JUMPING JACK
A Parallel Algorithm for Non-Monotonic Stream Compaction

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Abstract: Stream Compaction is an important task to perform in the context of data parallel computing, useful for many applications in Computer Graphics as well as for general purpose computation on graphics hardware. Given a data stream containing irrelevant elements, stream compaction outputs a stream comprised by the relevant elements, discarding the rest. The compaction mechanism has the potential to enable savings on further processing, memory storage and communication bandwidth. Traditionally, stream compaction is defined as a monotonic (or stable) operation in the sense that it preserves the relative order of the data. This is not a full requirement for many applications, therefore we distinguish between monotonic and non-monotonic algorithms. The latter motivated us to introduce the Jumping Jack algorithm as a new algorithm for non-monotonic compaction. In this paper, experimental results are presented and discussed showing that, although simple, the algorithm has interesting properties that enable it to perform faster than existent state-of-the-art algorithms, in many circumstances.

1 INTRODUCTION

Current Graphics Processing Units (GPUs) are programmable parallel platforms which provide high computational power with very large memory bandwidth at low cost. These features make them compelling not only under the graphics domain but also for computationally intensive general purpose tasks, leading to a relatively new research area focused on mapping general purpose computation to graphics processing units - GPGPU (Owens et al., 2007; GPGPU, 2008).

Stream compaction, also designated as stream non-uniform reduction and also as stream filtering, takes a data stream as input, uses a discriminator to select a wanted subset of elements, outputs a compacted stream of the selected elements, and discards the rest.

Several computer graphics applications, making use of the GPU programmable architecture, may benefit from stream compaction. Exclusion of non-relevant elements permits savings on further computational tasks, better memory footprints, and reduced overhead when transferring data from the GPU to the CPU. Stream compaction is also a fundamental component on algorithms dealing with data partitioning (e.g. some sorting algorithms and space hierarchies). Parallel stream compaction is typically based on another fundamental data parallel primitive, the parallel prefix sum (Blelloch, 1990).

Conventionally, stream compaction is referred as an order-preserving (or monotone) operation, i.e. the output preserves the relative order of the elements. In some circumstances, this can be a rather restrictive requirement. There are applications where monotonicity is not fundamental, as when the data is self-indexed (e.g. the data have coordinates, or a color index) or when the relative order is irrelevant to further processing. Therefore, we clearly distinguish two classes of stream compaction: monotonic compaction and non-monotonic compaction. The latter class motivated us to design the herein introduced Jumping Jack algorithm.

Divide-to-conquer strategies, such as segmented prefix-sum (Blelloch, 1990; Sengupta et al., 2007) and hierarchical stream compaction (Roger et al.
allow for processing large amounts of data and lead to increased efficiency.

The herein introduced Jumping Jack algorithm makes use of a similar strategy, *Block Stream Compaction*: it first splits the input into regular smaller blocks of data, compacts them, and finally concatenates the partial results into the desired compacted output stream. The block concatenation step uses the vertex engine and the texturing units of the GPU, in order to achieve a better computational complexity with respect to a global compaction approach.

The rest of the paper is organized as follows. Next section introduces some fundamental concepts and terminology on programmable graphics hardware. Section 3 reviews relevant prior work on scan primitives and stream compaction. The proposed Jumping Jack algorithm is presented in Section 4 and relevant details on the implementation are given in Section 5. The achieved results are presented and discussed in Section 6. Major conclusions are summarized in Section 7 alongside with possible directions to future work.

## 2 PROGRAMMABLE GPU ARCHITECTURE

Here we briefly introduce some fundamental concepts and terminology exhaustively used through the paper. The current OpenGL specification (OpenGL 2.1) exposes two GPU programmable units: the vertex and the fragment processors. A third programmable unit, the geometry processor, was recently exposed through OpenGL extensions but it has limited support and it is only available on very recent GPUs. GPUs are designed with several vertex and fragment processor units, enabling high levels of parallelism. Vertex and fragment programs can be coded in high level languages such as the OpenGL Shading Language (aka GLSL), HLSL and Cg, to name the most popular. A simplified scheme of the programmable pipeline is presented in Figure 1.

