Computation Independent Models: Bridging Problem and Solution Domains

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Abstract. Compliance between a problem and a solution domain(s) is a well-known issue in software development. A usual way of development is focusing on the solution, and adapting the solution to the problem domain only in case of occurred issues. Sometimes, the cost of such adaptation is very high, and then the cheapest way is to change operation of the problem domain. Certainly, such ways cannot satisfy a client. This paper considers a computation independent model as a place where overcoming of the gap must occur. It discusses ways for overcoming a gap between a problem domain and a solution domain(s) that are proposed within CIMs, and suggests a mathematical mechanism, continuous mapping, provided by a topological functioning model together with its other topological and functional properties as a formal bridge between those domains. This mechanism is explained by an example.

1 Introduction

Software development begins from analyzing a problem and finding a solution or solutions. In practice, developers design the solution without proper investigation of the problem as they consider that the required solution is this problem mentioned. Therefore, the question about what domain must be modeled at first, the domain of today reality ("system-as-is") or the domain of customer expected reality ("system-to-be"), still is open.

The answer on this question is not new. [17] pointed out that the first step should be evaluating of client’s current situation, and only after that developers should define what the new product will be able to do. He stated that the primary goal of the requirement phase is to notify what client needs. The same thought is repeated in [19] and Jackson’s work [9] at problem frames used for problem analysis. System requirements themselves are only constraints hung on real world phenomena, not vice versa [15].

There are two ways of problem domain analysis. The first one is when developers explore the problem domain by parts, at the beginning trying to understand each fragment of the problem domain and only after that trying to join those fragments together in the joined and more formal representation. The second one is the so called system thinking, where the problem is analyzed at the whole, and only then its fragments are separated and refined.
In both cases mappings between the problem domain and the solution (or solutions) must be determined. System thinking facilitates this issue as the problem domain is analyzed the first, and the solution is defined in accordance with the understood problem. Unfortunately, there is a lack of formal ways to map knowledge about the problem domain into the software development process. However, if we develop this software for some purposes in the real world, we must know how it will affect it. It has critical importance for business, mechatronic and embedded systems, where the cost of the fail could be human lives or vast damages.

Object Management Group’s Model Driven Architecture proposes three models for system specification, namely, a Computation Independent Model (CIM), a Platform Independent Model (PIM), and a Platform Specific Model (PSM). PIMs and PSMs are dedicated for specification of solutions, i.e., systems-to-be. This paper will discuss the first model mentioned, the CIM, where the specification domain (domains) is not so explicit. The CIM describes system requirements and the way the system works within its environment. Details of the application structure and realization are assumed to be hidden or as yet undetermined. The CIM is sometimes called a domain model and a domain vocabulary. However, domains that can be reflected by CIMs are not clearly stated in the specification of MDA [12].

In broad sense we may assume that both problem domain and solution domain can be specified by the computation independent model. And this assumption is correct as it will be shown in this paper. Thus, it is interesting to understand where and how this “gap” between the problem domain and the solution domain can be overcome and by what means.

The paper is organized as follows. Section 2 overviews other authors’ research on CIMs, and analyzes ways of the gap overcoming. Section 3 introduces a formal holistic CIM, i.e., a Topological Functioning Model (TFM) in brief. Section 4 discusses a formal mechanism provided by the TFM and illustrated by an example for overcoming the gap mentioned above. Conclusion summarizes main results of the research.

2 Computation Independent Models

By analyzing scientific publications described below, we have recognized that scientists distinguish three parts or layers within the CIM, namely, CIM – Knowledge Model, CIM – Business Model, and CIM – Business Requirements for the System. Let us consider those proposed models in more detail.

The idea of CIM-Knowledge Model proposed by [5] relates to the highest level of the CIM model levels. This model reflects an enterprise from the holistic point of view, thus providing the general vision of the enterprise with focus on enterprise knowledge. The CIM–Knowledge Model may include three types of diagrams, namely, block, ontological and knowledge diagrams.

Che, Wang, Wen and Ren [3] proposed the similar viewpoint on this level, but they called this model by Global Model. It describes function requirements of every enterprise domain and information transmission relationships between those requirements as well as the whole business logic and information transmission relationships, based on which CIMs at the detailed levels could be composed. Jeary,
Fouad and Phalp [10] discussed a pre-CIM level, where business managers can create informal models of department processes. The pre-CIM may include organizational hierarchies, informal documentation, private process views, details of responsibilities, any requirements relevant information, very informal concept models, etc. In other words, the pre-CIM should hold business domain knowledge, while CIMs holds business process models, and only after that requirements are defined. Garrido, Noguera, González, Hurtado and Rodríguez [4] presented ontology-based CIMs.

