Keywords: Process Mining, Workflow, Incremental Mining.

Abstract: A number of process mining algorithms have already been proposed to extract knowledge from application execution logs. This knowledge includes the business process itself as well as business rules, and organizational structure aspects, such as actors and roles. However, existent algorithms for extracting business processes neither scale very well when using larger datasets, nor support incremental mining of logs. Process mining can benefit from an incremental mining strategy especially when the information system source code is logically complex, requiring a large dataset of logs in order for the mining algorithm to discover and present its complete business process behavior. Incremental process mining can also pay off when it is necessary to extract the complete business process model gradually by extracting partial models in a first step and integrating them into a complete model in a final step. This paper presents an incremental algorithm for mining business processes. The new algorithm enables the update as well as the enlargement, and improvement of a partial process model as new log records are added to the log file. In this way, processing time can be significantly reduced since only new event traces are processed rather than the complete log data.

1 INTRODUCTION

Process mining aims extracting information from system event logs to discovery a business process based on its execution. Some examples of systems include workflow management systems, enterprise resource planning systems, customer relationship management, B2B systems, legacy systems, etc. This approach can also be used to compare both the captured and the designed business process in order to identify discrepancies in the model (van der Aalst, 2003).

Additionally to process mining algorithms, there are several other algorithms and methods for the extraction of business processes from information systems (e.g. Machine Learning, Source Code Analysis, etc). Techniques based on static source code analysis (Zou, 2006) (Zou, 2004), (Liu, 1999) usually extract the business process directly from the source code constructions (e.g. if and while statements, functions calls, etc). Thus, the final process model presents a similar structure as the source code. The problem here is that they seldom identify more complex constructions like parallelism and process participants. The main reason for this limitation is that this kind of information cannot be gathered from the static analysis of the source code alone, but needs a dynamic behavior analysis of the system additionally. Existing process mining algorithms (Ren, 2009), (Alves and Medeiros, 2007), (Weijters, 2006) extract information about process behavior directly from system execution logs (i.e. see Fig. 1). They can identify simple as well complex control flow structures (e.g., XOR/AND-split/join, activity participants) through the dynamic behavior analysis of the system.

![Figure 1: Overview of process mining.](image)

Although actual process mining algorithms are very effective for the extraction of business processes, they still present some limitations. The main limitations are (i) they do not scale very well during the mining of large execution logs and (ii) do not support the incremental mining of these logs. Large log files might be necessary when a
significant number of different as well as complex execution scenarios occur in the business process. In such cases, the complete behavior of the system can only be approximated by mining an ever growing dataset of executions. So, in these cases an incremental mining could extract partial results from the log and also execute the mining process in a more efficient way.

In this paper, we propose an incremental process mining algorithm, the IncrementalMiner, as an extension of the Heuristic Miner (Weijters, 2006) with support to incremental mining of execution traces, as showed in Fig 2. The main reason of relying upon the Heuristic Miner in spite of other existing mining algorithms, e.g., alpha++ (Wen, 2006) and Genetic Miner (Alves de Medeiros, 2007), is basically its satisfactory accuracy as well as its support in extracting all business process constructions (e.g., XOR/AND-split/join, loops, activities participants, etc).

![Figure 2: Incremental Process Mining from execution logs of information systems.](image)

The remainder of this paper is organized as follows. Section 2 introduces basics concepts related to process mining that are used throughout the paper. Section 3 provides a detailed discussion on the IncrementalMiner algorithm. In section 4, we evaluate the performance of the new algorithm and comment on the quality of the extracted models. Section 5 we introduce the works related to this research. Section 6 presents conclusions and outlook.

2 BASIC CONCEPTS

An event log can be defined as follows. Let $T$ be a set of process activities. $\sigma \in T^*$ is an event trace, i.e., an arbitrary sequence of activity identifiers. $W \subseteq T^*$ is an event log, i.e., a multiset (bag) of event traces, where every event trace can appear many times in a log.

To find a process model on the basis of an event log, the log must be analyzed for causal dependencies, e.g., if an activity is always followed by another activity, it is likely that there is a dependency relation between both activities. To analyze these relations, Weijters (Weijters, 2006) introduces the following notations. Let $W$ be an event log over $T$, i.e., $W \subseteq T^*$. Let $a, b \in T$:

1) $a > w b$ iff there is a trace $\sigma = t_1, t_2, ..., t_i$ and $i \in \{1, ..., n-1\}$ such that $\sigma \in W$ and $t_i = a$ and $t_{i+1} = b$. The relation $> w$ in this notation describes which activities appeared in sequence.

