REUSABLE STATE MACHINE COMPONENTS FOR EMBEDDED CONTROL SYSTEMS

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Abstract: The paper presents a software design method for embedded applications, featuring reconfigurable components such as a State Machine (SM) function block operating in conjunction with a composite Signal Generator (SG) function block. The method emphasizes separation of concerns, whereby the State Machine realizes the reactive aspect of system behaviour in separation from the transformational aspect, which is delegated to the Signal Generator. Instances of these function blocks can be used to configure event-driven state machines executed periodically in the context of control system tasks (actors). When activated, the SM determines the control step that has to be executed in response to a particular event. The control step is then indicated to the SG, which generates the corresponding control signals. The SM has been implemented using a new Binary Decision Diagram (BDD)-based design pattern, resulting in a simple, yet powerful component capable of processing both discrete and continuous signals, which can be used to efficiently implement control actors for sequential and hybrid control applications.

1 INTRODUCTION

The conventional implementation of state machines is based on manual encoding of an abstract model representing either the behaviour or the structure of the state machine. In the former case, the behavioural model, i.e. the state transition graph, is converted into code using various kinds of design patterns, such as the switch-case design pattern (Samek, 2002). In the latter case, the software implementation models the hardware structure of the state machine. The resulting program computes the state transition logic functions and executes the actions that are associated with various states. In particular, that is how sequential control programs are developed for industrial automation systems, where control logic is encoded using domain-specific languages, such as those defined in standards IEC 61131-3 (John and Tiegelkamp, 2001) and IEC 61499 (Lewis, 2001).

In both cases, conventional design methods have a major shortcoming: the resulting implementation is not reusable, because the logic of the state machine is built into the code. Consequently, a new program has to be developed whenever an application is created or modified. This is a time-consuming and error-prone process whose complexity grows rapidly with the number of states and state transitions. To some extent, the situation can be alleviated via automated program generation using validated models, but code reusability is still a problem.

This problem can be solved by developing reusable state machine components, featuring standard state machine drivers operating on reconfigurable data structures (Wang and Shin, 2002), (Wagner and Wolstenholme, 2003). The resulting software artifact can be viewed as an object of type ‘state machine’, which may have multiple instances defined by the contents of the encapsulated data structures (configuration tables). These can be configured and re-configured using a dedicated configuration tool. In this way, conventional software development is replaced by the configuration of reusable components and consequently, manual coding of state machines can be largely reduced and even eliminated.

This design philosophy has been adopted and further refined in a reconfigurable state-machine component for embedded control systems (Angelov et al., 2005). With that component, it is possible to invoke signal-processing function blocks (FBs) within the states of the execution control state...
However, the complexity of the component model is relatively high because it combines both reactive (state-based) and transformational behaviour in the context of hybrid control systems. This has motivated the development of the master-slave model presented in (Angelov et al., 2008) where system tasks (actors) are configured using stateful components of lower complexity, i.e. a state-machine function block coupled to a modal function block. However, in this model the state machine can process only binary event signals that are generated by pre-processing function blocks such as comparators, counters, timers, etc., which may result in increased complexity of the corresponding function block networks.

The above problem has been addressed with a design method featuring a new State Machine function block operating in conjunction with a composite Signal Generator, which is presented in this paper. The discussion is illustrated with a running example – a state machine used to implement one of the control actors of a Medical Ventilator Control System (Zhou et al., 2009).

The rest of the paper is structured as follows: Section 2 presents the design model of a state machine composed of State Machine and Signal Generator components and focuses on the implementation of a reconfigurable function block of class State Machine, using a design pattern that integrates pre-processing and control functions. Section 3 presents briefly the design pattern of the Signal Generator function block. A summary of the proposed software design method and its implications is given in the concluding section of the paper.

2 RECONFIGURABLE STATE MACHINE FUNCTION BLOCK

Embedded control system actors may exhibit complex stateful behaviour. Such actors can be built from reconfigurable software components, i.e. State Machine (SM) and Signal Generator (SG) function blocks. This approach emphasizes separation of concerns: the SM implements reactive behaviour by selecting the control step to be executed in response to a transition event defined in terms of one or more event signals that are sampled when the host actor is triggered. The control step is specified in terms of one or more output signals. These are generated by invoking a sequence of function blocks inside the SG - a composite component, which implements the transformational aspect of actor behaviour - from input signals to output signals (see Fig. 1).

Figure 1: State Machine and Signal Generator function blocks.

