EFFICIENT PLANAR CAMERA CALIBRATION VIA AUTOMATIC IMAGE SELECTION

Brendan P. Byrne, John Mallon and Paul F. Whelan
Centre for Image Processing & Analysis,
Dublin City University, Dublin 9, Ireland

Abstract: This paper details a novel approach to automatically selecting images which improve camera calibration results. An algorithm is presented which identifies calibration images that inherently improve camera parameter estimates based on their geometric configuration or image network geometry. Analysing images in a more intuitive geometric framework allows image networks to be formed based on the relationship between their world to image homographies. Geometrically, it is equivalent to enforcing maximum independence between calibration images, this ensures accuracy and stability when solving the planar calibration equations. A webcam application using the proposed strategy is presented. This demonstrates that careful consideration of image network geometry, which has largely been neglected within the community, can yield more accurate parameter estimates with less images.

1 INTRODUCTION

Camera calibration from planar targets is the dominant configuration when working with conventional perspective cameras. Its foundations were proposed independently by Sturm and Zhang (Sturm and Maybank, 1999; Zhang, 1999) and are well understood within the community today. Compared with traditional calibration techniques (Faugeras, 1993; Tsai, 1987; Wei and Ma, 1994), plane based calibration significantly reduces input data requirements. This coupled with readily available implementations, (Bouget, 2001; OpenCV, 2001), has contributed to its popularity.

Planar calibration simply requires the user to capture at least two images with varying planar target pose. We call these images the image network (IN). Typically many more images are used to improve calibration accuracy. The stability of planar calibration methods has been well studied in the literature ( Gonzalez et al., 2005; Salvi et al., 2002; Sun and Cooperstock, 2007). Generally the stability is characterised based on the reprojection error which is the Euclidean distance between the 3D world points, back projected onto the image plane, and the measured 2D image points. In all cases findings suggest that larger INs increase parameter estimation accuracy.

Although large INs yield more accurate results, practical constraints such as capturing a large data set, feature extraction, and calibration takes a considerable amount of time and expertise. To this end it would be desirable to achieve good calibration accuracy within these practical constraints. Thus the focus should be on forming smaller INs capable of producing accurate results. This paper outlines how this is achieved via automatic image selection (or a Selected Image Network (SIN)).

The possibility of degeneracies increases when considering a smaller image set. The degeneracies effect the conditioning of the planar calibration equations and lead to poor parameter estimates. Critical configurations have been identified and well studied by (Sturm and Maybank, 1999) and (Zhang, 1999) and shown to consist of pure rotation and translation, but images close to critical, which are difficult to identify and have received less attention in the community, also give poor results.

In (Rupp and Elter, 2007), an image selection strategy is employed to improve calibration results. However, the algorithm selects images based on their reprojection error which requires the camera to be calibrated in the first place. This defeats the purpose of an efficient calibration via image selection and adds considerable time and effort in doing so. Also, by us-
Thus a single planar homography matrix age plane it remains in homographic correspondence. world plane rotates about its intersection with the im-

proposed by (Gurdjos, 2001). In Figure 1, as theacteristics from the alternative geometric approach

The proposed algorithm selects images based on char-

2 METHOD

The proposed algorithm selects images based on character-

istics from the alternative geometric approach pro-

posed by (Gurdjos, 2001). In Figure 1, as the world plane rotates about its intersection with the image plane it remains in homographic correspondence. Thus a single planar homography matrix $H$ represents the transformation. The associated camera centres, of each rotating world to image plane, forms a locus of possible camera centres which in turn projects to the image plane in the form of a line, the Calibration Line (CL). By using the well known (Sturm and Maybank, 1999; Zhang, 1999) planar calibration equations constraints (1), and following some algebraic manipulations, an expression for the CL can be derived (2).

$$h_i^T \omega h_1 = h_i^T \omega h_2 = 0, \text{ } h_i^T \omega h_2 = 0$$ \hfill (1)

where $h_i$ is the $i$th column of $H$.

$$v_0 = \Gamma u_0 + \Lambda$$ \hfill (2)

where $\Gamma$ is the slope of the CL given by,

$$\Gamma = \frac{-h_{13}h_{32} + h_{12}h_{31} - h_{11}h_{32} + h_{12}h_{31}h_{32}}{h_{22}h_{31}h_{32} - h_{21}h_{31}h_{32} - h_{21}h_{32} + h_{22}h_{31}}$$ \hfill (3)

and $\Lambda$ is the y-intercept given by,

$$\Lambda = \frac{h_{21}h_{31} + h_{22}h_{32}}{h_{31}^2 + h_{32}^2} - \frac{h_{11}h_{31} + h_{12}h_{32}}{h_{31}^2 + h_{32}^2} \Gamma$$ \hfill (4)

In (Wang and Liu, 2006), the authors propose a method of linear calibration using the intersection point of CLs. In our method we use the CLs as a guide to choosing calibration images for the SINs. Suitable images are selected based on the orientation of their CLs. Since the CL encapsulates geometric information about the planar grid in the world, enforcing maximum independence between CLs ensures each image contributes independently to solving the system of planar calibration equations. Independence between images is evaluated based on the relative angle between image CLs. The angle between CLs, $\theta$, is dependant on the number of images in the IN ($N$).

$$\theta = \frac{180^\circ}{N}$$ \hfill (5)

Therefore if a four IN is required from a data set the angle between image CLs should be $45^\circ$. In practice, a tolerance of $\pm 1^\circ$ is enforced on $\theta$ for the selection process. Based on the homographies from multiple images, we employ an algorithm to select the most suitable images which will provide efficient calibration results.