A vertex program processes each vertex independently. The vertex processor has the ability of modifying the vertex positions, which can be used to redirect the output to a desired position, giving it memory *scattering* abilities (indirect writing). Memory *gathering* (indirect read) is possible at the vertex processor through texture fetching. Although conceptually interesting, the traditionally reduced number of vertex pipelines, the limited support for texture formats and the unoptimized read accesses (with big latency), impose limitations on the practical utility of such gathering mechanism.

At the fragment processor, each fragment is processed independently, with the fragment final position being pre-determined before the fragment is processed. Therefore, the fragment processor does not have *scatter* abilities. However, gathering is possible through texture fetching. A fragment program is allowed to render to texture target (RTT) and also to render to multiple targets (MRT), enabling it to easily re-use results from one pass to another. Rendering directly to the vertex buffer (RTVB) is not a widely supported mechanism, although it can be indirectly achieved in several ways.

Recently, GPU manufacturers adopted the so-called *unified architecture model*, comprising several (dozens to hundreds) of indistinct stream processors. Furthermore, global load-store memory, shared memory for threads running on the same multiprocessor and synchronization mechanisms, are some of the available capabilities. However, such capabilities have only been exposed through manufacturer dependent application programming interfaces (APIs) and tools (e.g. such as nVidia CUDA (Nickolls et al., 2008)), without support by architecture independent or by general purpose APIs.

The herein proposed algorithm is intended to allow implementations making use of widely supported GPU capabilities, such as the exposed by OpenGL. It is assumed that the GPU has programmable vertex processors with scatter and (potentially limited) gather abilities and programmable fragment processors with gather abilities but without scatter.

## 3 RELATED WORK

This section reviews relevant prior work on stream compaction. As existent algorithms are typically
based on prefix-sums, we begin by introducing the fundamental concepts and algorithms for parallel prefix sum and segmented prefix-sum in the first two subsections, with a special focus on their GPU implementation. The following subsection describes parallel stream compaction and approaches to implement it.

### 3.1 Prefix-Sum

The prefix-sum primitive (aka scan operation and also as prefix-reduction) is probably one of the most important primitives for parallel computing (Sengupta et al., 2007). This can be somewhat surprisingly, as the prefix-sum primitive is mostly unnecessary on sequential computation. Prefix-sum is successfully used as a fundamental strategy in the parallelization of algorithms that seem to be inherently sequential (Hillis and Steele JR, 1986; Blelloch, 1990).

The all-prefix-sum (or inclusive prefix-sum) operation (Blelloch, 1990) takes a binary associative operator \( \oplus \) and an ordered set of elements (e.g. an array or stream) \([a_0, a_1, \ldots, a_{n-1}]\) and returns an ordered set \([a_0, (a_0 \oplus a_1), \ldots, (a_0 \oplus a_1 \oplus \cdots \oplus a_{n-1}]\).

Typical prefix-sum operations use addition, maximum, minimum, product and logic operators, but any associative operator can be used. In the rest of this paper, addition will be used as the default operator for prefix-sum.

On sequential architectures, the all-prefix-sum operation is trivially implemented with linear time complexity \(O(s)\) using a single pass over the data. However, parallel computation of the all-prefix-sum can not be straightforwardly mapped from the sequential algorithm. Observe that each output depends on several input elements, as for instance, the computation of the prefix-sum at the last element (rightmost) involves all the others.

Horn (Horn, 2005) proposed a GPU implementation for a linear all-prefix-sum primitive based on a parallel recursive doubling algorithm as described by Hillis & Steele (Hillis and Steele JR, 1986) that is often utilized in parallel and high performance computing. Hensley et al. (Hensley et al., 2005) also used a parallel recursive doubling algorithm to carry out fast GPU based generation of summed area tables (SAT). SAT generation extends the recursive doubling into a 2D data structure by operating in two directions.