2) $a \rightarrow wb$ iff $a > wb$ and $b \not> w a$. The relation $\rightarrow w$ represents the direct dependency relation derived from event log $W$.

3) $a \| w b$ iff $a > wb$ and $b > wa$. The relation $\| w$ suggest potential parallelism between $a$ and $b$.

4) $a > w b$ iff there is a trace $\sigma = t_1, t_2, ..., t_n$ and $i \in \{1, ..., n-2\}$ such that $\sigma \in W$ and $t_i = a$ and $t_{i+1} = b$ and $t_{i+2} = a$. This relation suggest a short loop between $a$ and $b$.

3 ON THE INCREMENTAL MINER ALGORITHM

IncrementalMiner incrementally mines the control flow perspective of a business process from execution log files of this process. Incremental mining happens when several partial event logs are processed one by one improving the completeness of model. Table 1 shows an example of two event logs. The first one (Table 1a) contains the initial events generated by the first execution of a system. Each row in the table represents the events generated by the execution of one process instance. The second event log (Table 1b) contains additional and complementary events generated by new executions (i.e. the last row on Table 1b).

<table>
<thead>
<tr>
<th>ID</th>
<th>Trace</th>
</tr>
</thead>
<tbody>
<tr>
<td>1-9</td>
<td>A–C–B–D</td>
</tr>
<tr>
<td>10-19</td>
<td>A–E–D</td>
</tr>
<tr>
<td>20</td>
<td>A–B–C–E–D</td>
</tr>
<tr>
<td>21</td>
<td>A–E–C–B–D</td>
</tr>
</tbody>
</table>

(a) Partial log of event traces

<table>
<thead>
<tr>
<th>ID</th>
<th>Trace</th>
</tr>
</thead>
<tbody>
<tr>
<td>1-9</td>
<td>A–C–B–D</td>
</tr>
<tr>
<td>10-19</td>
<td>A–E–D</td>
</tr>
<tr>
<td>20</td>
<td>A–B–C–E–D</td>
</tr>
<tr>
<td>21</td>
<td>A–E–C–B–D</td>
</tr>
<tr>
<td>22-30</td>
<td>A–B–C–D</td>
</tr>
</tbody>
</table>

(b) Final log of event traces

3.1 Incremental Process Mining

The process that incrementally generates the log
starts with the definition of test case scenarios (i.e. Fig. 2a). These scenarios coordinate which functionalities of the system are executed. As the application is executed (i.e. Fig. 2b), new entries are added to the log. The IncrementalMiner algorithm can be executed at any time to handle these new entries (i.e. Fig. 2c). As a result, it either creates a new model (from scratch) at the first time, or it updates already created process models at each time it is executed (i.e. Fig 2d).

The incremental mining of logs allows more flexibility to extract business process since only specific processes could be selected, executed and mined from the events log. So, this fact reduces the total processing time of the mining since only new trace entries are processed rather than the complete log data when new processes must be considered.

3.2 The Algorithm Definition

This section gives an overview of the IncrementalMiner algorithm. We separated the algorithm in five distinct pseudo codes, as showed below.

