BLOCK AND QUADTREE BASED SIMPLIFICATION IN TILED BLOCKS TERRAIN ALGORITHMS

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Abstract: With the advent of modern graphic processors, rendering a complex terrain in real time was suddenly possible. However the constant struggle between rendering quality and real time performance is still demanding more that we can actually get. Terrains are a prime example of that, the sheer amount of geometry and the constant need to achieve higher standards in image quality are always taking the graphical processors to their limits. Level of detail techniques, are therefore very important in this area and were used in multiple algorithms through the years. Tiled blocks are a category of terrain algorithms where the terrain is partitioned into square patches that are tessellated at different resolutions. This paper describes and compares two of the most common approaches used in the simplification process: block based simplification, where the simplification is local to the block, and quadtree based simplification, which uses the spatial partitioning principle of the quadtree to perform the simplification.

1 INTRODUCTION

Rendering terrain areas is an integral part of many applications, ranging from the entertainment industry to architectural visualizations, cartography applications and military simulations. Unfortunately it is still a difficult challenge, despite the ever growing power of the graphical processors available today. To cope with that, level of detail techniques appeared as an essential tool in this area especially for large terrains. Most of them were used in the course of years in a number of algorithms that were specially designed for the rendering of large terrains at interactive frame rates. Two of the most commonly used, especially by the game industry, are the Geomipmapping (Boer, 2000) and the Chunked LOD (Ulrich, 2002) algorithms. They belong to a class of terrain algorithms commonly described as Tiled Blocks, following the classification proposed in (Lossaso, 2004). In these algorithms, the terrain is partitioned into square patches that are tessellated at different resolutions. In the Geomipmapping algorithm the level of detail decreases by the individual simplification of each block. In the Chunked LOD algorithm the level of detail decreases by the substitution of four blocks by one that represents the same area. Our objective was to analyze these two approaches, not by the specific

features of each individual algorithm but in more general terms as two different simplification techniques shared by other algorithms in the same category. We called this two approaches block based and quadtree based simplification and they will be the focus of this paper.

This paper is organized as follows. In Section 2 we talk briefly about the evolution of terrain rendering algorithms giving special emphasis to tiled block approaches. In Section 3 the main concepts beyond the two types of simplification are explained. In Section 4 the common points in the two simplification methods are highlighted and how we unified them under a unique framework. In Section 5 the role of the error metric in the simplification process is described. In Section 6 are discussed methods to correct cracks between adjacent blocks with different levels of detail. In Section 7 geomorphing is described as the method used to correct the "popping" effect resulting from a change of detail. In Section 8 the testing environment and the particular features implemented for each simplification algorithm are described. In Section 9 results of the performed tests are presented and in Section 10 we summarize the conclusions and point out future work.

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2 RELATED WORK

Terrain rendering algorithms have a long history, and a comprehensive overview of this subject is beyond the scope of this paper. For a more detailed presentation, we refer the reader to (Pajarola, 2007). In the following we will briefly trace a temporal line covering the most important algorithms and trends with special emphasis on the tiled block techniques.

From a historical perspective the first algorithms specially designed for the rendering of terrains appeared in the late seventies, for example (Fowler, 1979). However it was only in the middle nineties, when consumer hardware was already capable of representing terrains in real time, that some of the most important algorithms appeared. Approaches like (Lindstrom, 96), (Duchaineau, 97) and (Rottger, 98) became very popular. For most of them the main objective was to reach the perfect triangulation reducing the number of triangles processed by the graphic card but increasing the work on the CPU side. However, with the appearance of powerful processors, graphical reaching the perfect triangulation stopped being the main objective. On the contrary, sending big blocks of geometric data to the GPU is now the dominating trend. This means that the focus switched from the triangle to blocks of geometry which became in this process the new target of level of detail techniques. To deal with this new reality new types of algorithms started to appear mainly tiled block approaches that applied level of detail techniques to blocks of geometry. Algorithms like (Boer, 2000), (Ulrich, 2002), (Laurisen, 2005) and (Vistnes, 2006) are only examples of approaches that followed this new trend. The most recent algorithms are taking this trend even further offloading most of the work to the graphical processor. They use concentric rings of detail that work on a focal area using a windowed view of the terrain. One of the main characteristics of this new approach is the usage of vertex textures, a new functionality of shader model 3.0. This functionality enables the sampling of a texture in the vertex shader. This is particularly useful for terrain rendering, since it enables the storage of the elevation values in a texture which can be used in the vertex shader to displace the vertices. Algorithms like (Asirvatham, 2005) (Clasen, 2006) and (Pangerl, 2008) are good examples of this.