The recursive doubling approach proceeds as follows. For each element, and in parallel, the algorithm starts by summing to each element the value of the element placed one position to the left. In the next iteration, each element will sum itself to the value stored two positions to the left. By now, each record stores the sum of four original values, from its own position to three positions to the left; following iterations recurse the process doubling the offset to the left. For a stream with size \(s\), the algorithm iterates \(\log_2(s)\) times to complete. If there is a number of processors that equals the size \(s\) of the stream, the algorithm completes in \(O(\log(s))\) time leading to a total work of \(O(s \cdot \log(s))\). A graphical depiction of this process is illustrated in Figure 2.

![Figure 2: Parallel Prefix Sum using a recursive doubling algorithm for a stream with \(s = 8\) elements.](image)

**Algorithm 1**: Double Buffered Parallel All-Prefix-Sum.

```
begin
input : s : stream length
input : pSum\[in\] : input data stream
output : pSum\[out\] : all-prefix-sum stream
for p ← 1 to \(\log_2(s)\) do
offset = \(2^{p-1}\)
forall i < s in parallel do
  if i ≥ offset then
    pSum\[out\][i] ← pSum\[in\][i − offset] \(\oplus\) pSum\[in\][i]
  else
    pSum\[out\][i] ← pSum\[in\][i]
  end
swapBuffers\(\text{(in, out)}\)
end
```

As the GPU programming model does not allow for concurrent read and write on the same memory buffer, the usual workaround comprises using double buffered memory, i.e. two temporary streams (textures) and making one of the input (for read-only accesses by means of texture fetching, which may be done concurrently) and the other the output (the render-target with write-only access). After each pass, the role of these buffers are swapped. The technique is commonly mentioned as ping-pong. Algorithm 1 presents pseudo-code for a double buffered version of the recursive doubling algorithm, closer to a OpenGL/GPU implementation.
Even though widely used, the GPU recursive doubling algorithm can result work-inefficient. As, for large streams, there is a number of processors typically smaller than the stream size, the computation has to be serialized into batches. A key observation is that the recursive doubling algorithm does unnecessary computations at each element.

Sengupta et al. (Sengupta et al., 2006) noticed this fact and developed a work efficient prefix-sum algorithm for GPU implementation with work complexity of $O(s)$. Their algorithm uses a balanced tree approach adapted from the algorithm presented by Blelloch (Blelloch, 1990). An algorithm also with $O(s)$ work complexity, specially devoted to 2D data, has been independently developed by Greß et al. (Greß et al., 2006).

Blelloch proposes a two stage approach to compute an exclusive-prefix-sum using a binary tree structure. The first, the up-sweep, is a binary reduction. At each tree level, each node stores the sum of its children. Notice that for each subsequent level the number of active elements/processors is halved, leading to a total of $s - 1$ active processors. The second stage, referred as down-sweep, introduces the identity value (zero, for the addition) at the root node and then proceeds, level by level, updating the final result based on the partial results computed during the reduction step. Again, the number of active processors is $s - 1$, leading to an overall work complexity of $O(s)$. Although with better work efficiency, the number of passes in a typical GPU implementation requires twice the number of passes to complete, i.e. $2 \cdot \log_2(s)$, compared to the recursive doubling algorithm. Actually, the algorithm, as described, computes a exclusive prefix-sum. A final adjustment step is needed in order to compute the all-prefix-sum. This can be carried out by shifting all the elements one position to the left and placing the total sum at the rightmost element. Figure 3 visually illustrates the algorithm operation.

Sengupta et al. (Sengupta et al., 2006) observed that the balanced tree based algorithm has few active processors in passes / iterations that are close to the root and does more passes than the recursive doubling. The authors have proposed an hybrid algorithm that switches from the balanced tree into a recursive doubling approach when the number of active processors falls under the degree of parallelism (the maximum number of available parallel processors).

### 3.2 Segmented Prefix-Sum

The underlying strategy of segmented all-prefix-sum is a divide-to-conquer approach. A stream of elements can be partitioned into contiguous substreams that switches from the balanced tree into a recursive doubling approach when the number of active processors falls under the degree of parallelism (the maximum number of available parallel processors).

