BIDIRECTIONAL HIERARCHICAL NEURAL NETWORKS
Hebbian Learning Improves Generalization

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Abstract: Visual pattern recognition is a complex problem, and it has proven difficult to achieve satisfactorily in standard three-layer feed-forward artificial neural networks. For this reason, an increasing number of researchers are using networks whose architecture resembles the human visual system. These biologically-based networks are bidirectionally connected, use receptive fields, and have a hierarchical structure, with the input layer being the largest layer, and consecutive layers getting increasingly smaller. These networks are large and complex, and therefore run a risk of getting overfitted during learning, especially if small training sets are used, and if the input patterns are noisy. Many data sets, such as, for example, handwritten characters, are intrinsically noisy. The problem of overfitting is aggravated by the tendency of error-driven learning in large networks to treat all variations in the noisy input as significant. However, there is one way to balance this tendency to overfit, and that is to use a mixture of learning algorithms. In this study, we ran systematic tests on handwritten character recognition, where we compared generalization performance using a mixture of Hebbian learning and error-driven learning with generalization performance using pure error-driven learning. Our results indicate that injecting even a small amount of Hebbian learning, 0.01%, significantly improves the generalization performance of the network.

1 INTRODUCTION

Generalization is one of the most desired attributes of any object recognition system. It is unreasonable and impractical to present all existing instances of an object to a recognition system for learning. A well-designed system must be robust enough to learn the appearance of an object from a few available instances and to generalize the learnt response to novel instances of the same object.

Humans are generally flexible and quite good at generalization. For example, we can easily recognize any legible English letter, no matter who wrote it. In tasks such as this, we use our past knowledge of the shape of a letter for recognizing it. This capability of the human visual system attracts researchers to find out the underlying mechanism of the primate visual cortex and to emulate these mechanisms when developing artificial object recognition systems.

The human visual system is hierarchically organized, and has many layers. Consecutive layers are connected in both feed forward and feedback directions (Callaway, 2004). The interactive property of these biological networks is nicely captured by bidirectional hierarchical artificial neural networks, which are considered to be biological plausible, and are often used for modelling human vision.

Backpropagation of error is a powerful error-driven learning algorithm. Biologically-based forms of backpropagation of error are therefore a good candidate for learning algorithm that can be used in human-like bidirectional hierarchical networks. Error-driven learning is widely used in artificial neural networks for image processing and object recognition tasks. However, error driven learning in these networks is often used to drive weight changes on the level of individual pixels in the input image. This technique, on the one hand helps to learn a task very well; on the other hand, it creates a risk for overfitting. This risk increases as the network size in terms of number hidden layers and number of units in each layer increases.

There are different ways to overcome the risk of overfitting. One way is to increase the training input to the network. But this option is not always a feasible option due to obvious reason of limited
resources and time for training.

Second, one could keep down the degrees of freedom in the network, either through careful choice of hidden layer size and number of weights, or by introducing a bias on weight development during training for example, using weight decay to kill off weak weights that tend to encode noise in the input, or by actually pruning the network structure, cutting off small weights.

Third, one can use a network structure that facilitates feature extraction that is, encoding of local features in the input (Fukushima, 1993). Encoding of local features is necessary if the network is to recognize novel input where individual features are combined in a new way.

In this study we will mix amount of Hebbian learning with the error driven learning to see how it affect the generalization performance of the network.

2 HIERARCHICAL NETWORKS

Hierarchical networks for image processing are inspired by the human visual system and have been demonstrated to be especially well suited for extracting local features from an image (Fukushima, 2008). In hierarchical networks, the hidden layers are selectively connected to the previous layer, so that groups of units in layer $k$ send signals to a smaller number of groups in layer $k+1$. This connectivity pattern will yield a hierarchical communication structure, where contiguous patches of the input image are processed by an array of receiving groups in the first hidden layer. These groups in turn project to a smaller number of groups in the subsequent layer, and so on, until a single group of units covers the complete input (see figure 1 for an illustration). The advantage of such a connectivity pattern is that it forces the network to look at local features in the input image.

A bidirectional hierarchical network is a hierarchical network with bidirectional connection between adjacent layers. Bidirectional networks are quite powerful, but may also be difficult to understand due to the relatively complex attractor dynamics that can arise as a result of the bidirectional connectivity.

2.1 Hebbian Learning

In its original form, Hebbian learning rewards the co-activation of pairs of receiving and sending units, increasing the weights of co-activated units (Hebb, 1949). In addition to this, modified Hebbian learning rules can also decrease the weights of nodes that are inconsistently activated, one node being activated and the other not (O'Reilly, 2000). These modified Hebbian learning rules turn out to capture the statistical regularities in the input space, and will develop a weight structure that promotes the detection of local features in the input (McClelland, 2005).

The question is: What role does Hebbian learning play for the generalization capability of these networks?

Previous research suggests that Hebbian lear-
ning is important for generalization in bidirectionally connected networks (O’Reilly, 2001). The role of Hebbian learning has, however, not been investigated in bidirectional hierarchical networks. Bidirectional hierarchical networks are used in human vision and account for many important biological vision phenomena like attention, pattern completion, and memory (Wallis, 1997). It is therefore motivated to investigate these networks’ learning and generalization performance.

