors:** images that constitute the bulk of the database to be searched. In the actual setting, this would include all the objects of interest e.g. book covers, ... etc.
2. **Probe:** labeled images, two types per object:
   (a) **Model Image:** the ground truth image to be retrieved for that object
   (b) **Probe Images:** “distorted” images for each object that are used for querying the database, representing the object in the model image from different view points, lighting conditions, scales, ... etc.

Figure 1: Example distractor images. Each row depicts a different set: D1, D2, D3, and D4, respectively, see sec. 3.1.

**Distractor Sets**
- **D1:** Caltech-Covers. A set of \( \sim 100K \) images of CD/DVD covers used in (Aly et al., 2009a).
- **D2:** Flickr-Buildings. A set of \( \sim 1M \) images of buildings collected from http://flickr.com
- **D3:** Image-net. A set of \( \sim 400K \) images of “objects” collected from http://image-net.org, specifically images under synsets: instrument, furniture, and tools.
- **D4:** Flickr-Geo. A set of \( \sim 1M \) geo-tagged images collected from http://flickr.com

Figure 1 shows some examples of images from these distractor sets.

**Probe Sets**
- **P1:** CD Covers. A set of \( 5 \times 97 \equiv 485 \) images of CD/DVD covers.
- **P2:** Pasadena Buildings. A set of \( 6 \times 125 \equiv 750 \) images of buildings around Pasadena, CA from (Aly et al., 2009a).
Figure 2: Example probe images. Each row depicts a different set: P1, P2, P3, and P4, respectively. Each row shows two model images and 2 or 3 of its probe images, see sec. 3.1.

Table 1: Probe Sets Properties and Evaluation Scenarios.

<table>
<thead>
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<th>Table 1: Probe Sets Properties and Evaluation Scenarios.</th>
<th></th>
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<tbody>
<tr>
<td>total</td>
<td>#model</td>
<td>#probe</td>
<td>Scenario</td>
</tr>
<tr>
<td>P1</td>
<td>485</td>
<td>97</td>
<td>388</td>
</tr>
<tr>
<td>P2</td>
<td>750</td>
<td>25</td>
<td>525</td>
</tr>
<tr>
<td>P3</td>
<td>720</td>
<td>80</td>
<td>640</td>
</tr>
<tr>
<td>P4</td>
<td>957</td>
<td>231</td>
<td>724</td>
</tr>
</tbody>
</table>

- **P3**: ALOI. A set of 9×80=640 3D objects images from the ALOI collection (Geusebroek et al., 2005) with different illuminations and view points.
- **P4**: INRIA Holidays. a set of 957 images, which forms a subset of images from (Jégou et al., 2008), with groups of at least 3 images.

Figure 2 shows some examples of images from these distractor sets. Table 1 summarizes the properties of these probe sets.

### 3.2 Setup

We used four different evaluation scenarios, where in each we use a specific distractor/probe set pair. Table 1 lists the scenarios used. Evaluation was done by increasing the size of the dataset from 100, 1k, 10k, 50k, 100k, and 400K. For each such size, we include all the model images to the specified number of distractor images e.g. for 1k images, we have 1000 images from the distractor set in addition to all images in the probe set. Performance is measured as the percentage of probe images correctly matched to their corresponding distractor set. The probe sets were not included in the dictionary generation to avoid biasing the results. All experiments were performed on machines with Intel dual Quad-Core Xeon E5420 2.5GHz processor and 32GB of RAM. We implemented all the algorithms using Matlab and Mex/C++ scripts.