3 SIMPLIFICATION METHODS

To comprehend the differences between block based

simplification and quadtree based simplification we have to understand precisely what happens in each one of the methods. For that, we will use a top view representation of a recursive walk on a quadtree in a 33x33 terrain with a 5x5 block, like the ones depicted in Figure 1. In this figure the triangle represents the frustum and the tessellated squares correspond to the blocks that are contained or intersected by the frustum. In Figure 1 a) all the blocks are at maximum resolution (5x5), so it represents the typical brute force approach to terrain rendering. Decreasing the resolution, i.e., level of detail of the blocks, is the purpose of block and quadtree based simplification. Block size is critical in these methods because the number of levels needed to represent the terrain in the quadtree is based on it.

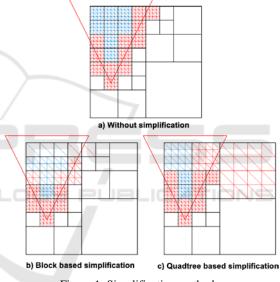


Figure 1: Simplification methods.

Let us start with block based simplification. This kind of simplification is depicted in Figure 1 b). In this method an error metric is used to determine the most appropriate level of detail for each block, so the simplification is completely independent from the one applied to the other blocks. Therefore it is common to have neighbouring blocks with different levels of detail. Moreover, the number of vertices changes according to the detail level but the size of the block is constant, so the number of draw calls issued in this method only depends on the number of blocks that intersect or are contained in the frustum.

With quadtree based simplification like the one depicted in Figure 1 c), the size of the block can change but the number of vertices in each block is constant. This kind of simplification uses the spatial partitioning principle of the quadtree to determine the most appropriate block size. More precisely an error metric is used on the recursive walk made on the quadtree to decide the most appropriate block size for each region of the terrain. Higher levels of the quadtree represent larger areas of the terrain with lower detail. Lower levels of the quadtree represent smaller areas of the terrain with greater detail. This works recursively from the root node of the quadtree to the leaf nodes where the underlying resolution of the terrain is matched. In this method the number of draw calls depends not only on the point of view but also on the error metric. Also, a block can have neighbours with different sizes, making any possible correlation between blocks difficult to achieve.

4 UNIFYING THE APPROACHES

Making a comparison between these two approaches will be surely flawed if they are seen as completely different. The common point here is the underlying spatial partitioning structure, the quadtree. With that in mind we can differentiate the two methods by assuming that each one represents a different way of making the recursive walk on the quadtree. With a block based simplification scheme the quadtree is used only to identify the visible blocks, i.e. blocks that are intersected or are contained in the frustum. No level of detail is calculated at this stage and all these blocks are at the same level in the quadtree as they have the same block size. Therefore one possible optimization is to stop the recursion sooner, when we reach a node that is completely contained in the frustum even if the resolution of that node does not match the desired block size. For example, if the first quadrant of the first level of the quadtree is completely contained in the frustum, we can stop the recursion for that branch adding all the blocks of the desired block size that are contained in this larger block. Finally for each one of these blocks we have to choose the most appropriate level of detail basing our decision on the error metric. With quadtree based simplification the main difference lies on the recursion which can stop sooner because the level of detail evaluation is done for each node of the quadtree so it is possible to choose larger blocks and render them. These larger blocks have the same number of vertices but the space between those vertices is greater.

