Keywords: AFIS, SVM, Classification rate.

Abstract: In this work a hybrid technique for classification of fingerprint identification has been developed to decrease the matching time. For classification a Support Vector Machine is described and used. Automatic Fingerprint Identification Systems are widely used today, and it is therefore necessary to find a classification system that is less time-consuming. The given fingerprint database is decomposed into four different subclasses and a SVM algorithm is used to train the system to do correct classification. The classification rate has been estimated to about 87.0% of unseen fingerprints. The average matching time is decreased with a factor of about 3.5 compared to brute force search applied.

1 INTRODUCTION

Fingerprints have been used for identification for hundreds of years. The first years, the matching of fingerprints was done by human experts. 40 years ago, researchers started to load digital fingerprint data onto computers. The first Automatic Fingerprint Identification System (AFIS) was developed in 1991, and since then, there has been an enormous progress in the field. Due to the ever-growing capabilities of computers and great achievements in research, the recognition rate has improved significantly. There is nevertheless a huge amount of work to be done.

The current work in this field concentrates on reducing the computation time for feature extraction and matching. Embedded fingerprint systems supporting instant identification or verification are increasingly used, and the computation time for these processes is thus an important research field. One way to decrease this time is to divide the fingerprint database into different subclasses based on specific properties, such that only a part of the fingerprints needs to be considered for matching.

The uniqueness of fingerprints has been widely tested, and two identical fingerprints have still not been found (Pankanti et al., 2002). However, current fingerprint identification systems do not use all the discriminating information present in a fingerprint, and the probability of finding two identical fingerprints using the systems therefore increases. A lot of work is being done today to decide which information in fingerprints should be used to keep the uniqueness. In addition to this work, the current work in this field concentrates on reducing the computation time for feature extraction and matching.

Various methods have been used for classification, and some of the most successful ones use artificial neural networks as a classifier. In this paper, however, a Support Vector Machine has been used for classification. The SVM network is given a feature vector as input, based on computation of the Poincare index. This method was first proposed by Jain, Prabhakar and Hong (Jain et al., 1999).

Among all the biometric techniques fingerprint identification is today the most widely used biometric identification form. It has been used in numerous applications. Everyone is supposed to have a unique, immutable fingerprint. It is also the one that is scoring highest overall compared to other forms as iris, signature, voice, etc. In 2002 fingerprint based biometric systems had a market of 52.1% (Maltoni et al., 2005).

The problem is to develop algorithms which are robust to noise in the fingerprints and are able to deliver accuracy in real time.

Fingerprint matching algorithms vary greatly in terms of false positive and false negative errors. They may also vary with respect to features such as
image rotation invariance and independence from a reference point, given as the centre or the core of the fingerprint pattern.

2 BACKGROUND

In an automatic fingerprint identification system (AFIS), the fingerprint database can be huge, often tens of thousands of fingerprints. If you were supposed to check for similarity between the query fingerprint and every other fingerprint in the database, it would take an enormous amount of time.

With this in mind, fingerprint classification is an important step that has to be implemented in every fingerprint identification system. The classification criteria most widely used are the modification or extension of the standard Galton-Henry classification system (Henry, 1990). Here, fingerprints are divided into 5 subclasses: whorl (W), right loop (RL), left loop (LL), arch (A) and tented arch (TA).

2.1 Singularities

Three singularities can be found in the fingerprint to more easily distinguish between the classes. These three singularities are the loop, the delta and the whorl. A whorl fingerprint contains one or more ridges that make a complete 360-degree path around the centre of the fingerprint. Two loops (or one whorl) and two deltas are present. The deltas are placed under the whorl, one at the right and one at the left side. A loop fingerprint has one or more ridges that enter from one side, curves back and exits at the same side as they entered. In a left and right loop, the ridges enter from the left side and the right side, respectively. A loop and a delta singularity are present, with the delta under the loop, at the left in a right loop fingerprint and at the right in a left loop fingerprint. An arch fingerprint has ridges that enter from one side, rises to a small bump and exits at the opposite side.

When no singularities are present, this will make the classification of the class rather difficult. A tented arch fingerprint contains one or more ridges that enter from one side, loops in a high curvature and exit at the opposite site. When one loop and one delta singularity are present, the delta is typically placed right under the loop as shown in figure 2.