The idea of CIM–Business Model proposed by Grangel et al.[5] and Hendryx, [6] is a “pure” business model that is focused on the business scope and goals as well as terminology, resources, facts, roles, policies, rules, organizations, locations and events of concern to the business. However, it does not reflect system considerations. The scope of the Business Model in the CIM must, at a minimum, include business functions served by the system.

Authors in Grangel et al., Kanyaru, Coles, Jeary and Phalp [5, 11], and Garrido et al., [4] defined three possible types of models within the CIM–Business Model. The Organizational Model can be described in terms of goals, organizational structure, analysis diagrams and business rule diagrams. The Structural Model includes product and resource diagrams, and the Behavior Model includes process and service diagrams. Authors in [8] refined them to Organization Model, Process Model, Data Model, System Model, and Service Model. In essence, these models also can be reduced to those three models described previously.

The CIM–Business Requirements for the System proposed in [6] contains the contract between the business and IT about what the business people expect the IS will automate. This model is built on and refers to the CIM–Business Model. Authors in [7] and [18] stated that in case of ISs each requirement is a system’s obligation to execute a business rule or rules. Hence, requirements for the system must be in consistency with the environment where they will be implemented and as complete as possible. Cao, Miao and Chen [2] proposed a use of feature models for developing CIMs. In turn, Trujillo, Soler, Fernández-Medina and Piattini [20] proposed the CIM for requirements analysis for data warehouse modeling based on an extension of the $i^*$ framework that deals only with functional requirements at the business level.

2.1 Overcoming the “Gap” between the Problem and Solution

There are two possible kinds of representing systems. The first and wide-used is fragmental representation. This means that in order to overcome complexity of the system under consideration, developers divide specification of the system from a certain viewpoint into several fragments as in case of use cases, where multiple use cases (fragments) and intuitively and weakly defined dependencies among them constitute this entire view on the system.

The second kind is holistic representation. Holistic representation may be described either as a single indivisible (or formally refined) model or as a view on the system on the whole from different aspects. The latter means that there are formally defined dependencies among elements in aspects.

We believe that only holistic models are able to overcome the gap between the problem domain and solution domains completely. Moreover, such models must be able to represent both domains in order to formally define relationships among them.
In order to overcome the gap between the problem domain and solution domains, requirements must be in conformity with a business model that describes the problem domain. The assisting model should be a business model that specifies the solution domain and is composed in accordance with compliant requirements and reality specified in the business model of the problem domain. In most of the propositions discussed business requirements are stated in accordance with the business model that reflects the solution domain.

Propositions in [5, 10], and [8] have a relation with the business model of the problem domain. In [5] this relation is obtained by selecting those business functions from the “pure” business model of the problem domain that are to be served by the system, and composing corresponding structural and behavioural models. In [10] this relating node is the business process model of the problem domain that is created based on the Pre-CIM (an informal model of business processes, organizational hierarchies, informal documentation and very informal concept model) and on which business requirements for the system are grounded. In [8] the joining element is the business context and business requirements for the enterprise integration system. This context defines existing organization, services, processes and data, and specifies requirements for the integration system.

Summarizing, the proposed ways of overcoming the gap mentioned before are rather intuitive then formal. Even if functions of the solution domain are obtained by selection from functions of the problem domain, it is not clear how new functions must be handled in order to keep conformity among two domains or how exclusion of problem domain functions in the solution domain will affect enterprise operation.

In our paper we present the Topological Functioning Model (TFM), which is a formal mathematical model for holistic (single indivisible) representation of both problem and solution domains and provides a mathematical mechanism for overcoming the gap between a problem and a solution.

3 The Formal Holistic CIM - Business Model: Topological Functioning Model

A Topological Functioning Model (TFM) is developed at Riga Technical University by Janis Osis [13]. The topological model of problem domain is the advantage for analysis and decomposition of complex systems as described in [14].

The TFM is a mathematically formal model that describes a topology among systems functional properties from the computation independent viewpoint. It is independent of any modeling and implementation technique. It comes about through the acquisition of the experts' knowledge about the complex system, verbal description, and other documents concerning the structure and functioning.

TFM formalism is based on assumption that a complex system can be described in abstract terms as a topological space \((X, Q)\), where \(X\) is a finite set of functional features and \(Q\) is a topology, given in the form of a digraph (oriented graph).

A functional feature is a characteristic of the system (in its general sense) that is designed for achieving some system’s goal. The functional features are activities that help the system to realize its functionality. These activities can be considered as (specialized) functional features [13], i.e., functional features, whose further
expansion is not necessary at this stage. Functional features can be joined in a functional feature set, representing a certain business function. Therefore, a set of specialized functional features can be correlated with the appropriate business function and corresponding business process.