To unify this approaches even further we take advantage of a very useful property in a regular grid triangulation: every block can be described by a scale and a translation factor. To make this property useful we have to separate the elevation values from

the geometric description of the block. This is achieved with two vertex streams. A vertex stream is essentially an array of vertex component data. For instance it is possible to assemble vertices from several vertex streams, where each stream consists of a component of the vertex (e.g., one stream contains position info, another contains colour info, another texture coordinate info, etc.). In our approach the first stream contains the position of the vertices and the second stream contains the elevation values. Since we use canonical values for the position of the vertices this vertex data is valid for all the blocks of the terrain. Later when rendering, we transform the canonical values in the vertex shader to obtain the correct position of the block. For that we only need a couple of uniform shader parameters, in this case, the scale and the translation associated with each block.

The main advantage of a multi-stream approach is that it enables us to use vertex textures in machines that support shader model 3.0. In this case, the memory requirements are reduced since we only need one stream with the geometric description of the block because the elevation data is stored on a texture. Without vertex textures we need to send the elevation values in a second stream.

To connect the vertices in a block we need a list of indices, however this list is different in each method. With quadtree based simplification we only need to describe a block since in this method the geometrical structure of the block does not change, only the area that it occupies. With block based simplification we need to represent all the possible levels of detail of a block. For example if we have a 5x5 block, like the one used in the previous figures, we need to represent a 5x5, a 3x3 and 2x2 block. This is done with different sequences of indices each one representing one of the aforementioned levels of detail.

5 ERROR METRIC

The error metric has a very important role to fulfil in tiled block algorithms as it is used to decide when the transition to lower/higher detail levels happens. With block based simplification it is used to control the level of detail of the block, i.e., when a higher/lower detailed version of the block should be used to represent the associated region on the terrain. With quadtree based simplification it is used to decide the number of blocks that should represent a region of the terrain, more precisely when a block can be substituted by its four more detailed children or the other way around, to decide when four blocks can be substituted by its less detailed parent.

The error metric used in the two algorithms is the one presented in the Geomipmapping algorithm (Boer, 2000), which uses block based simplification. This error metric can be easily adapted, as described in (Laurisen, 2005), to a quadtree based simplification. It involves the calculation of a constant C in a pre-processing stage and of a minimum distance D, for each level of detail n.

The constant C is calculated with Equation 1, where n is the near clipping plane, t the top coordinate of the near clipping plane, τ the error threshold in pixels and Vres the vertical resolution in pixels

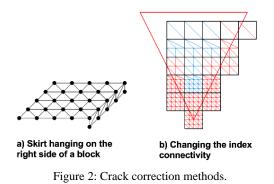
The D for each level of detail n is calculated with Equation 2, where δ is the geometric error and C the constant calculated with Equation 1.

$$C = \frac{n}{|t|} \times 1/\left(\frac{2 \cdot \tau}{V_{res}}\right) \tag{1}$$
$$D_n = |\delta| \cdot C \tag{2}$$

6 SPATIAL COHERENCE

The appearance of cracks between neighbouring blocks with different levels of detail is a common problem in tiled block approaches like the ones described in this paper. There are several ways to correct this problem but most of them are far from ideal as they have a very noticeable impact in performance. The fastest methods are the ones that do not imply changes to the list of vertices or to the list of indices committed to the graphical processor. Adding vertical skirts around each block is a solution that meets this objective. This method was first introduced in (Ulrich, 2002) and is represented in Figure 2 a). However, we should select carefully the skirt size since it can have big impact in the fill rate. It should be big enough to cover any possible cracks that can appear between the tile and the neighbouring tiles but not greater than that.