2.2 Different Methods

Many fingerprint classification methods have been proposed in literature. In general, these methods can be categorised into five approaches (Maltoni, et al., 2005):

- rule-based
- syntactic-based
- structure-based
- statistical-based
- neural-network based

In this work we have concentrated on the statistical-based approach and want to see how the performance of an AFIS comes out, based on SVM as a classifier.
The current work in this field concentrates on reducing the computation time for feature extraction and matching. Embedded fingerprint systems supporting instant identification or verification are increasingly used, and the computation time for these processes is thus an important research field. One way to decrease this time is to divide the fingerprint database into different subclasses based on specific properties, such that only a part of the fingerprints needs to be considered for matching.

3 EXTRACTING FEATURES

3.1 Extracting Classification Features

The SVM network needs an input vector to be able to classify the fingerprints. This vector can be made by extracting features of the fingerprint, and then represent these features in a suitable way. We have chosen to create this vector based on a technique proposed by (Maltoni et al., 2005). Here, the authors present a feature vector called FingerCode, which is a vector consisting of 640 feature values.

First, a reference point in the fingerprint is to be found. We set the core of the fingerprint as the reference point. Then, the image is filtered in eight different directions using different Gabor filters, each enhancing ridges oriented in different angles. Each of these eight images are divided into 80 sectors according to specific rules. The standard deviation of each sector is finally calculated, and these values represent the feature values. The total number of feature values is 640 (8 x 80), and a vector containing these values is used as input vector to the SVM network.

3.2 Reference Point Detection

We have chosen to use the core point as the reference point. This core point is defined as the most northern loop singularity in a fingerprint. A loop singularity can be detected by a method based on the Poincare index proposed in (Jain et al., 1999).

Let $G$ be a vector field and $C$ be a curve immersed in $G$. Then, the Poincare index is defined as the total rotation of the vectors of $G$ along $C$. Here, $G$ is the vector field associated with an orientation image of the fingerprint. The curve $C$ is a closed path defined as an ordered sequence of the neighbour elements $d_k$ of position $(i,j)$ in the orientation image. Then, the Poincare index at position $(i,j)$ is defined as the sum of the orientation differences between adjacent elements of $C$:

$$P_{G,C} = \sum_{k=1}^{8} \angle(d_{k}, d_{(k+1) \mod 8})$$ (1)

where $d_k$ is the neighbouring elements as shown in Figure 3. This figure shows a typical loop singularity, and the sum of angles will here be 180 degrees. Because the left neighbour of $d_7$ is $d_0$, $d_{(k+1) \mod 8}$ is used instead of $d_{k+1}$.

![Figure 3: Computation of the Poincare index in the eight-neighbourhood of pixel $(i, j)$.](image)

It is shown that the sum of Poincare indexes must be either -360, -180, 0, 180 or 360. These indexes thereby give a clear indication of which singular region (SR) a pixel $(i,j)$ belongs to, see (Kawagoe, Tojo, 1984):

$$P_{G,C} = \begin{cases} 
0 \text{ deg. if } (i,j) \text{ does not belong to any SR} \\
360 \text{ deg. if } (i,j) \text{ belongs to a whorl type SR} \\
180 \text{ deg. if } (i,j) \text{ belongs to a loop type SR} \\
-180 \text{ deg. if } (i,j) \text{ belongs to a delta type SR} 
\end{cases}$$ (2)

As mentioned, the core point is the northern most loop. We assume that the fingerprints are captured with the finger in an approximately normal position, but tolerate a rotation of up to 45 degrees either clockwise or counter clockwise. The core point is used as reference point in the extraction of classification features.

3.3 Gabor Filtering

After the reference point is detected, the image is filtered using eight different Gabor filters. The image needs to be divided into 80 sectors, as illustrated in Figure 4. Here, the reference point is marked with a cross. Note that the innermost band is not divided into sectors, as it contains very few
pixels, and the standard deviation will then become very unreliable. Before filtering, each of the 80 sectors has to be normalized, setting the mean and variance to desired values.

Figure 4: Computation of the Poincare index in the eight-neighbourhood of pixel (i, j).

Each sector is normalized locally, so the mean and variance have to be calculated for each sector. The desired mean and variance value for each sector are both set to 100, as recommended by the authors in (Delima, Yen, 2003).