2.2 Our Network Architecture

A bidirectional hierarchical network was developed in Emergent (Aisa, 2008). It consists of five layers, namely Input V1, V2, V4 and Dir (Figure 1). An additional layer correct_dir was introduced. This layer does not take part in actual processing of the data, but allow us to visually compare the network’s output with desired output. Input layer consists of 66X66 units. This layer is divided into nine rectangular receptive fields each of size 26 X 26 with an overlap of 6 units on each side. Second layer V1, containing 24 X 24 units, is divided into 9 equal rectangular parts. Where as each part consists of 8 X 8 units. Each part receives input from a corresponding receptive field from input layer. Third layer V2 is of size 16 X 16. This layer is divided into 4 equal parts. Each part receives input from a group of 16 X 16 units from the previous layers. Fourth layer V3 is of size 12 X 12. It is fully connected with the previous V2 layer. The last layer, Output layer, contains eight units. Each represents one of the eight English alphabets for recognition.

Figure 2: Data sets used for testing and training.

3 TESTING PROCEDURE

The network’s task was to recognize eight different categories of handwritten English capital letters. The choice of the letters was made on the basis of their structure. We wanted to use letters that shared some features, in order to make the categorization task more difficult. The problem that could arise in a badly trained network is that the constituent features or one letter were recombined and gave rise to false recognition of another letter. For example, letters ‘E’ and ‘H’ share the vertical line ‘I’ and horizontal line ‘-‘as feature. We got five different hand written letter sets from five different persons, where as each set consist of eight letters. The original images were resized and shifted in four steps in eight directions, producing about 3600 images. Out of the six set of images, we kept aside one set of images (600 images) for testing with trained network as novel images. From the remaining five sets, we used 75 % of images as training the network and 25 % for testing the trained network. In this way we wanted to evaluate the performance of the network on trained as well as entirely novel set of images.

We ran systematic tests of pairs of identical networks, the only difference being the amount of Hebbian learning in the learning mix for various connections. For some network pairs, we used the same learning mix for all connections. In the particular test described here, we let the first level of connections, going from the input layer to the first hidden layer, V1, use 1% Hebbian learning, and let subsequent connections use 0.1% Hebbian learning. In contrast, for the no_Hebb version of the network, we removed Hebbian learning from the learning mix for all connections.

Table 1: Results from the generalization tests using both a 5% testing set reserved, i.e., excluded from the training set (same handwriting), and a novel set of handwritten letters.

<table>
<thead>
<tr>
<th>Batch No</th>
<th>With 5% testing set (Count error in %)</th>
<th>New set of 600 letters (Count error in %)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>No Hebbian</td>
<td>Hebbian</td>
</tr>
<tr>
<td>1</td>
<td>3.16</td>
<td>1.33</td>
</tr>
<tr>
<td>2</td>
<td>1.16</td>
<td>0.66</td>
</tr>
<tr>
<td>3</td>
<td>1.66</td>
<td>0.66</td>
</tr>
<tr>
<td>4</td>
<td>1.66</td>
<td>0.66</td>
</tr>
<tr>
<td>5</td>
<td>1</td>
<td>0.76</td>
</tr>
</tbody>
</table>

Emergent offers a sigmoid-like activation function, and saturating weights limited to the interval [0, 1]. Learning in the network was based on combination of Conditional Principal Component Analysis, which is a Hebbian learning algorithm and Contrastive Hebbian learning (CHL), which is a biologically-based error-driven algorithm, an alternative to backpropagation of error (O’Reilly,2000):
CPCA: 
\[ \Delta_{\text{hebb}} = \varepsilon y_j (x_i - w_{ij}) \]  
\( x_i \) = activation of sending unit \( i \)  
\( y_j \) = activation of receiving unit \( j \)  
\( w_{ij} \) = weight from unit \( i \) to unit \( j \)  

CHL: 
\[ \Delta w_{ij} = \varepsilon (x_i^+ y_j^- - x_i^- y_j^+) = \Delta_{\text{err}}. \]  
\( x_i \) = activation of sending unit \( i \)  
\( y_j \) = activation of receiving unit \( j \)  
\( x_i^+ \), \( y_j^- \) = act when only output clamped  
\( x_i^- \), \( y_j^+ \) = act when only input is clamped  

Learning mix: 
\[ \Delta w_{ij} = \varepsilon [c_{\text{hebb}} \Delta_{\text{hebb}} + (1 - c_{\text{hebb}}) \Delta_{\text{err}}] \]  
\( \varepsilon \) = learning rate  
\( c_{\text{hebb}} \) = proportion of Hebbian learning  

For the Hebb case we used \( c_{\text{hebb}} = 0.01 \) for connections from input to V1 and \( c_{\text{hebb}} = 0.001 \) for all subsequent connections. For the No-Hebb case we used \( c_{\text{hebb}} = 0 \) for all connections. The low amount of Hebbian learning is motivated by previous experience and the fact that Hebbian learning exerts a powerful influence on learning (O’Reilly, 2000).  