Cause-and-effect relations among functional features (or topology) must be set. It is assumed that a cause-and-effect relation between two functional features of the system exists if the appearance of one feature is caused by the appearance of the other feature without participation of any third (intermediary) feature.

The TFM has topological and functional properties [13]. The topological properties are connectedness, closure, neighborhood and continuous mapping. The functional properties are cause-effect relations, cycle structure, inputs and outputs.

4 Continuous Mapping: The Bridge between Problem Domain and Solution Domain Models

This paper highlights one of TFM topological properties, namely, continuous mapping, which together with other TFM topological and functional properties allows overcoming the gap between the problem and solution.

Fig. 1 illustrates a use of the topological functioning model in software development. First, a model of the problem domain is constructed by analyzing knowledge of the system-as-is. Simultaneously client’s requirements (or desires) are gathered. They are checked up for compliance with the constructed TFM and mapped onto its functional features. The result is a topological functioning model of the solution domain that implements continuous mapping into the TFM of the problem domain. However, we should note that this is a model of the solution domain at the business level not at the application level. The application level is specified in the CIM – Business Requirements for the System that is a behavior model in this case.

4.1 Mathematical Foundations of the Continuous Mapping

According to the statement and corollaries of continuous mapping defined in [13], the model with any complexity can be abstracted to the simpler one and vice versa. This means that continuous mapping of topological models is realized. Continuous mapping states that direction of topological model arcs must be kept as in a refined as in a simplified model. Moreover, a lack of knowledge about the system can be filled up with knowledge that is obtained from the continuous mapping of the same type model to the system model under consideration.

Statement: If some more detailed functioning system is formed by substitution of a subset of specialized properties for some functional property, then continuous mapping exists between a detailed model and a simplified parent topological model of the same system.

Proof: The continuous mapping of the topological space of the detailed system $T^*$ into the topological space of the simple parent system $T$ will take place, if neighborhoods of $T^*$ will map into neighborhoods of $T$. 
Let us assume that the contrary is the case, i.e., that neighborhoods of $T^*$ are not mapped into neighborhoods of $T$. This means that $T^*$ possesses other essential topological properties. Therefore, either the mode of functioning of the detailed system will be different, or the detailed system will cease to exist at all. It follows that new essential functional features are being added but it contradicts to the premise of the statement. It’s easy to prove also the converse statement.

### 4.2 Discussion

Let us explain and demonstrate the theoretical foundations mentioned above by an example of a library.

Let us assume that we have the following description of the problem domain, i.e., a fragment of operation “as is” of this small enterprise: “The library invites people to come. The Advertising Company gives the informational support for the library. When a reader comes, he is serviced by a librarian. Each month and after taking back the librarian evaluates the condition of used prints. If a print is damaged, then it is either restored by the Restoration Company or removed by the Liquidating Company. The removed prints are liquidated by the Liquidating Company, while the library continues to use the restored prints. Library’s Fund Company gives the financial support that is based on annual library’s reports. The Library’s Fund Company itself is credited by its partners. Library’s fund gets this financial support. The library distributes the obtained income among paying salaries to employees, restoring prints, removing damaged prints and purchasing prints. Each three months the library purchases prints which are published by publishing houses in order to service their readers. Before each purchase, the library evaluates readers’ requirements as well the condition of library’s prints. The library gives the information support by fee.”

The topological functioning model of this library illustrated in Fig. 2-a is constructed in accordance with a method that is described in detail in [16].
Description of functional features that is a simplified form of the description in [1] is the following:  

**<label: name, preconditions, postconditions>:**  

- **a:** Publishing a print;  
- **b:** Coming a reader;  
- **c:** Purchasing a print;  
- **d:** Servicing a reader, **postcondition** "income";  
- **e:** Evaluating the condition of a print, **precondition** "each month and after tacking back a print", **postcondition** "damaged OR undamaged condition";  
- **f:** Evaluating the requirements of a reader, **postcondition** "reader’s requirements";  
- **g:** Restoring a print, **precondition** "if a print is damaged";  
- **h:** Distributing income;  
- **i:** Giving financial support, **precondition** "if it is a review of library’s annual report", **postcondition** "income";  
- **j:** Paying the salary to an employee;  
- **k:** Giving informational support;  
- **l:** Creating a report, **precondition** "if it is a deadline of annual report submission";  
- **m:** Inviting a man;  
- **n:** Crediting library’s fund company

Let us assume that a client wants to receive an information system (IS) that supports functions dedicated to servicing readers, i.e. the following functional requirements for the IS are set:  

- **F1:** The system shall provide servicing readers (functional feature **d**);  
- **F2:** The system shall provide evaluating print conditions (functional feature **e**);  
- **F3:** The system shall provide restoring a print (functional feature **g**);  
- **F4:** The system shall provide paying for print damages.