Let \( I(i, j) \) denote the gray level at pixel \((i, j)\) in a fingerprint image of size \(m \times n\) and let \((i_c, j_c)\) denote the reference point or core point. The region of interest is defined by a collection of sectors \(S_p\), where the sector \(S_p\) is computed in terms of parameters \((r, \theta)\) defined by (Burges, 1998):

\[
S_p = \{i, j | b(T_p + 1) \leq r \leq b(T_p + 2)\} \\
1 \leq i \leq n, 1 \leq j \leq m, \\
\theta_p \leq \theta < \theta_p + 1 \tag{3}
\]

where
\[
T_p = p \text{ div } k, \tag{4}
\]
\[
\theta_p = (p \text{ mod } k)(2\pi/k) \tag{5}
\]
\[
r = \sqrt{(i - i_c)^2 + (j - j_c)^2} \tag{6}
\]
\[
\theta = \tan^{-1}((j - j_c)/(i - i_c)) \tag{7}
\]

\(b\) is the width of each band and \(k\) is the number of sectors considered in each band. The Gabor filters use eight fixed angle values; \(\theta \in \{0 \text{ degrees}, 22.5 \text{ degrees}, 45 \text{ degrees}, \ldots, 157.5 \text{ degrees}\}\). The frequency is fixed, to limit computation, and set as the average ridge frequency in the region of interest. The region of interest is here the union of all the sectors defined above. The Gabor filtering results in eight images that each enhance the ridges in a specific direction and also remove noise, thereby emphasising the relevant information.

### 3.4 The Feature Vector

The feature vector is, as earlier mentioned, a vector consisting of 80 values for each of the eight Gabor filtered images. In each of these images, a section of the fingerprint containing ridges that are parallel to the corresponding filter direction, exhibits a higher variation. A section containing ridges that are not parallel to the corresponding filter tends to be smoothed by the filter, which results in a lower variation. The spatial distribution of the variations in the different sectors of the component images can thereby be a good characterisation of the global ridge structure. With this in mind, the feature vector is defined as a vector containing the standard deviation of all 80 sectors in the filtered image for all angles \(\theta\) [8].

Let \(F_p(i, j)\) be the \(\theta\)-direction filtered image for section \(S_p\). For \(p \in \{0, 1, \ldots, 79\}\) and \(\theta \in \{0 \text{ degrees}, 22.5 \text{ degrees}, \ldots, 157.5 \text{ degrees}\}\), the feature value is the standard deviation \(V_{p\theta}\), defined as:

\[
V_{p\theta} = \frac{1}{K_p} \sum_{x_p} (F_p(i, j) - P_{p\theta}) \tag{8}
\]

where \(K_p\) is the number of pixels in \(S_p\) and \(P_{p\theta}\) is the mean value of pixels in \(S_p\) in image \(F_p(i, j)\). Now, we have a 640-dimensional feature vector that can be used as input vector to the SVM network.

### 3.5 Scaling

To improve the classification rate, all feature vectors are scaled before training. The main advantage of scaling is to avoid attributes with big values which dominate those with small values.

Another advantage is to avoid numerical difficulties during the calculation. Because the kernel values in a Support Vector Machines depend on the inner products of the feature vectors, large attribute values may cause numerical problems. Scaling also makes the training run faster, and decreases the chance of getting stuck in local optima. The feature vectors are linearly scaled to the range \([-1, +1]\). Each value \(j\) in a feature vector \(i\) is scaled individually:
\[ S_{ij} = -1 + 2 \frac{FV(i, j) - \min_i}{\max_j - \min_j} \]  \hspace{1cm} (9)

where \( FV(i, j) \) and \( S_{ij} \) are the feature value and scaled feature value at position \( j \) for feature vector \( i \), respectively. \( \min_j \) and \( \max_j \) are the minimum and maximum feature value at position \( j \) for all feature vectors, respectively. The table must appear inside the designated margins or it may span the two columns.

4 SUPPORT VECTOR MACHINES

Support Vector Machines is a computationally efficient learning technique that is now being widely used in pattern recognition and classification problems (Burges, 1998). This approach has been derived from some of the ideas of the statistical learning theory regarding controlling the generalization abilities of a learning machine (Vapnik, 1998, Vapnik, 1999).

In this approach the machine learns an optimum hyper plane that classifies the given pattern. By use of kernel functions, the input feature space by applications of a non-linear function can be transformed into a higher dimensional space where the optimum hyper plane can be learnt. This gives a flexibility of using one of many learning models by changing the kernel functions.

4.1 The SVM Classifier

The basic idea of an SVM classifier is illustrated in Figure 5. This figure shows the simplest case in which the data vectors (marked by 'X' s and 'O' s) can be separated by a hyper plane. In such a case there may exist many separating hyper planes. Among them, the SVM classifier seeks the separating hyper plane that produces the largest separation margin.

In the more general case in which the data points are not linearly separable in the input space, a non-linear transformation is used to map the data vectors into a high-dimensional space (called feature space) prior to applying the linear maximum margin classifier. To avoid the potential pitfall of over-fitting in this higher dimensional space, an SVM uses a kernel function in which the non-linear mapping is implicitly embedded. A function qualifies as a kernel function if it satisfies the Mercer's condition (Vapnik, 1998).