3 IMAGE SELECTION

Automatic image selection is implemented in two stages. The initial step requires each image CL to be formed (as in section 2) with the angle of each CL relative to the x-axis calculated via the slope (arctan($\Gamma$)). CLs that have absolute angle near 0° or 90° are rejected for consideration as they correspond to unstable IN geometry (fronto-parallel). Once $N$ is chosen the optimal $\theta$ can be calculated (5) which is used to form the SINs.

The underlying search method of the proposed image selection strategy is a binary search approach (Knuth, 1998). In Figure 2 the proposed strategy is presented. Each node represents an image number while the number adjacent to each node is its CL orientation. In a real situation all nodes are connected to each other where the connecting lines represent the angle between image CLs. To aid explanation all possible connecting lines are not shown, instead the valid search paths are shown i.e each line is in fact equal to the binary search key which is $|\theta| \pm 1$.

In this example, $N$, the number of images required in the SIN, is set to four therefore $\theta$ is $45^\circ$. The search begins with the seed node 1. When a route
corresponding to the search key is identified (node 3) the search continues with node 3 as the seed. In this case there are two possible routes, node 12 and 17. Since a binary search exploits only one route at a time, the proposed strategy implements the search in a cascaded fashion. Therefore the search will return to this point and follow other routes in the next cycle. If node 12 is chosen there are three candidates to form the SIN - 22, 31 and 64. When one possibility is chosen the SIN is formed and the node is deleted. This will allow the binary search to find the next valid IN with subsequent searches. When all possible SINs along the (1,3,12) route have been formed, all image nodes are reintroduced but node 12 is deleted. This enables the algorithm to return to the point (1,3) and follow route 17. The search continues in this fashion until all valid routes have been identified.

![Figure 2: Image Space](image)

**3.1 Search Algorithm Implementation**

The implementation of the search algorithm is presented in Figure 3. The algorithm is initialised with the seed node which is stored in the IN matrix. The binary search is implemented and if it’s successful, the current IN size, \( N_T \), is incremented and the image found, \( int \), is stored in IN. A check is performed to see if \( N_T \) is equal to \( N \) the desired IN size. If true the current \( int \) is deleted from the search space and the algorithm loops back to run the binary search again. This is a similar situation as in Figure 2 when tier 4 was reached, the node was deleted so other nodes could be found in subsequent searches. In the case where \( N_T \neq N \), the algorithm simply loops back to find the next image in the network via the binary search.

The most significant branch point in the algorithm is the binary search junction. When a search fails it indicates that there are no more routes in a particular tier of the search space. A check is performed on \( N_T \) to see if the search has failed in tier 2 (i.e. if \( N_T = 1 \)). If it has failed the overall search is finished and all valid INs are stored in the IN matrix. On the other hand, if \( N_T \neq 1 \), all nodes are reintroduced to the search space and the \( N_T \) node of the current IN is deleted from the list. This is a similar situation to the example given in Figure 2 where the IN was \( (1,3,12) \). When all tier 4 nodes were found and subsequently deleted, node 12 was removed which allowed the binary search to follow the \((1,3,17)\) route. The search continues until \( N_T = 1 \) which indicates that all possible routes have been explored. The algorithm is implemented in this fashion for each node in the search space. Further refinement can be applied to the algorithm if duplicate INs are stored.

![Figure 3: Algorithm Flowchart](image)

**4 APPLICATION**

A webcam calibration application was developed to demonstrate the benefits of the image selection scheme. A labtec “web” webcam capturing 15fps at \( 320 \times 240 \) pixels was used. The application captures images for 20 seconds thus giving 300 images for the calibration data set. Images are captured by varying the location of the camera, while also ensuring the planar calibration target remains within the field of view of the webcam. OpenCV is used to extract the planar pattern corners from each frame to subpixel accuracy. The homographies are calculated for each frame followed by implementation of the proposed image selection algorithm to identify the SINs. The planar calibration method of (Zhang, 1999) is used to verify results.

**5 RESULTS**

Validation of the SINs is performed by comparison with randomly drawn INs from the data set. Random INs (RIN) are used as there are no specific methods to compare with currently in the literature. Three experiments are conducted to illustrate the calibration
accuracy and overall benefit of using SINs. The first experiment examines the accuracy of the calibration result as the number of views increases. This is followed by a rigorous comparison of the IN configurations with less images. The final experiment validates the calibration accuracy of SINs by analysing the lens distortion in the images. As there is no ground truth a calibration result is calculated using all 300 frames and used as an indicative optimal result for comparison.