Note that, for optimal performance the skirts have to be drawn in the same call as the block so the vertices and the indices should be arranged to make that possible. This technique can be used with block or quadtree based simplification. However this method does not correct the geometry, in fact the difference of height between adjacent tiles is only hidden by the skirts. Another technique that can be used to correct the cracks is to change the connectivity (or indexing) of the vertices at the edge of the block. This was originally suggested in (Boer, 2000) and is exemplified in Figure 2 b) for block based simplification where the tile with the higher level of detail adapts its borders to the level of detail of its neighbour(s). This technique implies changes to the list of indices at runtime and therefore it is not completely static, quite the contrary of skirts.



Unfortunately it cannot be used with quadtree based simplification, since adjacent blocks can change in size. This means that a block can have triangles bigger than its neighbours. For example, it can happen that a triangle spans two or more neighbouring blocks. In these cases any change in the index connectivity of the neighbours will not

7 TEMPORAL COHERENCE

correct the problem.

Another important problem with tiled blocks and with level of detail algorithms in general is the so called "popping" effect. This is the result of a sudden change of detail (to more or less detail) which can originate a very noticeable effect. This is caused by the appearing or disappearing of vertices which cause a sudden "pop" in the geometry that is very unnatural and contributes negatively to the level of realism that we are trying to achieve. The most common way of handling this problem is with geomorphing (Luebke, 2003). The objective is to slowly morph the vertices from one level of detail to another. This can either be done over time or based on the error. The latter is the best approach since in this way the morphing only occurs when the viewpoint is moving which helps hide the swirling artefacts that it can cause. Concerning the simplification methods discussed in this paper there is no noticeable differences between the two approaches since what we really need to know when moving between levels of detail is which vertices disappear and the error that results from that. This is what is normally needed to perform the geomorphing. Therefore all we need to do is to store that information in the list of elevation values since it changes with each elevation value. This raises a problem when we use vertex textures to displace the vertices in the vertex shader since in that situation we do not have a list elevation values, but only one texture. The solution is to use another texture to store for each vertex the level where it disappears and the resulting error.

The morphing itself is executed on the vertex shader. Since we receive all the necessary data this is normally very fast and therefore it should be used whenever possible as it can help increase the realism significantly.

8 TESTING FRAMEWORK

We have developed a framework in XNA which unifies under the same architecture the most relevant characteristics of tiled blocks algorithms. With this framework we have implemented the two simplification methods and a brute force approach where we did not make any simplification. The results of brute force algorithm are used as baseline performance values. We have also implemented frustum culling which uses the quadtree to test each block against the frustum as was already mentioned in Section 4. To reach meaningful results it was equally important to use the same error metric in the simplification methods. Geomipmapping (Boer, 2000) error metric was adopted as explained in section 5. To correct the cracks we have used the skirt and the index update methods described in Section 6 and to correct the "popping" effect we have implemented geomorphing using the approaches described in (Boer, 2000) and (Laurisen, 2005) for each one of the simplification methods.

Concerning the lightning we used per-pixel lightning also known as normal mapping (Kilgard, 2000). Finally for the texturing of the terrain we have used one colour texture.

9 RESULTS

The tests were performed on three computers: a laptop with a Mobile Intel 945 GM graphical card, which we called N1, a laptop with a ATI Mobility Radeon 9700, which we called N2, and a desktop with a NVIDIA GeForce 7950 GX2 graphical card, which we called D1. These setups represent two low end systems with a graphical card that support shader model 2.0 and a high-end system with a graphical card that supports shader model 3.0. Two procedurally generated terrains were used in the

tests: a 1025x1025 terrain, called Terrace, and a 2049x2049 terrain, called Highland.

To gather the performance results we have prerecorded a 60 seconds walk on each terrain at relatively low altitude.

The results obtained using two streams, vertices and elevation values, are summarized in Table 1 where it is possible to compare the average frames per second obtained in each terrain. For each machine we have measured the performance of the brute force approach and of the two simplification methods discussed in this paper. We have considered three different block sizes, 17x17, 33x33 and 65x65 and two types of crack correction methods: index update and skirts. We have used a maximum error of 8 pixels.

simplification method The quadtree in conjunction with skirts was the fastest approach in two of the three machines considered. This was expected as the number of draw calls is much lower in this method. The only exception was the N2 machine where block based simplification was faster. On the N1 machine, the slowest, it makes in fact the difference between a working real time representation of the terrain with a frame rate above the 60 frames per second and a slow representation almost unusable and is therefore an obvious choice. The fastest block size was 17x17 with the exception of machine N2 where the fastest block size was 33x33. However, on that machine the fastest simplification method was also different and the two simplification methods analyzed use different ways of reducing the detail.