With the use of a kernel function, the discriminant function in an SVM classifier has the following form

\[ f(x) = \sum_{i=1}^{N} \alpha_i y_i K(x_i, x) + \alpha_0 \]  \hspace{1cm} (10)

where \( K(\cdot, \cdot) \) is the kernel function, \( x_i \) are the support vectors determined from the training data, \( y_i \) is the class indicator e.g. +1 and -1 for a two class problem associated with each \( x_i \), \( N \) is the number of supporting vectors determined during training.

Figure 5: A support vector machine classification defined by a linear hyper plane that maximizes the separating margins between the classes.

Support vectors are elements of the training set that lie either exactly on or inside the decision boundaries of the classifier. In essence, they consist of those training examples that are most difficult to classify. The SVM classifier uses these borderline examples to define its decision boundary between the two classes.

4.2 SVM Kernel Functions

The kernel function plays a central role of implicitly mapping the input vectors into a high dimensional feature space, in which linear separability is achieved. The most commonly used kernel functions are the polynomial kernel given by:

\[ K(x,y) = (x^T y + 1)^p \]  \hspace{1cm} (11)

where \( p > 0 \) is a constant, and the Gaussian radial basis function (RBF) kernel given by

\[ K(x,y) = \exp \left( -\frac{||x-y||}{2\sigma^2} \right) \]  \hspace{1cm} (12)

where \( \sigma > 0 \) is a constant that defines the kernel width. Both of these kernels satisfy the Mercer condition mentioned earlier.
4.3 SVM Training

The fingerprints are classified by a Support Vector Machine (SVM). The feature vector created is used as an input pattern to the classifier. The SVM network needs to be trained well to be able to classify unknown patterns correctly.

We have manually labelled the fingerprint images according to the Henry classification to create a training set. Each classifier is trained using the feature vector extracted from these labelled images. The SVM classifier has been tested by presenting it to an unknown set of fingerprints to see how SVM is able to classify unknown patterns correctly. Fingerprint images with no core point or a core point too lose to an edge or segmented area is not used for training, due to false feature values. If such an image occurs in the classification stage, the images cannot be classified and must be matched against every other fingerprint in the final matching stage.

5 EXPERIMENTS AND RESULTS

A Support Vector Machine is trained according to the numbers specified in Table 1. Arch images have no singularities present, and a reference point of these fingerprints are thereby not possible by our methods. However, loops constitute about 65 percent of the total fingerprint patterns, whorls about 30 percent, and arches and tented arches together account for the other 5 percent (Karu, Jain, 1996). This makes the problem of not being able to classify arches less important.

Table 1: The number of training and testing instances for each fingerprint.

<table>
<thead>
<tr>
<th></th>
<th>Training</th>
<th>Testing</th>
</tr>
</thead>
<tbody>
<tr>
<td>LL</td>
<td>127</td>
<td>63</td>
</tr>
<tr>
<td>RL</td>
<td>123</td>
<td>59</td>
</tr>
<tr>
<td>TA</td>
<td>10</td>
<td>6</td>
</tr>
<tr>
<td>W</td>
<td>83</td>
<td>41</td>
</tr>
<tr>
<td>Total</td>
<td>343</td>
<td>169</td>
</tr>
</tbody>
</table>

We have used the LIBSVM library for SVM-classification (Chang, Lin, 2001). The SVM is trained using a Radial Basis Function kernel, as given in equation 13.

\[ K(\mathbf{x}_i, \mathbf{x}_j) = e^{-\gamma \|\mathbf{x}_i - \mathbf{x}_j\|^2}, \quad \gamma > 0 \]  

(13)

Before training, the parameters C and \( \gamma \) above have to be set to correct values. C is the penalty parameter of the error term and \( \gamma \) is a kernel parameter. By cross-validation, the best \( C \) and \( \gamma \)-values are found to be 8.0 and 0.001953125, respectively. We have used a one-vs-one approach to a multi-class problem. This splits our classification problem into six separate problems, that in the end are combined into one final set of support vectors. In total, this set, which is used for classification of the unknown fingerprints, contains 232 support vectors.

The classification results using SVM as a classifier are shown in Table 2.

Table 2: Classification results of each class using a SVM network.