Here, **F1** completely corresponds to functional feature " **d:** Servicing a reader, **postcondition** \{income\}";  
**F2** completely corresponds to functional feature " **e:** Evaluating the condition of a print, **precondition** \{each month\}, **postcondition** \{damaged OR undamaged condition\}"; and **F3** completely corresponds to functional feature " **g:** Restoring a print, **precondition** \{if a print is damaged\}".

In turn, **F4** does not correspond to any existing functional feature in the TFM of the problem domain. This means that this requirement will introduce new functionality as in the solution domain (the IS itself) as in the problem domain (operation of the library as an enterprise). This case requires careful investigation of cause and effect relations among the existing functional features in the problem domain and this new one.

In order to introduce this new function into the TFM of the problem domain, we have created new functional feature " **r:** Paying for the damage of a print, **precondition** \{if a print is damaged\}". By analyzing existing functionality, we can assume that the cause is functional feature **e**, and an effect is functional feature **d**. If the cause is evident, then the effect is implicitly stated. We may assume that if a reader has not paid for damages done, then he/she will not be able to get library’s services next time (Fig. 2-b).

The IS to be implemented is a subsystem of the library system. Hence, we can separate the topological functioning model of the IS from the model of the library. Accordingly to the rules of separation of the topological model from the topological space that is illustrated in detail in [16], after the closing operation we have obtained the topological functioning model of library’s IS (Fig. 2-c).

Functionality described by functional features **d**, **e**, and **g** that are specified for implementation already exists in the library as an enterprise (Fig. 2-a). But the function that supports paying for damaged prints and that will be implemented in the IS modifies operation of this enterprise by introducing this new responsibility, functional feature **r**, as it is shown in the TFM in Fig. 2-b and Fig. 2-c.

Continuous mapping from the TFM of the information system to the TFM of the library with the IS ("to be") to the TFM if the library without the IS ("as is") is
mathematically proved by mappings of the neighborhoods of the system functional features, where $X_{i}^{**}$ is a neighborhood of the functional feature of the IS (Fig. 2-c), $X_{i}^{*}$ is a neighborhood of the functional feature of the library with the IS (Fig. 2-b), and $X_{i}$ is a neighborhood of the functional feature of the library without the IS (Fig. 2-a):

$$
\begin{align*}
X_{i}^{**} &= \{b, d\} \rightarrow X_{i}^{*} = \{b, d\} \rightarrow X_{i} = \{b, d\} \\
X_{i}^{**} &= \{c, d\} \rightarrow X_{i}^{*} = \{c, d\} \rightarrow X_{i} = \{c, d\} \\
X_{i}^{**} &= \{d, f, h, c\} \rightarrow X_{i}^{*} = \{d, f, h, c\} \rightarrow X_{i} = \{d, f, h, c\} \\
X_{i}^{**} &= \{e, r, i, g\} \rightarrow X_{i}^{*} = \{e, r, i, g\} \rightarrow X_{i} = \{e, i, g\} \\
X_{i}^{**} &= \{h, g\} \rightarrow X_{i}^{*} = \{h, g, k, c, i, l, m\} \rightarrow X_{i} = \{h, g, k, c, i, l, m\} \\
X_{i}^{**} &= \{g, d\} \rightarrow X_{i}^{*} = \{g, d\} \rightarrow X_{i} = \{g, d\} \\
X_{i}^{**} &= \{k, d\} \rightarrow X_{i}^{*} = \{k, d\} \rightarrow X_{i} = \{k, d\} \\
X_{i}^{**} &= \{r, d\} \rightarrow X_{i}^{*} = \{r, d\} \rightarrow \emptyset
\end{align*}
$$

The mappings between the neighborhoods explicitly demonstrate that functional feature $r$ is not continuously mapped to the initial TFM of the library (the system “as is”), because it is a new function for the library. However, it is continuously mapped from the model of the information system to the modified TFM of the library, thus the solution is in compliance with the problem domain.
5 Conclusions

Discovering gaps between the problem domain and the solution domain is an open issue in software development. The CIM is the only model within model-driven development that can specify both these domains and should show such issues explicitly. Analysis of the existing proposition of CIMs shown that even if both domains are modeled in the CIM, the relation among them is rather intuitive then formally defined and specified. This is a cause of future issues with solution’s inadequacy to the enterprise operation.

This paper illustrated the mathematical mechanism for such inadequacy identification and handling. The mechanism is TFM topological and functional properties that support continuous mapping between the system and its subsystems, and the system and its modifications. Discovered gaps between domains are explicit and mathematically proved, and possible changes in the system functionality are done taking onto account already existing interrelationships among system functions. This mechanism is planned to be implemented in the modeling tool to be developed.

References