### 3.3 Stream Compaction

Stream compaction is an operator that takes a data stream as input, uses a discriminator to select a valid subset of elements, and outputs a compacted stream of the selected elements, discarding the rest. Sequential stream reduction is trivially implemented in $O(s)$
with a single pass over the data.

Parallel stream compaction is an important operation for several applications. Examples in the graphics domain that benefit from stream compaction include collision detection (Greß et al., 2006), ray-tracing (Roger et al., 2007), shadow mapping (Lefohn et al., 2007), point-list generation (Ziegler et al., 2006) and, in general, all algorithms that make use of data partitioning.

While seeming an inherently sequential computation, stream compaction can be parallelized using the all-prefix-sum. The fundamental idea is to discriminate data using a value of one to mark invalid elements and zero to mark valid elements. Then, the all-prefix-sum of this discriminated stream is computed. The resulting stream stores, for each position, the number of invalid elements to the left. This value corresponds to the displacement to the left that each valid element has to undertake in order to build the compacted stream (see Figure 5).

![Figure 5: Compaction of a stream based on the all-prefix-sum.](image)

For parallel architectures with scattering abilities, the compaction process could be implemented in a single pass, writing the valid elements to their final positions using the displacements available from the all-prefix-sum (Sengupta et al., 2007). As noticed, scattering is not available at the fragment processor. Consequently, scatter has to be converted to gather through vertex texture fetching (VTF), additional passes or search (Harris, 2005; Horn, 2005).

A straightforward solution to parallel compaction might also make use of GPU based sorting. Although, GPU-sorting solutions are typically based on sorting networks and variations of bitonic search yielding to an overall computational complexity of \(O(\log^2(s))\) (refer to Owens et al., 2007) for a comprehensive survey on GPGPU). Horn (Horn, 2005) noticed this and proposed an improved algorithm from stream compaction. His algorithm improves the overall complexity by a factor of \(\log(s)\) yielding to an overall complexity of \(O(\log(s))\). The solution is based on the observation that the all-prefix-sum \(pSum[\ ]\) is an ascending sorted stream and, as a result, a search can be conducted on the all-prefix-sum stream, in order to find the positions corresponding to the elements that will comprise the output compacted stream. The fundamental idea is to conduct, in parallel, a binary search, for all the first \(c\) indexes (where \(c \leq v\), with \(v\) denoting for the number of valid elements), in order to find an index \(f\) that satisfies \(f = c + pSum[f]\) and for which the original data stream has a valid element (Horn, 2005). The solution avoids the need of scattering, which is converted to gathering through search, with a computational complexity of order \(O(\log(s))\) and total work of order \(O(s \cdot \log(s))\).

### 3.4 Block Stream Compaction

Similarly to segmented prefix-sum, a divide to conquer strategy can be applied to compaction, as the hierarchical compaction scheme proposed by Roger et al. (Roger et al., 2007) (Figure 6). The stream can be segmented in blocks, the compaction process is done for each block, and then a second-level process recomputes an overall compacted stream based on the inter-segment all-prefix-sums. As, subsequently to the inner block compaction, the valid elements are contiguously stored, the inter-block prefix-sum gives the displacement to apply to each compacted substream. The concept is easily extended to a hierarchical process, and any prefix-sum or compaction algorithm may apply.

![Figure 6: The block based compaction approach (after Roger et al., 2007).](image)

As large streams are mapped into 2D textures, an immediate benefit from the block based compaction arises from avoiding massive 1D \(\rightarrow\) 2D coordinate conversions. A line by line, or segment by segment computation avoids these conversions, but a final step must be attained in order to concatenate the compacted parts of the blocks into a global compacted stream. As all elements of each compacted block must displace the same amount to the left, texture mapping can be used, with expected linear work, to attain such goal without the need for a scatter to gather conversion.
4 JUMPING JACK ALGORITHM

This section introduces an original algorithm for non-monotonic compression, i.e. the relative order of the valid elements is not preserved on the output. The algorithm was named Jumping Jack after observing the pattern of the search process that seems to consecutively jump forwards and backwards on the stream (Figure 7).