Concerning the crack correction methods used in block based simplification, in almost every situation the index update method was slower. In fact it had a tremendous impact in the performance mainly in machines N2 e D1. As we have already mentioned in Section 7, index update implies changes in the list of indices at runtime and this results confirm that it can cause a significant frame rate drop.

We have also tested the performance with vertex textures this time only on the D1 machine since it is the only that supports shader model 3.0. The results are summarized in Table 2.

If we compare the results in Table 2 with the results obtained for the same machine in Table 1 we can see that using vertex textures is slower. This was expected since this behaviour was already observed by other authors, for example it is mentioned in (Asirvatham, 2005), (Clasen, 2006) and on (Pangerl, 2008). However with vertex textures the fastest method was block based simplification which shows that sampling a vertex texture with quadtree based simplification is somewhat slower than with block based simplification.

Terrace 17x17 52 52 49 126 N1 33x33 43 55 55 99 65x65 26 59 65 45 N2 33x33 102 146 229 180 65x65 92 143 176 139 0 65x65 92 143 176 139 17x17 606 190 532 1336 D1 3x33 567 328 1302 1051 65x65 514 357 1070 791 Highland 17x17 14 14 13 75 N1 33x33 13 17 17 51 65x65 7 22 25 24 N1 33x33 37 51 174 129 65x65 33 72 131 95 91 D1 3x33 188 10			Brute Force	Block (Index Update)	Block (Skirts)	Quadtree (Skirts)
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17x17 38 23 74 159 N2 33x33 37 51 174 129 65x65 33 72 131 95 17x17 149 44 121 919 D1 33x33 188 101 498 690	N1	33x33	13	17	17	51
N2 33x33 37 51 174 129 65x65 33 72 131 95 17x17 149 44 121 919 D1 33x33 188 101 498 690		65x65	7	22	25	24
65x65 33 72 131 95 17x17 149 44 121 919 D1 33x33 188 101 498 690		17x17	38	23	74	159
17x17 149 44 121 919 D1 33x33 188 101 498 690	N2	33x33	37	51	174	129
D1 33x33 188 101 498 690		65x65	33	72	131	95
		17x17	149	44	121	919
65x65 177 127 785 511	D1	33x33	188	101	498	690
		65x65	177	127	785	511

Table 1: Average frames per second.

Table 2: Average frames per second with vertex textures.

		Brute Force	Block (Index Update)	Block (Skirts)	Quadtree (Skirts)
Teri	ace				
D1	17x17	384	217	602	742
	33x33	256	347	834	329
	65x65	216	348	436	252
High	land				
D1	17x17	105	52	131	464
	33x33	75	112	480	217
	65x65	66	125	356	136

10 CONCLUSIONS

We analyzed two of the most common simplification methods used in tiled block approaches to terrain rendering. We have discussed algorithms and techniques to keep temporal and spatial coherence, respectively, geomorphing and skirts or index update. We have come to the conclusion that quadtree based approaches are the best option in most of the situations, mainly when the terrain is very large and/or the machine is slow. In these cases the reduction of the draw calls has a very noticeable impact in terms of performance.

We have also concluded that skirts are the best approach to handle the cracks. The other method implies changes to the list of indices at runtime and affected performance significantly.

In the future we plan to analyze the impact of occlusion culling techniques on the performance of each simplification method and also to pursue new approaches to the correction of cracks mainly the generation of all the possible combinations between a level of detail of a tile and its neighbour's level of detail in block based simplification. We are also planning support out-of-core data to cope with terrains with sizes beyond the available memory.

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