<table>
<thead>
<tr>
<th>True Classes</th>
<th>Produced Classes</th>
</tr>
</thead>
<tbody>
<tr>
<td>LL</td>
<td>RL</td>
</tr>
<tr>
<td>LL</td>
<td>59</td>
</tr>
<tr>
<td>RL</td>
<td>1</td>
</tr>
<tr>
<td>TA</td>
<td>2</td>
</tr>
<tr>
<td>W</td>
<td>4</td>
</tr>
<tr>
<td>Best</td>
<td>96.8</td>
</tr>
</tbody>
</table>

From table 3 we see that the SVM classifier is able to classify the loops very well (93.7% and 93.2%), but is not able to classify the whorls and tented arches at the same rate.

A benchmark test was carried out on the whole set of fingerprints available to measure the average matching time of a fingerprint query by using a brute force search through the whole finger database compared to a regime with a classification stage. The benchmark test showed that the matching time was reduced with a factor of about 3.5 by introducing a classification in the AFIS regime.

Table 3: Classification rate for each class using a SVM network.

<table>
<thead>
<tr>
<th></th>
<th>Correct</th>
<th>Wrong</th>
<th>Percent Correct</th>
</tr>
</thead>
<tbody>
<tr>
<td>LL</td>
<td>59</td>
<td>4</td>
<td>93.7</td>
</tr>
<tr>
<td>RL</td>
<td>55</td>
<td>4</td>
<td>93.2</td>
</tr>
<tr>
<td>TA</td>
<td>2</td>
<td>4</td>
<td>33.3</td>
</tr>
<tr>
<td>W</td>
<td>31</td>
<td>10</td>
<td>75.6</td>
</tr>
<tr>
<td>Total</td>
<td>147</td>
<td>22</td>
<td>87.0</td>
</tr>
</tbody>
</table>

6 DISCUSSION

The performance rate of the SVM network has been estimated to about 87.0%. The SVM classifier failed in classifying most of the tented arch fingerprints, but this is because we believe there are too few training instances belonging to the tented arch class. SVM also performed better in classification of left loops and right loops than
classification of whorls. We believe that this is caused by the limited region-of-interest used to calculate the feature vector, causing many whorls to be wrongly classified as loops.

There are two main classes of whorls, classic whorl and double loop, and the double loop causes the classification problem. This is because the region-of-interest centred in the core looks quite similar in double loops and normal loops. Thereby, they can easily be misclassified as loops. A solution could be to increase the region-of-interest, but this would also increase the rejection rate, as more sectors would be outside the fingerprint area or even outside the entire image.

The experiments have shown that a SVM network is able to do a correct classification with a rate of about 87.0% on a four-class classification problem. To see how well such a classification rate is, it is compared with results obtained from literature. In [10], a classification algorithm based on the number of cores and deltas, and their relative positions, is presented. The authors achieved a correct classification rate of 85.4% on a five-class classification task.

In (Cappelli et al., 1999) one partitioned the directional image into connected regions according to the fingerprint topology, thus giving a synthetic representation which can be exploited as a basis for the classification. This method achieved a correct classification rate of 92.1% on a five-class classification task.

The authors in (Jain et al., 1999) used an approach similar to the one used in this paper, with the FingerCode as feature vector. The classification was done by a Multi Layered Perceptron (MLP) neural network. The network was able to achieve a correct classification rate of 86.4% on a five-class classification task and 92.1% on a four class classification problem.

In this paper a SVM network has been used in the classification stage. We observe that using a SVM network as a classifier gives nearly similar results as those found in the literature. From our experience with SVM network we believe that a larger database than was available would probably increase the performance rate, since a SVM network is capable to handle higher dimensional input spaces often in a better way than a MLP network and also generalize better. Such a classifier will then be more able to distinguish between more subtle differences of the fingerprint classes.

A benchmark test of a trained SVM network has been carried out on the total set of fingerprints to measure the average matching time of a query fingerprint compared to the query fingerprint using a subclass regime. The matching time of the last regime was also reduced by the factor of 3.5 compared to the brute force search regime.

7 CONCLUSIONS

One way to decrease the identification time of an AFIS is to divide a finger database into different subclasses so that a query fingerprint does not have to be tested against every fingerprint in the database. To solve such a problem we have implemented a classification stage in the AFIS by using a SVM classifier.

The SVM classifier is able to classify different unseen fingerprints with a performance rate of approximately 87.0%. However, by using a classification stage one is also able to reduce the average matching time compared to a total search which may be important when the fingerprint database is becoming huge.

However, the main objection by the method used in this paper is that the number of training examples are too small compared to the number of features in the FingerCode vector. By training the SVM with an extended training database we believe that the performance rate will greatly improve. Other types of neural networks may also be used to do the classification instead of the SVM network. This belongs to our future research.

REFERENCES