Although its simplicity, it has very interesting properties alongside with some limitations. We will discuss how these limitations can be mitigated leading to a suitable implementation on the GPU, turning it competitive or faster than existing stream compaction algorithms.

For a stream with size \( s \) with \( v \) valid elements, the idea is to keep the valid elements positioned within the first \( v \) indexes and fill the remaining positions (holes) by finding valid elements in the rest of the stream.

For each stream element, the all-prefix-sum has the ability to communicate some information about the past elements (e.g. number of non valid elements to the left). Thus, for each position, given the known non-valid elements to the left, one can compute the potential maximum size of the compacted stream (this number can also be interpreted as the first index that undoubtedly will not be part of the compacted stream). We refer this index as the max-allowable-size (MAS). MAS is easily evaluated as the difference of the stream size by the all-prefix-sum (Equation 1). Computation of the MAS stream can be done explicitly by a straightforward adaptation of the the all-prefix-sum computation, or embedded in the algorithm.

\[
\text{MAS}[i] = s - \text{pSum}[i];
\]

The search proceeds as follows. For a given index \( i \) within the first \( v \) positions, if the original data is valid, then the corresponding value is copied to the final stream. Otherwise, the algorithm uses the MAS value at position \( i \) and jumps to the corresponding index. This will be the first index where valid elements may be found. The process is then repeated until a valid element is found. The pseudo-code for the algorithm is given in Algorithm 2.

Applied to each position, the algorithm has the ability to find all the remaining valid elements (i.e. there is a one-to-one mapping between the first \( v \) positions and the positions of the valid elements).

To enable a better understanding of the algorithm, a visual trace of its operation for a stream with 6 valid elements in a total of 16 is depicted in Figure 7. As it can be observed, there are three valid elements within

![Algorithm 2: Jumping Jack (no order preserving).](image)

The fundamental property of this algorithm is that, for any given position, it will find a different valid element. Other very interesting property is that the parallel work (the sum of the work carried out by all processors) is linear and upper bounded by \( s-v \) search steps.

Nevertheless, for very sparse data, this work can be imbalanced, i.e. for some positions, finding a valid element will take much more work than others. The worst case happens when a unique valid element exists, and it is positioned in the middle of the stream. In such case, \( s-1 \) search steps will be needed to find it.
Theoretically, and if an arbitrary large number of processors is available, the algorithm is inefficient, as the overall computation only completes as the last parallel processor finishes its operation. Therefore, in the worst case, the parallel cost will be of quadratic order. This constitutes the algorithm major weakness.

In practice, there is not an unlimited number of fragment processors on the GPU. Therefore, the compaction of large streams has to be serialized into batches to the available processors mitigating the possibly imbalanced behavior of the algorithm.

To further limit the influence of this undesirable property, we make use of a segmented compaction strategy in order to bound the maximum number of iterations that may be performed by each element (by reducing the size of the individual streams to compact, as described in Section 3.4).

From the above discussion one can expect that, for not very sparse data distributions, the algorithm can be very fast in finding the unpositioned valid elements.

5 IMPLEMENTATION

Implementation was done using OpenGL 2.0, making use of FBOs (frame buffer objects) with single component 32-bit float texture formats for the input and output data, as well as, for intermediary memory buffers. Four component (RGBA) 32-bit float formats were used for the described block compaction mechanism. The presented results were taken using a nVidia GeForce 7300 Go (G72M) GPU. Fragment programs were coded using the Cg Language, but are straightforwardly convertible to GLSL. All timings were taken at GPU side using the query mechanism provided by the OpenGL GL_EXT_timer_query extension.

The Jumping Jack Algorithm (Section 4) was implemented to be used by a block based compaction mechanism (Section 3.4). For the MAS computation we implemented both the recursive doubling (Hillis and Steele JR, 1986) and balanced tree (Blelloch, 1990) algorithms (Section 3.1).

We adopted (Roger et al., 2007) ideas to implement the block based compaction mechanism. The process is depicted by Figure 8 and comprises three stages.