Algorithm 1: IncrementalMiner.
1. for every new instance \( \sigma \in L \)
   (a) for every event \( e_i \in \sigma \)
      (i) \( e_i = e_1, e_2 = e_{i-1} \)
      (ii) \( \text{Process Relation}(e_i, e_2, e_3) \).
2. Calculate confidence \( a \Rightarrow wb \) of rel\((e_i, e_2)\).
3. If \( e_1 \) equal \( e_2 \) then
   (a) Calculate short loop size \( 1 \) confidence \( a \Rightarrow wb \) between \( e_1 \) and \( e_2 \).
   (b) If the Support of rel\((e_i, e_2)\) is above Loop1 threshold then
      (i) AddRelationToGraph\((e_i, e_2)\).
4. Else if \( e_1 \) equal \( e_3 \) then
   (a) Calculate short loop size \( 2 \) confidence \( a \Rightarrow w2b \) between \( e_1 \) and \( e_3 \).
   (b) If support of rel\((e_i, e_3)\) is above Loop2 threshold then
      (i) AddRelationToGraph\((e_i, e_3)\).
5. Update rel\((e_i, e_3)\) in the dependency tree of \( e_i \) element.
6. Update split/join relation Confidence \( a \Rightarrow wbc \) for \( e_i, e_2 \) and \( e_3 \).
7. UpdateBestRelation\((e_i, e_2, \text{bestDependenciesTreeOf}(e_i))\).
8. UpdateBestRelation\((e_i, e_3, \text{bestCausesTreeOf}(e_i))\).
9. If rel\((e_i, e_2)\) is the best dependency relation of \( e_i \) or rel\((e_i, e_3)\) is the best cause relation of \( e_i \) then
   (a) AddRelationToGraph\((e_i, e_2)\).
Algorithm 3: UpdateBestRelation\((e_i, e_2, \text{relationTree})\).
1. If Confidence of rel\((e_i, e_2)\) is less than Confidence of relations in relationTree then
   (a) RemoveRelationFromGraph\((e_i, e_2)\).
2. Else
   (a) If Confidence of rel\((e_i, e_3)\) is greater than relations Confidence in relationTree then
      (i) For each old best relation in relationTree: (x) Remove old best relation from relationTree.
      (y) RemoveRelationFromGraph\((\text{firstElementOf(old best rel)}, \text{secondElementOf(old best rel)})\).
   (b) Add r to the relationTree.

Algorithm 4: AddRelationToGraph\((e_i, e_2)\).
1. Add vertex\((e_i)\) and vertex\((e_2)\) to the dependency graph.
2. Add edge\((e_i, e_2)\) to the dependency graph.

Algorithm 5: RemoveRelationFromGraph\((e_i, e_2)\).
1. Remove edge\((e_i, e_2)\) from dependency graph.
2. If vertex\((e_i)\) does not contain incoming and outgoing edges then
   (a) Remove vertex\((e_i)\) from dependency graph.
3. If vertex\((e_2)\) does not contain incoming and outgoing edges then
   (a) Remove vertex\((e_2)\) from dependency graph.

To exemplify how IncrementalMiner works, consider the partial log \( W = \{\text{ACBD}^2, \text{AED}^3, \text{ABCD}^2, \text{AECD}^2\} \) (i.e. the log presented in the Table 1a). For every three consecutive events in the trace (e.g., events A, C, B in the trace ACBD), the algorithm IncrementalMiner applies heuristics to them to extract valid relations. The first heuristic to be applied is the dependency relation (i.e. Algorithm 2, item 2) between the first and second element of the tuple (e.g. A and C). Let \( W \) be an event log on \( T \), and \( a, b \in T \). Then \( a \Rightarrow wb \) is the number of times \( a > wb \) occurs in \( W \), and:

\[
a \Rightarrow wb = \frac{|a > wb| - |b > wa|}{|a > wb| + |b > wa| + 1}
\]

This above heuristic calculate the Partial Confidence (i.e. the Confidence value until this iteration of algorithm) of this relation, using the support of \( a > wb \) (e.g. number of times that A comes before C) and the support of \( b > wa \) (e.g. number of times that C comes before A). In the example, \( a \Rightarrow wb = (1-0) / (1+0+1) = 0.5 \). After iterating all log traces in our example, the value of \( a \Rightarrow wb \) is (9-0) / (9+0+1) = 0.900. The calculated values are inserted into the Dependency Tree of Figure 3 (i.e. see node C, in the dependency tree of A). This dependency tree is an AVL tree that keeps the actual candidate relations (i.e. relations that could be considered in the final graph of process) together with their Confidence and Support values.
respectively. The next two heuristics below verify the occurrence of short loops in the trace (item 3 of Algorithm 2). That is, it checks the existence of an iteration composed by either $e_1$ or $e_2$ and $e_2$ (e.g. AA or ABA). Let $W$ be an event log over $T$, and $a, b \in T$. Then $|a >_{wb} a|$ is the number of times $a >_{wb} a$ occurs in $W$, and $|a >_{wb} b|$ is the number of times $a >_{wb} b$ occurs in $W$:

$$ a \Rightarrow wa = \frac{|a > wa|}{|a > wa| + 1} \quad (2) $$

$$ a \Rightarrow 2wb = \frac{|a >> wb| - |b >> wa|}{|a >> wb| + |b >> wa| + 1} \quad (3) $$