4 TEST RESULTS  

We tested the network’s generalization capability in two ways: First, by using the 5% testing set and second by using translations (size, orientation, and position variations) of one remaining set of alphabet set. We recorded the number of errors and calculated the percent errors that were made (table 1). It is clear from the table 1 that Generalization performance of the network improved for both 5% testing set as well as novel set of images when we used both error driven and Hebbian learning.  

In addition to the above tests we analyzed the weight structure developed during training using an indirect method called activation-based receptive field analysis. This analysis is based on the co-activation of input-units and a particular receiving unit. The average co-activation taken over all input images reflects a tendency of this particular receiving unit to react to particular forms of input.  

The plots in figure 3 represent the sixty-four units of the lower left group in V1 organized in the same order as they appear within the layer. The plot on the top of figure 3 shows receptive fields from the input layer into the sixty-four units in V1. Note that all these sixty-four units have the same receptive field that is, they take input from the same image-patch (marked with white squares). The patterns in the large boxes are the weighted averages of input patterns over the activation of respective V1 unit. Thus, input patterns that the receiving unit became strongly activated for are represented with a larger weight in the weighted average. The part of the pattern in the big box which is delineated with the small white box is the actual pattern which appears in the receptive field of the given unit. The plot on the bottom of figure 3 shows the projection fields from the same units in V1 into the output layer. Each unit-size rectangle in the projective fields represents the average co-activation of a given V1 unit and the corresponding output unit, calculated for the full set of input patterns. Thus, the projective field show how strongly a given V1 unit signals indirectly to each output category. As can be seen, most units have developed useful feature representations, and project to a small number of directional units in the output layer.  

4.1 Hebbian Learning Mix  

Looking at the receptive field analysis for these networks (figure 3) it can be seen that most of the averaged patterns in the large boxes originate from a specific character, or a few similar characters. This indicates that the detector units are sensitive to useful features that are part of similarly shaped letters. This conclusion can be further verified by looking at the projective field of the same units. For example, the unit in the second row from the bottom and fourth column from has learnt to specialize for feature that is part of the letter ‘Q’. If we look at the corresponding projective field pattern in the second row and fourth column, the rectangle shows only a single active unit (marked with intensive yellow). This means that this particular unit in V1 is indirectly contributing to the recognition of only one category of letters, namely the letter ‘Q’. There are some units which are sensitive to a feature which is part of more than one class of letters, but in a graded fashion. For example the weighted average pattern at the eighth row and first column is a mix of ‘Q’ and ‘O’. If we look at the corresponding projection field, there are two output units that receive activation from this unit, but in a graded way. Hence, the feature that is extracted by this unit is available in both letters. The final decision about which output category should be activated is made.
Figure 3: Activation-based receptive field and projective field analysis for layer V1, when Hebbian learning was included in the learning mix. (top) Each big box in the plot represents the input layer and the small white box within each big box signifies the actual receptive field for the units of a given V1 group. (bottom) Each rectangle in the plot represents the output layer with eight units. Gray color is default background color. Pattern colors from red to yellow (dark to light) signify the increasing activation/intensity value. Light (yellow) color represents high pixel and dark (red color) low pixel values.
Finally, we note that there are some units which have not developed any useful features. For example, the unit in the second row and first column is not selective for any particular class of letters. The corresponding projective field of the unit shows that the V1 unit in question projects to several output
units, and thus is likely not to play a useful role in the task.

4.2 Pure Error-driven Learning

Figure 4 presents the activation-based receptive field and projective field analysis for the lower left unit group in layer V1 when pure error-driven learning was used for training (no Hebbian injected). Compared to the previous figure, there are many units here that have not developed any useful feature representation, and project equally strongly to a large number of output units. In addition, quite a few units are never activated during processing. This is probably why generalization performance suffered when Hebbian learning was excluded from the learning mix (Equation 3; Figures 4).

5 CONCLUSIONS

In this article, we have studied the effect of mixing error driven and Hebbian learning in bidirectional hierarchical networks for object recognition. Error driven learning alone is a powerful learning mechanism which could solve the task at hand by learning to relate individual pixels in the input patterns to desired perceptual categories. However, handwritten letters are intrinsically noisy as they contain small variations due to different handwritings, and this increases the risk for overfitting—especially so in large networks. Hence, there is a risk that error-driven learning might not give optimal generalization performance for these networks.

We run systematic training and generalization tests on a handwritten letter recognition task using pure error-driven learning as compared to using a mixture of error-driven and Hebbian learning. The simulations indicate that mixing Hebbian and error-driven learning can be quite successful in terms of improving the generalization performance of bidirectional hierarchical networks in cases when there is much noise in the input, and an increased risk for overfitting.

Additionally, we also believe that Hebbian learning can be a good candidate for generic, local feature extraction for image processing and pattern recognition tasks. In contrast to pre-wired feature detectors, for example, Gabor-filters, Hebbian leaning provides a more flexible means for detecting the underlying statistical structure of the input patterns as it has no a priori constraints on the size or shape of these local features.

REFERENCES