COMPLEXITY MEASUREMENT OF PRODUCT MODELS

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Abstract: Complexity management in product development is a challenging task. Modelling the relations in and between partial models from different domains in an integrated semantic product model is a step towards complexity awareness. However it still lacks the quantitative measurement of the overall complexity which can be used to compare product models and control development progress. In this paper we present an approach to evaluate the impact of relations on the overall complexity which results into a complexity measure. The approach is based on a regression model created from a RDF/OWL graph.

1 INTRODUCTION

Developing new products is a critical task for every company in the globalized market. Shortening product lifecycles and customer demands put a high pressure on the project managers. However these projects still often fail or cannot meet their expectations (G. Stevens & Burley 1997) (Cooper 2001, S.9). One of the most frequently named reasons for these failures is the complexity of the project (Lebcir 2006) which is not limited to large scale projects (Wallance u. a. 2004). The well-known canon “You can’t control what you can’t measure” (DeMarco 2004) applies to the aspect of complexity as well. There have been many approaches to make complexity measurable (Bashir & Thomson 1999)(Kearney u. a. 1986). However most of these approaches are limited to one of the previously named aspects and their specific models cannot be adapted to the manifold sources of complexity projects can have.

An integrated product model connects data meaningfully from different perspectives of a product development (Hahn u. a. 2008). By making progress and performance measurable project controlling in new product development projects can be greatly improved. The complexity of the designed product model is a key indicator. In this paper we propose a generic approach for the analysis of product models which quantifies the complexity of design objects and the overall product model. A concrete measure is derived from an individually chosen comparable reference product model. The measure is then defined relative to the reference.

2 COMPLEXITY IN PRODUCT MODELS

Product development involves people from different domains, each contributing with their own view on the product. E.g. project managers, engineers, programmers and usability experts use their own models and the more sophisticated a product is the more views on the product must be considered. E.g. a car is not only modelled in a part structure but also in specialised models such as car electronic model or pedestrian collusion simulation. These partial models make up the overall product model that contains all information on the future product. Because the partial models are heavily interconnected the integrated product model is a complex system of systems. Product Lifecycle Management (PLM) tools use an extended product structure model as meta model for partial models including partial models from other lifecycle phases e.g. maintenance statistics. Ontologies have been considered as basis for PLM models (Mostefai & Bouras 2006) (Borsato u. a. 2010). Recently a W3C incubator group for product modelling using semantics was founded (Böhns u. a. 2009).

Another viewpoint is the domain of systems engineering that deals with the methods necessary for developing and implementing complex systems (R. Stevens 1998). A popular approach in this area
to overcome the complexity of product models is the use of correlation matrices in and between different domain models. Well-known cross-domain examples are the correlation matrices of the Quality Function Deployment method by (Akao 1994) and the additional matrices by (King 1989) that connect domains such as marketing, product structure and process. The design structure matrix (DSM) (Steward 1981) is primarily used for in-domain dependency analysis and optimization but can also be extended to multiple-domain matrices to capture correlations between domains (Danilovic & Browning 2007) (Lindemann u. a. 2008). However DSM matrices are designed as qualitative and not as quantitative model which limits quantitative measurements (Kreimeyer u. a. 2008).

The matrices can also be viewed as equivalent graphs and thus have similarities to ontology graph based product modelling. These models use ontologies to model the concepts and relations of a partial model and corresponding graphs as model instances. E.g. ontology mappings are used by (Tudorache 2006) for consistency checks between partial models.

3 APPROACH

The main goal of the presented approach is to provide a basis for project controlling by providing a reliable key figure. An important aspect of this requirement is the flexibility of providing an adaptable framework that can be tailored to individual project environments rather than a fixed measure. Thus the measure must be suitable for arbitrary partial models. Additionally the measurement process should be automatable. This will not divert the developers from their work and the figures can be included in regular or real-time reports and quality assurance.

Complexity is quantified in terms of effort to address the management of time and resources in project controlling. This implies that complexity is not a negative property of product models but a quantification of product models in terms of development output. This output figure should have a graspable unit rather than be an abstract value to make the impact on the development process clear. E.g. a product model should be quantified by the average time needed to create it.

The subject of the measurement is the integrated product model. The statements in this model represent the knowledge gained about the future product. A simple measure to quantify this model is to count the statements. However the problem is that the statements are differently meaningful. It is necessary to assess their impact on the overall complexity. This can only be done on the semantic level of the partial models. Thus the complexity measure must consider the graph data level as well as the ontology layers of the partial models.

Based on these requirements the basic idea of this approach is to statistically analyse a comparable reference product model to define a relative measure for comparable products. E.g. the reference model can be a cole most helpful for the reader.

1. The procedure as the user sees it.
2. Implementation details of prototype.
3. Abstract graph discussion.

3.1 Create an Integrated Product Model

The first step is to create the reference product model that is used to calibrate the measure. The framework provides transformations from several native formats (Java, STEP, VHDL and MS Project). Other small partial models such as stakeholders can be modeled using OWL editors and imported directly. The partial models still need to be connected to create an integrated semantic product model. This is done using automatic or manual mappings tools. The parsing and mapping of partial models is illustrated in Figure 1.