The first two stages are straightforward. The second stage can use any compaction algorithm. We only notice that the number of invalid elements per block must be provided as a result from the second stage (e.g. the value of the all-prefix-sum at the last block element). We will now detail on the third stage which is more elaborated.

Given the number of invalid elements per block, the displacements, for each of the block compacted substreams, can be computed using an inter-block all-prefix-sum. These displacements have to be converted from 1D coordinates to 2D coordinates from which the \((x,y)\) coordinates for the two endpoints of each block are obtained. As it is shown (Figure 8, block B4) there are compacted blocks that may wrap between consecutive lines in the result. Notice that these have not to be split in more than two parts (as the block size is less or equal than the line width). To simplify, we assumed that all compacted blocks wrap and actually we compute four endpoints corresponding to the start and end positions of the first section and the (potential) second section. Texture coordinates are assigned to each endpoint in accordance with the compacted substream position.

These values are intended to be used by the geometry engine. This is actually implemented using a Render to Vertex Array (RTVA) technique, but other options exist as outlined later in the text. As the number of lines to be rendered is a priori known (twice the number of blocks) we devised to use the fragment processor to compute and pack the four endpoints and texture coordinates into two RGBA textures, each having twice the number of elements as the number of blocks. One of these textures packs the endpoints and textures coordinates for the first (mandatory non wrapping section) line segment and the other those corresponding to the second (potentially wrapping section) line segment. These textures are then used as input data for the geometry engine, in order to create the texturized lines, forwarding them to the subsequent graphics pipeline. The graphics hardware clips the lines, generates the fragments with interpolated texture coordinates, and eventually render them. As a result, the overall compacted stream is obtained.

Figure 8: Block Based Compaction implementation.
True direct RTVA is not directly supported by OpenGL but it can be achieved using buffer objects. As in OpenGL these buffer objects are not unified, the solution comprises rendering into a framebuffer object (FBO), then copying the data into a pixel-buffer object (PBO) and re-casting it as a vertex buffer object (VBO). The VBO is then used as geometry input by an OpenGL call. Copying from the FBO into a PBO does not involve transfers from GPU to CPU or vice-versa as it is performed internally and therefore can be very fast due to the high memory bandwidth of internal GPU memory.

Other approaches exist as fetching the texture directly from the vertex processor (VTF), or from the geometry processor when available (e.g. as suggested by (Roger et al., 2007)). The latter should enable a theoretical more optimized process of the wrapping problem, as the geometry processor has the ability to generate geometry in a data dependent manner, therefore enabling the creation of the second line segment only when necessary.

6 RESULTS

The intra-block all-prefix-sum computation has no data dependencies, however it depends on the block size. We implemented both the double recursive and the balanced tree approaches. The achieved results for a 4M element stream (we will use the M prefix to denote for $\times 2^{20}$) are depicted in Figure 9. Results demonstrate the block-size dependency but the algorithms show opposite behaviors. The recursive doubling algorithm is more efficient for small block sizes, whereas the balanced tree becomes more efficient as the block size increases. As a result, the choice for one algorithm may have consequences on the overall performance, if not tuned as a function of the block size.

To have a better insight on how the concatenation varies with the block size, we measured the concatenation times for several block sizes. We used a data set with 50% of invalid elements. Notice that only the block level compaction component is affected by the data distribution. Figure 10 presents average timings to concatenate a 4M stream for block sizes ranging between 16 and 2048. As expected, the inter-block sum is faster for greater block sizes. The block-level compaction is also faster for greater block sizes, however it appears to revert this behavior for block sizes above 1024.

We also observed experimentally, as it was expectable, that the concatenation process depends on the number of valid elements. Notice that the work carried out by the inter-block all-prefix-sum depends on the number of blocks. Consequently, this data dependent variation has more impact for large block sizes, as the all-prefix-sum is faster (reduced number of blocks) and the number of textured lines is smaller (less effort by the geometry engine), but the number of valid elements to render increases (stressing the rasterizer and texturing units).