5.1 Convergence of Image Networks

This experiment examines the accuracy of the calibration result as the number of images in the IN increases. The results are given in terms of percentage error for each calibration result. For each image network instance (2 to 25 INs) ten SINs are compared with ten RINs from the data set. From Figure 4, it is evident that the SINs produce more accurate and reliable calibration results than the RINs, especially for the smaller INs. As the number of views increases the stability of the SIN results clearly outperform the RINs. The most significant result here is that less images are needed to achieve accurate calibration results when SINs are used. The following experiment examines this in more detail.

![Convergence of SIN v RIN](image)

Figure 4: Calibration accuracy as the number of views increases from 2 to 25 INs. Standard deviation is represented by bars at each IN instance.

5.2 Reduced Number of Images

The number of images for each IN configuration is reduced for this set of experiments to validate the previous results which identified that SINs can achieve more accurate results than the RINs with less images. All results in Table 1 are given in terms of percentage error with respect to the indicative optimal calibration results. There are 50 two INs, 30 three and 25 four INs in the SIN cases of Table 1. The RINs consist of 2500 randomly drawn image combinations for each IN size. This consisted of 50 trials of 50 IN instances for each test. This insured that a wide range of RINs were compared for the results.

The results in Table 1 indicate that the SINs significantly outperform the RINs. This is due to the geometry of the SINs, which avoid degenerate configurations, and also have favorable image geometry for solving the calibration equations more efficiently. This is a significant result in terms of the input requirements for planar camera calibration, by exploiting geometric properties of the images, less input images are needed to achieve accurate calibration results.

<table>
<thead>
<tr>
<th>Image Network Consensus</th>
<th>No. Images</th>
<th>fx (\overline{x} (\sigma))</th>
<th>fy (\overline{y} (\sigma))</th>
<th>u (\overline{u} (\sigma))</th>
<th>v (\overline{v} (\sigma))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Random</td>
<td>2</td>
<td>23.3 (\pm 1.9)</td>
<td>20.7 (\pm 2.3)</td>
<td>23.7 (\pm 1.3)</td>
<td>23.5 (\pm 2.1)</td>
</tr>
<tr>
<td>SIN</td>
<td>2</td>
<td>11.5 (\pm 1.7)</td>
<td>11.1 (\pm 1.7)</td>
<td>13.3 (\pm 1.3)</td>
<td>24.1 (\pm 1.6)</td>
</tr>
<tr>
<td>Random</td>
<td>3</td>
<td>20.2 (\pm 3.9)</td>
<td>20.5 (\pm 3.9)</td>
<td>24.2 (\pm 7.5)</td>
<td>25.1 (\pm 7.9)</td>
</tr>
<tr>
<td>SIN</td>
<td>3</td>
<td>3.8 (\pm 3.9)</td>
<td>3.6 (\pm 3.9)</td>
<td>5.3 (\pm 7.5)</td>
<td>9.9 (\pm 7.9)</td>
</tr>
<tr>
<td>Random</td>
<td>4</td>
<td>8.9 (\pm 21.1)</td>
<td>8.9 (\pm 21.1)</td>
<td>10.8 (\pm 22.9)</td>
<td>11.1 (\pm 19.4)</td>
</tr>
<tr>
<td>SIN</td>
<td>4</td>
<td>1.59 (\pm 1.69)</td>
<td>1.49 (\pm 1.69)</td>
<td>2.74 (\pm 3.31)</td>
<td>3.88 (\pm 3.32)</td>
</tr>
</tbody>
</table>

5.3 Distortion Correction

This experiment further justifies the use of the SINs by analysing distortion in the images. The benefit of un-distorting the images is that the canonical calibration plane is used as ground truth which gives the distortion correction residuals. Calibration results using two INs is used for this experiment since it is the minimum case for solving planar calibration. The plots in Figure 5 represent the error vectors of the un-distortion estimation (scaled by 20 for plots). The SINs have removed most radial distortion from the image (mean residual 0.2 pixels) whereas the random network still has significant distortion present (mean residual 0.39 pixels).
6 CONCLUSIONS

This paper has presented a new approach to choosing planar calibration images which give accurate calibration results. This is accomplished by considering geometric aspects of images in the form of the CL and thus forming selected image networks (SINs). Unlike previous image selection methods it does not require a pre-calibration stage, it simply takes the image set and calibrates based on the image CLs. This ensures independence in the calibration images and avoids degenerate configurations. Experimentation has shown that less input images are needed to achieve efficient results using SINs. The application presented also provides a simple means of achieving accurate results for non-expert practitioners, as the only input needed is varying the camera location while capturing the images.

ACKNOWLEDGEMENTS

This research is funded by the Irish Research Council for Science, Engineering and Technology: funded by the National Development Plan.

REFERENCES