The framework is implemented as an Eclipse RCP application that provides a Jena based domain independent core component for the management of layered and interconnected RDF models. The native domains models are added to the framework as plugins which define the domain ontology (t-box) and parsers. By choosing a suitable set of plugins the framework can be adapted to different engineering domains. The set of relevant models actually used is an individual choice and should be based on project manager experiences.

The resulting semantic product model is in context of measurement calibration threat as a single graph $G = (V, E)$ consisting of a set of nodes $V$ and a set of labelled directed edges $E$. The nodes are
defined by the models RDF resources and the edges by the statements. RDF collections and n-ary relations modelled using anonymous nodes must be transformed into single statements.

3.2 Annotate Artifact Complexity

As discussed in the previous section complexity is regarded as an output value. This value must be known for the artifacts in the reference product. E.g. program modules or classes can be rated by their authors or if available by cost records in working hours or in dollar or euro units. The value type and unit is arbitrary but should respond to a graspable development input value that the designer can best relate to design elements.

Internally a union copy of the semantic product models partial models is created and some design element classes are defined to be subclasses of the class Artifact. The instances of those classes are annotated with complexity values (see Figure 2).

Each of n artifacts in the weighting model is represented by an equation with \( c(a_i) \) - the defined complexity value of the artifact and \( \beta_1 \ldots \beta_p \) - the set of known property types. The value \( x_{ip} \) is given by the number of values for the property type \( p \) for artifact \( i \). This transformation into a system of linear equations is illustrated in Figure 3. The wizard solves the linear equation system using a linear solver from the Apache Commons mathematics library.

![Figure 2: Step 2 - Annotate artifact complexity.](image1)

The class Artifact defines a subset \( A \subset V \) of the nodes in the graph. In the following the annotated complexity value is described as function \( c(a) \mapsto \mathbb{R} \), \( a \in A \).

3.3 Transform Weighting Model into System of Linear Equations

In this step the annotated graph is used to derive the impact of different property types on the artifacts complexity and thus to define a measure. The framework provides a wizard to perform this step automatically.

The wizard performs a regression analysis on the annotated semantic product model. The analysis is based on the assumption that statement complexity values are additive and that the sum of all complexities of statements of an artifact is the artifact’s complexity. The basic idea is that under this assumption a system of linear equations can be defined with statements complexities as variables on the left hand and artifact complexities on right hand. Thus the model takes the following form:

\[
\beta_1 x_{i1} + \ldots + \beta_p x_{ip} = c(a_i) \quad i = 1, \ldots, n
\]  

(1)

Each of \( n \) artifacts in the weighting model is represented by an equation with \( c(a_i) \) - the defined complexity value of the artifact and \( \beta_1 \ldots \beta_p \) - the set of known property types. The value \( x_{ip} \) is given by the number of values for the property type \( p \) for artifact \( i \). This transformation into a system of linear equations is illustrated in Figure 3. The wizard solves the linear equation system using a linear solver from the Apache Commons mathematics library.

![Figure 3: Step 3 - Transformation into system of linear equations.](image2)

The analysis model created by the wizard represents a multiple linear regression in terms of multivariate statistical analysis. The model consists of a vector of observations \( y(n \times 1) \) on the response variable complexity and a data matrix \( X(n \times p) \) on the explanatory variables property value occurrences. The explanatory variables are also called regressors. The model can be written shortly as matrix formula

\[
X\hat{\beta} + \epsilon = y
\]  

(2)

where variable \( \epsilon \) is the unexplained error. Using the least-square method the best-fitting prediction vector \( \hat{\beta} \) is searched that minimizes the residuals. The residuals are the difference vector between the actual observation vector \( y \) and the predicted vector \( \hat{y} = X\hat{\beta} \). The vector \( \hat{\beta} \) represents the calibrated measure as it can be used against other data matrices from other semantic product models where the complexity values are unknown. The sum of the predicted artifact complexities is according to our notion of complexity the complexity of the semantic product model. The coefficient of determination can be used as quality indicator for the derived measure. However the results still have to be checked for plausibility and validated.

The complexity of an artifact in the semantic product may not only depend on the adjacent vertices or properties. E.g. the complexity of an artifact can depend on the type of requirement (functional or non-functional) the property implements points to. In other domains a cycle path may have a significant impact on complexity, e.g. a property controls. The approach can be extended by a generalization of the regressors used in the regression model. Other artifact measures \( f(a) \mapsto \mathbb{R} \),
a ∈ A can be considered. Regressors can generated from the domain schema ontologies like the property value occurrences regressors are derived from the set of known properties.

4 SUMMARY

This paper proposed a complexity analysis for semantic product models. The structure of semantic product models as a layered graph-based representation of the design partial models was explained. The proposed complexity measure is a relative measure to a reference semantic product model. A concrete measure is derived from the reference model using a regression analysis. The analysis is based on the knowledge about the properties in the domain ontologies.

The approach has been tested with source code and product structure models. Further research includes larger models to test the scalability of the approach. It seems likely that this approach can also be applied to other properties such as maintainability or quality. However, these properties do not have exact the same characteristics as the underlying notion of complexity. Thus we do not have any evidence yet and current work focuses on refinement of the method and improving the support through the framework.

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