### 4 METHODS PARAMETERS

#### 4.1 Inverted File Parameters

In the Inverted File method, we can use different combinations of histogram weighting, normalizations, and distance functions:

- **Weighting:**
  1. none: use the raw histogram
  2. binary: binarize the histogram i.e. just record whether the image has the visual word or not
  3. tf-idf: weight the counts in such a way to decrease the influence of more common words and increase the influence of more distinctive words

- **Normalizations:** how to normalize the histograms
  1. $l_1$: normalize so that $\sum_i |h_i| = 1$
  2. $l_2$: normalize so that $\sum_i h_i^2 = 1$

- **Distance:**
  1. $d_1$: use the sum of absolute differences i.e. $d_1(h, g) = \sum_i |h_i - g_i|$
  2. $d_2$: use the sum of squared differences i.e. $d_2(h, g) = \sum_i (h_i - g_i)^2$
  3. cos: use the dot product i.e. $d_{cos}(h, g) = 2 - \sum_i h_i \times g_i$. Note that for $l_2$-normalized histograms, this is equivalent to $l_2$ distance since $\|h\|_2 = \|g\|_2 = 1$ and $d_{l2} = \|h - g\|_2^2 = \|h\|_2^2 + \|g\|_2^2 - 2\sum_i h_i g_i$. We consider the following five combinations 

  - \{tf-idf, $l_2$, cos\}: This is the standard way of computing nearest neighbors in IF (Philbin et al., 2007; Philbin et al., 2008).
Figure 3: Effect of Inverted File (IF) Parameters. Results for different weightings, normalizations, and distance functions using dictionaries of 1M words. Recognition performance is measured before any geometric checks, and time represents visual words computation and IF search. See sec. 4.1.

- \{bin, l_1, l_2\}, \{bin, l_1\}: The first was shown to work well with larger dictionaries in (Jégou et al., 2009). The second is a novel one using \( l_1 \) distance.
- \{none, l_1, l_2\}, \{none, l_2\}: These use the \( l_1 \) & \( l_2 \) distance on the raw histograms.

Figure 3 shows results for these different combinations on a dictionary of 1 million visual words computed using the Approximate K-Means (AKM) (Philbin et al., 2007) method. We first note that the run time is similar for all methods. This run time includes both the time to compute the visual words of the features and the time to search the IF. We note that using the standard combination \{tf-idf, \( l_2 \), cos\} is generally inferior to the rest, and quite similar to \{none, \( l_2 \), \( l_2 \}\) i.e. leaving out the tf-idf weighting does not affect performance. We also confirm that using binary histograms yields better performance. We also note that using binary histograms outperforms the standard combination, as shown in (Jégou et al., 2009).

Finally, we note that using the \( l_1 \) distance is generally significantly superior to using cos distance, especially with raw (as reported in (Nister and Stewenius, 2006)) but with binary histograms as well. This might be explained in that it gathers more information, since in the \( d_{cos} \), whenever a word is missing from one image, it is left out of the calculations regardless of whether the other image includes it or not. On the other hand, with \( l_1 \) distance, this information is taken into account.

### 4.2 Min-Hash Parameters

Min-Hash has two parameters: (a) Number of hash functions per table \( H \), and (b) Number of hash tables \( T \). We tried different sizes for hash functions: 1, 2, and 3 and different numbers of tables: 1, 5, 25, and 100. Figure 4 show results for these different settings. Performance is measured after the geometric consistency check, since performance beforehand is significantly worse. Likewise, time represents the total processing time: visual words computation, MH search and RANSAC. It is clear that using more hash tables and less hash functions yields better results, in particular, using 100 tables with 1 function each gives the best overall performance, while the search time is not significantly larger than using 25 tables.

### 4.3 Dictionary Size

The number of visual words in the dictionary affects greatly the recognition performance and run time of the BoW approach. It has been shown that using larger dictionaries, in the order of hundreds of thousands, improves performance and reduces search time in the inverted file. Dictionaries were generated using the Approximate K-Means (AKM) (Philbin et al., 2007) method using random Kd-trees (Arya et al., 1998) to perform an approximate nearest neighbor search. Figure 5 shows results for using \{none, \( l_1 \), \( l_1 \}) combination with dictionaries of sizes 10K, 100K, and 1M visual words. We note that increasing the dictionary size generally increases the recognition performance, specially with harder scenarios like 2 and
4. We also note that with larger dictionaries, the time to compute visual words for features increases slightly (since we are using Kd-trees), however, the time to search the IF decreases. This is intuitive since the number of images with similar words goes down as the number of words increases. This suggests that using larger dictionaries is generally the way to go.