The SM function block can be implemented using a new version of the State Logic Controller (SLC) design pattern originally introduced in (Angelov et al., 2005). The SLC employs a data structure that represents the state transition graph of a Moore machine realizing the desired control behaviour. It can be efficiently encoded as a table containing binary decision diagrams that represent the next-state mappings of various states in the set of states S, and the corresponding control steps, in accordance with the state transition graph.

The next-state mapping of a state s is defined as the subset $F_s = \{s'\}$ involving those states that are immediate successors of s. Hence, a state transition graph can be symbolically represented by specifying the next-state mappings of all states $s \in S$, whereby the transition arcs are defined as tuples $(s, s' | s' \in F_s)$ that are associated with the corresponding transition events and event-priority symbols.

This technique will be illustrated with a running example, i.e. a control state machine encapsulated in the Volume Control Ventilation (VCV) actor of a Medical Ventilator Machine (Zhou et al., 2009), see Fig. 2. Its state transition graph can be represented as follows:
\[ \begin{align*}
F_{s0} &= s_i / Y_i [c] \\
F_{s1} &= s_i / Y_i [c] \\
F_{s2} &= s_i / Y_i [c] \\
F_{s3} &= s_i / Y_i [e_i], s_i / NOP [e_i] \\
F_{s4} &= s_i / Y_i [c] \\
F_{s5} &= s_i / Y_i [e_i, 1], s_i / Y_i [e_i, 2], s_i / NOP [e_i, e_i],
\end{align*} \]

where \( s_0 \) denotes the initial pseudo-state, \( s_1 - s_5 \) denote operational states; \( Y_1 - Y_5 \) denote the corresponding control steps – initialization (init), close inspiration valve (\( close_{\text{IV}} \)), open expiration valve (\( open_{\text{EV}} \)), close expiration valve (\( close_{\text{EV}} \)), PID control of inspiration valve (\( PID_{\text{control}} \)), \( e_1 \) and \( e_2 \) denote events represented by signals \( inspFlag \) and \( expFlag \) respectively, and \( c \) denotes the default clock event; bracketed expressions denote the corresponding triggering events or \( <\text{event} - \text{event-priority}> \) pairs (when necessary).

Next-state mappings can be conveniently represented by means of binary decision diagrams, as shown in Fig. 3 for the example state machine. In these diagrams, circular nodes denote event signals that have to be tested in order to determine the current state/step to be executed from among the subset of successors of the previous state/step. These are tested in a predefined sequence that reflects the priority of the corresponding transitions.

![Figure 3: Binary decision diagrams for next state (step) mappings.](image)

For example, it is possible to make a transition from \( s_1 \) to either \( s_2 \) or \( s_4 \), whereby the former transition has higher importance, i.e. lower event priority than the other one. That is encoded in the BDD whereby the event signal \( e_2 \) is checked first and the transition to \( s_2 \) – taken if \( e_2 \) is true; the transition to \( s_4 \) will be taken only if \( e_2 \) is false and \( e_1 \) – true. In case neither of the event signals is present, the parsing of the BDD ends up in a no-operation (NOP) node, meaning that no transition is taken and the previous state has to be maintained in the current period without executing a control action.

<table>
<thead>
<tr>
<th>Node</th>
<th>SuccTrue</th>
<th>SuccFalse</th>
<th>Mapping</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>( Y_1 )</td>
<td>1</td>
<td>( x )</td>
</tr>
<tr>
<td>1</td>
<td>( Y_2 )</td>
<td>2</td>
<td>( x )</td>
</tr>
<tr>
<td>2</td>
<td>( Y_3 )</td>
<td>3</td>
<td>( x )</td>
</tr>
<tr>
<td>3</td>
<td>( e_1 )</td>
<td>4</td>
<td>5</td>
</tr>
<tr>
<td>4</td>
<td>( Y_4 )</td>
<td>6</td>
<td>( x )</td>
</tr>
<tr>
<td>5</td>
<td>NOP</td>
<td>3</td>
<td>( x )</td>
</tr>
<tr>
<td>6</td>
<td>( Y_5 )</td>
<td>7</td>
<td>( x )</td>
</tr>
<tr>
<td>7</td>
<td>( e_2 )</td>
<td>1</td>
<td>8</td>
</tr>
<tr>
<td>8</td>
<td>( e_1 )</td>
<td>6</td>
<td>9</td>
</tr>
<tr>
<td>9</td>
<td>NOP</td>
<td>7</td>
<td>( x )</td>
</tr>
</tbody>
</table>

The binary decision diagrams of the next-state mappings can be encoded in a Step Sequence Table (also called the BDD Table) as shown in Table 1. It consists of the columns \( \text{Node} \), \( \text{successorTrue} \) / \( \text{successorFalse} \), and \( \text{Mapping} \), whereby the first column contains symbols denoting BDD nodes, and the other two columns – pointers to rows containing the corresponding BDD elements. The rows are grouped into segments containing the next-state mappings of states \( s_0 - s_5 \).