The next heuristic (i.e. heuristic 4) is used by algorithm 2 (i.e. item 6) to verify the occurrence of non-observable activities in the log (i.e. AND/XOR-split/join elements). Let $W$ be an event log over $T$, and $a, b, c \in T$, and $b$ and $c$ are in depending relation with $a$. Then:

$$ a \Rightarrow wb^c = \frac{|b > wc| + |c > wb|}{|a > wb| + |a > wc| + 1} \quad (4) $$

The $|a > wb| + |a > wc|$ represent the number of positive observations and $|b > wc| + |c > wb|$ represent the number of times that $b$ and $c$ appear directly after each other. Considering the event log example, the value of $a \Rightarrow wb^c = (1 + 0) / (11 + 9 + 1) = 0.05$ indicates that $E$ and $C$ are in a XOR-relation after activity $A$ (i.e. high values to $a \Rightarrow wb^c$ indicates a possible AND-relation and low values a XOR-relation).

All heuristics defined above are used to calculate the candidate relations that can be added to the dependency graph of the business process (i.e., the best relations graph, represented in Fig. 5). To select the candidate relations that will compose the graph, we use the best relations trees (see Fig. 4).

The algorithm 3 is used to update these best relation trees. These trees keep the best dependency and causal relations of the dependency tree (i.e. the relations with highest Confidence value). A best relation tree can have several relations with high confidence value inside it, but all relations in it must have the same confidence value for that element.

The final dependency graph is similar to the one of Fig. 5a. We need yet to process the second log file in its last state (see Table 1b). From this log file we obtain the multiset $W = \{ACBD, AED, ABCD, AECBD, ABCD\}$. After applying IncrementalMiner to this log, we obtain the final dependency graph of Fig. 5b. This graph shows additional structures which were extracted from the new trace $ABCD$ (i.e. nine occurrences of it) available in the last events of the log. All the other traces available in the log (i.e. also available in the first log) are discarded by the algorithm. This happens since the IncrementalMiner maintains a list of already processed event traces (column ID in Table 1 can be used for this control).

### 3.3 Using Threshold to Deal with Noise

Additionaly to the best relations tree, IncrementalMiner uses all thresholds defined in HeuristicMiner algorithm to decide whether a relation will be considered in the final dependency graph (see items 3.(b), 4.(b) and 9 of Algorithm 2). These thresholds help preventing the generation of false relations caused by noise. Thus, we can also accept dependency relations between activities that have (i) a dependency measure above the value of the Dependency threshold, and (ii) have a frequency higher than the value of the Positive observations
threshold, and (iii) have a dependency measure for which the difference with the “best” dependency measure is lower than the value of Relative to best threshold (Weijters, 2006).

4 PERFORMANCE EVALUATION THROUGH A CASE STUDY

The experiments have been divided into two groups. The first group compared the performance results using the IncrementalMiner and other existent algorithms. The second group was used to compare the quality of models discovered by the process mining algorithms.

4.1 Generating Event Log from Legacy System Execution

For all experiments discussed here, we used datasets generated through successive executions of an information system, following the process defined in Fig. 2. In the end, a large dataset with approximately 10,000 event trace instances were generated. In the experiments we used a PC with an Intel Core 2 Duo 2GHz processor and 2GB RAM. The IncrementalMiner algorithm was implemented using Java language.

4.2 Performance Analysis

To test the performance of the incremental feature of the IncrementalMiner, we collected five event trace log files. The files were recorded with complementary contents and named respectively as A, B, C, D and E where \( A \subseteq B \subseteq C \subseteq D \subseteq E \).

Table 2: IncrementalMiner time comparative (in seconds). Row A: mining of all log content. Row B: incremental mining of log content. * In thousands of instances.