4.4 Dictionary Type

The two leading methods to compute dictionaries with large number of words are:
Figure 6. Effect of dictionary type. Results for using AKM and HKM dictionaries with 1M words. In the bottom row, solid lines represent time to compute visual words, while dashed lines show time to search the inverted file. Performance is measured before any geometric checks. See sec. 4.4.

1. **Approximate K-Means (AKM):** which approximates the nearest neighbor search within K-Means using a set of randomized Kd-trees (Philbin et al., 2007).

2. **Hierarchical K-Means (HKM):** which builds a vocabulary tree by applying K-Means recursively (Nister and Stewenius, 2006) at each node in the tree.

Figure 6 shows results comparing these two methods with 1M words. AKM uses 8 kd-trees with 100 backtracking steps, while HKM uses a tree of depth 6 with a branching factor of 10. Recognition performance for AKM is slightly better than HKM, however, it is at least 10 times slower (note that the time to search the IF is the same for both). This suggests that for time sensitive applications, it is acceptable to use HKM at the expense of a slight decrease in performance.

### 4.5 Geometric Consistency Check

After getting initial candidate matching images from either IF or MH, there is an optional step of re-ranking these images by using geometric consistency of corresponding features. Feature matching is done crudely using the visual words, i.e. features that have the same visual word are considered matched. Other more advanced techniques can be used, for example (Jégou et al., 2008), but here we consider the simplest approach. These feature matches are then used to fit an affine transformation between the probe image and the candidate images using RANSAC (Forsyth and Ponce, 2002). The images are then sorted based on the number of inliers. The geometric step is crucial for MH method, and without it the performance is disastrous.

For IF, it sometimes help, as in scenario 1, and sometimes does not. We believe this depends on the nature of the dataset. For scenario 1, the dataset consists of CD covers with flat art, strong geometric properties, and less clutter. However, this is not the case with the rest of the datasets, especially 2 & 4, which have buildings and other objects of interest surrounded by a lot of clutter e.g. trees, street pavements, sky, clouds, ... etc. This gives the geometric check much harder time and makes the number of inliers for the true match go down by matching also to clutter from other images. This suggests that for some applications, we can do away with the geometric step altogether when using IF. Note also that after the geometric step MH gives performance that is comparable to, but slightly worse than, IF.

### 4.6 Benchmark and Conclusions

Figure 8 shows a comparison of both MH and IF using the best parameters. For IF, we report performance before the geometric step, as it is generally not needed, and for MH we report performance afterwards. We notice that IF gives superior recognition performance and less run time, especially when using $l_1$ distance function, compared to MH.

We note the following:
Figure 7: Effect of the geometric check step. Results for using AKM with 1M words. Top row is recognition performance before the geometric step, and bottom row is after. See sec. 4.5.

Figure 8: Comparison of IF and MH. Top row shows recognition performance, while bottom row shows total matching time per image. Performance reported before the geometric step for IF and after for MH, and similarly for the processing time. See sec. 4.6.

1. Using the $l_1$ distance function in the IF method gives better performance than the other widely used schemes, both with raw and binary histograms. The improvements sometimes exceed 10-15 percentage points over the other distance functions.
2. For Min-Hash, better performance is achieved with more tables and less functions per table.
3. Using larger dictionaries in general helps improve recognition performance and decrease search time in the IF.
4. Performance of AKM dictionaries is generally better than HKM ones, however they are at least 10 times slower. For time sensitive applications, HKM is the way to go, otherwise AKM is a good choice.
5. Geometric consistency checks are indispensable for MH. For IF, it does not always improve the performance, and it depends on the nature of the dataset.
6. Inverted File is superior to Min-Hash in the object recognition setting. It provides much better

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recognition performance and and less run time, specially with larger and difficult datasets. Note in scenarios 2 & 4, performance of IF is around 40% while that of MH is below 5%. This suggests that MH is more suited to near duplicate detection applications.

7. The overall performance of BoW methods is still disappointing. For 400K images, the recognition rate is less than 40% for some scenarios. This suggests that more research is needed to improve the performance of BoW. Possible directions include better ways to generate the visual words, better ways to incorporate geometric information, and to combine information from different features or dictionaries.

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REFERENCES