The Step Sequence Table can be interpreted much in the same way as its graphical counterpart. This can be done by a standard routine – a State Machine Driver (SMD), which is activated periodically by the host actor. Within each cycle, the SMD processes the BDD segment containing the successor states/steps of the state visited in the previous cycle, in order to determine the current state/step. If a state transition has taken place, the control step index variable is updated accordingly, and the associated Signal Generator function block is subsequently invoked to execute the corresponding control step. However, it is executed only when the state is visited for the first time; it will not be executed in subsequent cycles if the state is maintained, unless a self-transition is explicitly specified (execute-once semantics).

The above discussion is based on the assumption that event signals are Boolean variables supplied by external components, e.g. pre-processing function...
blocks such as digital and analogue signal comparators, timers, event counters, etc. However, this may result in relatively complex function block networks modelling application actors. That problem can be eliminated by executing pre-processing operations as internal functions of the state machine function block. In that case, the condition nodes of the BDD may be interpreted as various types of compare, event counting and timer operations whose result is tested in order to make a branching decision within the BDD.

Each node of the BDD is thus associated with an operation that has to be executed by the State Machine Driver when processing the node. To that end, an operation code is used to specify the node operation, e.g. a control step executed in a state node. Likewise, it is necessary to specify operation codes (or function pointers) for various Boolean test, compare, and counter/timer operations executed in condition-testing nodes of the BDD.

The BDD table of the state machine function block can be encoded using records of the following format:

```
BDD_Record = Operation, CondTest | Operation, ControlStep;
Operation = CondOp1 | ... | CondOpk | CtrlStepOp;
CondTest = Operand1, Operand2, SuccessorTrue, SuccessorFalse;
ControlStep = ControlStepIndex, NextStateMapping;
```

where the Operation code specifies one of the following node-processing operations:
- Boolean operations
- Compare Integer operations
- Compare Real operations
- Count Events operation
- Control Step operation

In case of condition evaluation, the CondTest part of the BDD record contains operand fields, which are interpreted in the context of the executed node-processing operation as follows:
- Boolean operations use Operand1 and Operand2 as pointers to the tested variable locations.
- Compare Integer and Compare Real operations use Operand1 as a pointer to the first compared variable and Operand2 as a pointer to the second compared variable or constant.

The Count Events operation uses Operand1 as a pointer to the counted event variable. The initial value of the event counter and the event counter itself are passed as parameters via the Operand2 field.

The remaining two items of the condition-test record are used to implement branching decisions, as follows:
- Successor1 is used as a pointer to the next line to be processed if the test/compare/counter operation returns True.
- Successor0 is a pointer to the next line to be processed if the test/compare/counter operation returns False.

In case of control step execution, the Operation field is accompanied by a ControlStep field comprising:
- ControlStepIndex – an index of the control step that has to be executed in the current state. A NOP encoding of the control step index denotes no operation.
- NextStateMapping – a pointer to the first line of the corresponding next-state mapping.

The above operations are executed by the State Machine Driver while processing binary decision diagrams, as follows:
- Boolean operations and compare operations are implemented by means of C-library compare routines, which return True or False depending on the result.
- The Count Events operation interprets Operand1 as a pointer to the input variable of the event counter. If that is a NULL pointer, the event counter is driven by the periodic timing events triggering the host actor, and operates as a timer measuring time intervals that are multiples of the actor period. The initial value of the event counter and the counter itself are passed as a pointer to a dedicated data structure in the second operand field. The operation returns False if \[\text{counter}\] \neq 0 after decrementing the counter; if \[\text{counter} = 0\], the operation re-initializes the counter and returns True.

The control step index is supplied to the SG as an input parameter used to invoke the corresponding sequence of function blocks in order to generate the required control signals. If the SM state in the current cycle is the same as in the previous one (NOP BDD node), a NOP control step index is generated, in accordance with the adopted execute-
once semantics. However, a self loop may be used if a control step has to be executed repeatedly in successive periods (e.g. \textit{PID} in state \textit{s5} of Fig. 2).