<table>
<thead>
<tr>
<th>Instances*</th>
<th>2</th>
<th>4</th>
<th>6</th>
<th>8</th>
<th>10</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>1.4</td>
<td>2.7</td>
<td>4.0</td>
<td>5.4</td>
<td>6.7</td>
<td>20.2s</td>
</tr>
<tr>
<td>B</td>
<td>1.4</td>
<td>1.5</td>
<td>1.4</td>
<td>1.5</td>
<td>1.5</td>
<td>7.2s</td>
</tr>
</tbody>
</table>

The obtained results can be seen in Fig. 6 below. IncrementalMiner processed the complete dataset five times faster (500%) than Alpha++ and eighty times faster than HeuristicMiner (8000%). Furthermore, Table 2 shows the total processing time reduction with IncrementalMiner. Rows A and B sum the total processing time to process the log content without the incremental approach and with it, respectively. At the end we obtained a gain of 64% on total processing time using incremental mining of datasets.

4.3 Quality Analysis

Table 3: Quality Metrics Comparative between IncrementalMiner (IM), HeuristicMiner (HM), Genetic Miner (GM) and Alpha++ miner.

<table>
<thead>
<tr>
<th>Metric</th>
<th>IM/ HM</th>
<th>GM</th>
<th>A+</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fitness Parsing Measure PM</td>
<td>1</td>
<td>1</td>
<td>0.006</td>
</tr>
<tr>
<td>Token Based Fitness (f)</td>
<td>1</td>
<td>1</td>
<td>0.926</td>
</tr>
<tr>
<td>Fitness (PF_{\text{complete}})</td>
<td>1</td>
<td>1</td>
<td>0.728</td>
</tr>
<tr>
<td>Behavioral Appropriateness (a)</td>
<td>0.78</td>
<td>0.98</td>
<td>0.720</td>
</tr>
<tr>
<td>Behavioral Precision (Bp)</td>
<td>1</td>
<td>1</td>
<td>0.907</td>
</tr>
<tr>
<td>Behavioral Recall (Br)</td>
<td>1</td>
<td>1</td>
<td>0.907</td>
</tr>
<tr>
<td>Causal Footprint</td>
<td>0.99</td>
<td>1</td>
<td>0.96</td>
</tr>
<tr>
<td>Structural Appropriateness (a)</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Structural Precision (S_p)</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Structural Recall (S_r)</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Duplicates Precision (D_p)</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Duplicates Recall (D_r)</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

This quality comparison followed the quality metrics defined in (Rozinat, 2007a). Such metrics describe several measurements to assess the quality of a model based on the behavior observed in the execution log. According to Rozinat (Rozinat, 2007a), a value can be considered a “good metric” if it is near or equal to “1”.

To execute these experiments, we have used the Control Flow Benchmark plug-in of the ProM tool (van Dongen, 2005b). Table 3 presents the result of this analysis. We observed that all discovered
models except the models returned by Alpha++ miner fit the log and have good precision. The details of each metric can be seen in the work of Rozinat.

5 RELATED WORK

The first group of related work includes process mining algorithms. They allow the mining of execution traces of a system to extract information, as business processes, aspects of organizational structures and types of business rules (van der Aalst, 2003). Related to that, one of the main algorithms is the Genetic Miner. It uses adaptive search methods that simulate the evolution process. This algorithm presents better accuracy when compared with other existing ones (e.g., Petrify Miner, Alpha++, etc). However, existing algorithms do not consider the incremental mining of business process from the event log, using only historical data logs.

The source code analysis approach proposed in (Zou, 2004) represents a model driven business process recovery framework that captures the essential functional features represented as a business process. In another work, Zou (Zou, 2006) compares the structural features of the designed workflow with the implemented workflow, using an intermediate behavioral model. Finally, Liu (Liu, 1999) uses a requirements recovery approach which relies on three basic steps: 1) Behavior capturing; 2) Dynamic behavior modeling; and 3) Requirements derivation as formal documents. All these approaches use only static information to extract business process models from information systems.

6 SUMMARY AND OUTLOOK

This paper proposed the IncrementalMiner, an incremental process mining algorithm for the extraction of business processes models from information system event log. The algorithm is an extension of the HeuristicMiner where the data structure used was restructured in order to support the incremental update of the model. In its performance evaluation, the total processing time of logs was reduced in 64% during the incremental mining and was five times faster than Alpha++ and eighty times faster than HeuristicMiner. The extracted process models showed good accuracy when compared with results of other process mining algorithms.

Altogether, the main contribution of this work is the incremental functionality of the algorithm to support incremental learning of business processes models by processing event trace logs that are recorded during successive system executions.

In the near future, we intend to do additional performance and quality tests with IncrementalMiner to consider other types of processes and datasets.

REFERENCES