We proceed by analyzing the results achieved by the Jumping Jack Algorithm and compare them with those achieved by the binary search proposed by Horn (Horn, 2005). The results herein presented make use of the block compaction approach. Figure 11 presents the timings achieved to compact a 4M element stream against the density of invalid elements (randomly generated). A block size of 256 was used. Presented time values correspond to the overall stream compaction process.

Jumping Jack Algorithm has a stable performance under densities of 95%, with timings increasing almost linearly as the density increases. Above 95%, there is a significative drop in performance. Notice that jumping Jack, theoretically, performs the search process for the number of unpositioned valid elements. As the invalid densities increases, the probability of unpositioned elements also increases. On the other hand, as the invalid densities increase, it also
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![Graph](image1.png)

Figure 11: Overall time spent for compaction of a 4M stream by the two tested algorithms, versus the invalid elements density. A block size of 256 was used.

Increases the probability of having imbalanced work with some elements doing longer searches than others. This factor is very noticeable for high densities of invalid elements.

Horn’s algorithm has a theoretical search complexity, per valid element, that increases with the number of invalid elements by a factor $\log_2(s-v)$. As the number of invalid elements increases, the search complexity increases logarithmically, but the search is conducted for less elements. The timings until densities of 20% are dominated by the logarithmic factor, being then dominated by the number of valid elements, with timings decreasing as the percentage of invalids increases.

It can be observed that Jumping Jack algorithm performs faster than Horn’s for densities under 78%, demonstrating the practical utility of the algorithm, when monotonicity is not a requirement, and specifically when very sparse data is not expectable.

Next, we present the results for the inter-block compaction process using several block sizes. We have tested the compaction in two architectures to conclude about the scalability of the proposed algorithm. Figure 12 shows the achieved timings for the tested GPU nVidia Go 7300 (3 vertex processors, 4 fragment processors), and Figure 13 for a more recent nVidia GeForce 9500 M GS (NB8P) GPU (with 32 unified processors).

The achieved results demonstrate that Jumping Jack globally maintains its behavior, being faster than Horn for densities under 70%. A relevant observation is that, for very sparse data, the Jumping Jack algorithm performs comparatively better with the more recent GPU. In such circumstances, it can be observed a lesser noticeable drop in performance. This is an expected result, as the more recent GPU has a better branch granularity and better loop support.

We observed that speedups ranging between $5 \times$ and $8 \times$ were achieved, depending on the algorithm, block size and data density. A direct comparison cannot be easily made as there is no control over the assignment of unified processors to each pipeline stage. Another important observation is that, for the more recent GPU, the algorithms tend to perform better with smaller block sizes, whereas the older GPU has an opposite behavior. Thus, the underlying GPU architecture clearly influences the algorithms performance.

7 CONCLUSIONS AND FUTURE WORK

This paper introduces Jumping Jack, an original algorithm for non-monotonic stream compaction. To take full advantage of it, a block based compaction scheme is proposed. The algorithm is very simple to implement and has interesting computational complexity properties. A major weakness of the algorithm rests in its imbalanced behavior, which is more notably revealed in presence of very sparse data.

The achieved results demonstrate the practical usefulness of our proposal, for which we pointed out the advantages and limitations compared to prior work. We devised strategies and implementation notes on how to make it useful and demonstrated that
the algorithm can perform considerably faster than existent algorithms.

Our implementations have room to be further optimized, as they served fundamentally as a proof of concept. We plan to continue testing the algorithms in a broader range of hardware platforms and diversified data sets, expecting further insights that can lead to improved variations and ideas. Another avenue to future work is to study how these algorithms and concepts adapt to the forthcoming (and expectably more flexible) architectures and standards.

A major conclusion is that performance of compaction algorithms may have large data and architectural (inter)dependencies. Tuning an optimal solution, if possible, is therefore a complex task which is likely to rely on several variables.

Aware of this, and as a future work avenue, we are devising solutions that have the ability to adaptively self-tune in order to achieve a better performance. This goal is likely to encompass several approaches, as for instance, developing new algorithms, hybrid algorithms (retaining the best properties of each component), and by the use of a generic optimization framework, as outlined in (Moreira et al., 2006), to enable a dynamic optimization of the compaction process.

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