The algorithm given below can be used to implement a state machine driver for a reusable and reconfigurable function block of class \textit{StateMachine}:

```c
void StateMachineDriver(void *FB) {
    // Restore execution history
    BDD_Record *r = FB->tableRecord;

    // Determine current step and update output
    do {
        // Condition-testing node?
        if (r->operation != CTRL_STEP_OP) {
            if ((r->operation)(r->operand1, r->operand2)) { // True
                r = r->successorTrue;
            } else { // False
                r = r->successorFalse;
            }
        } else {
            // Control step node?
            // Update control step index
            FB->ctrlStepIndex = r->ctrlStepIndex;

            // Save execution history
            if (r->ctrlStepIndex != NOP )
                FB->tableRecord = r->nextStateMapping;

            return; // Leave the driver
        }
    } while( TRUE );
}
```

The \textit{SM} function block instance is invoked with a pointer to an execution record of type \textit{StateMachine} denoted as \textit{FB}, which contains relevant data, such as output buffer for the control step index variable as well as a \textit{tableRecord} history variable, i.e. a pointer to the first line of the next-state mapping segment, to be processed during the next activation of the \textit{SM} function block.

### 3 SIGNAL GENERATOR FUNCTION BLOCK

The Signal Generator is a composite function block containing instances of function blocks that are to be invoked within statically defined execution schedules - control step (CS) sequences, in order to generate the control signals associated with the corresponding control steps.

To that end, the control step index generated by the \textit{SM} is used to access a table containing records such as \textit{<CSSequenceStart, CSSequenceLength>}, where each line corresponds to one particular control step. These two parameters are used to access a \textit{Function Block Table (FBT)} where each line corresponds to a function block instance specified by the record \textit{<FBFunction, FBinstance>}.

In particular, the \textit{CSSequenceStart} is used to access a \textit{FBT} record specifying the first function block instance of a control step sequence, and \textit{CSSequenceLength} - the number of function block instances that have to be invoked in order to execute the control step. Hence, the \textit{FBT} can be viewed as a concatenation of control step sequences that are specified by the corresponding sub-networks of the function block network encapsulated in the Signal Generator.

It is possible that several control steps generate one and the same continuous control signal, e.g. a control signal that is generated in both manual and automatic mode of operation. In that case, a Multiplexor \textit{FB} shall be used, whereby different Multiplexor functions are invoked to switch the corresponding input signals to the multiplexor output.

Discrete (on/off) control signals can be generated by means of another kind of function block that may be invoked within the Signal Generator – the \textit{Discrete Control Function Block (DCFB)}). The \textit{DCFB} employs the concept of \textit{control memory} storing binary control words: a particular word is accessed using the corresponding control step index, and is subsequently stored in the \textit{DCFB} output buffer.

Discrete control signals can also be generated by means of a digital multiplexor function block. In this case, the control step index is used to select an input binary word to be switched to the multiplexor output in order to generate the corresponding on/off control signals. This solution is preferable for applications featuring a small number of discrete control steps, as is the case with the example state machine of Fig. 1.
The Signal Generator of the example state machine is shown in Fig. 4. It incorporates two function block instances, i.e. a Multiplexor FB instance generating on/off control signals for the control steps open_EV and close_EV, and a PID FB instance generating the signal pid_control and close_IV. The PID function block encapsulates three functions: initialize(), PID() and stop(). The first one is invoked when executing the init control step and the other two – when executing the control steps pid_control and close_IV (by applying a zero voltage to the inspiration valve of the ventilator).

The combination of state machine and signal generator can be used to engineer sequential and modal continuous control systems, as well as systems generating continuous control signals in some states and discrete on/off control signals in other states, as shown in the example.

4 CONCLUSIONS

The paper presents a software design method for embedded control applications, which employs two types of reconfigurable component that can be used to configure control system tasks (actors) – State Machine and Signal Generator function blocks. The State Machine function block realizes the reactive (control flow) aspect of actor behaviour, in separation from the transformational (data flow) aspect, which is assigned to the Signal Generator.

The presented version of the State Machine function block is capable of processing any kind of input signal – Boolean, binary-coded or analogue in order to compute Boolean event variables needed to implicitly select the state to be activated, and to explicitly select the control step to be executed in that state. The index of the control step is then indicated to the Signal Generator, in order to activate the corresponding FB sequence used to generate the corresponding control signals.

The State Machine has been implemented as a reusable and reconfigurable function block using a new BDD-based State Logic Controller design pattern, resulting in a simple, yet powerful component that can be combined with a reconfigurable Signal Generator to efficiently implement state machines of arbitrary complexity for a broad range of sequential and hybrid control applications.

REFERENCES