NEW ALGORITHMS FOR GPU STREAM COMPACTION  
A Comparative Study

Pedro Miguel Moreira¹,², Luís Paulo Reis²,³ and A. Augusto de Sousa²,⁴
¹ESTG-IPVC, Instituto Politécnico de Viana do Castelo, Viana do Castelo, Portugal
²DEI/FEUP, Faculdade de Engenharia da Universidade do Porto, Porto, Portugal
³LIACC, Laboratório de Inteligência Artificial e Ciência de Computadores, Porto, Portugal
⁴INESC-Porto, Instituto de Engenharia de Sistemas e Computadores do Porto, Portugal

Keywords: Stream Compaction, Parallel Algorithms, Parallel Processing, Graphics Hardware.

Abstract: With the advent of GPU programmability, many applications have transferred computational intensive tasks into it. Some of them compute intermediate data comprised by a mixture of relevant and irrelevant elements in respect to further processing tasks. Hence, the ability to discard irrelevant data and preserve the relevant portion is a desired feature, with benefits on further computational effort, memory and communication bandwidth. Parallel stream compaction is an operation that, given a discriminator, is able to output the valid elements discarding the rest. In this paper we contribute two original algorithms for parallel stream compaction on the GPU. We tested and compared our proposals with state-of-art algorithms against different data-sets. Results demonstrate that our proposals can outperform prior algorithms. Result analysis also demonstrate that there is not a best algorithm for all data distributions and that such optimal setting is difficult to be achieved without prior knowledge of the data characteristics.

1 INTRODUCTION

Graphics Processing Units (GPUs) are parallel platforms which provide high computational power with very large memory bandwidth at low cost. With the advent of GPU’s programmability, many algorithms, that usually were performed by the CPU, were enabled to run at the GPU side taking advantage from its parallel processing capabilities. Nowadays, GPUs are compelling programmable platforms, not only under the graphics domain, but also for general purpose computational intensive tasks, leading to a relatively new research area focused on mapping general purpose computation to graphics processing units - GPGPU (Owens et al., 2007; GPGPU, 2008).

Stream compaction, also designated as stream non-uniform reduction and also as stream filtering, takes a data stream as input, uses a discriminator to select a wanted subset of elements, and outputs a compacted stream of the selected elements, discarding the rest.

Several computer graphics applications, making use of the GPU programmable architecture, may take advantage from parallel stream compaction algorithms in several ways. Key benefits, enabled by exclusion of non-relevant data, comprise: savings on computational effort on further processing stages; better memory footprint; and savings on bandwidth when data has to be readback to the CPU. Stream compaction is also a fundamental component on algorithms that deal with data partitioning (e.g. some sorting algorithms and space hierarchies). Reported work taking advantage from GPU stream compaction include: collision detection (Horn, 2005; Greß et al., 2006), ray-tracing (Roger et al., 2007), shadow mapping (Lefohn et al., 2007), point list generation (Ziegler et al., 2006), and, in general, algorithms that make use of data partitioning.

The current OpenGL specification (OpenGL v.2.1) (Segal and Akeley, 2006) exposes two GPU programmable units: the vertex and the fragment processors. A third programmable unit, the geometry processor, was recently exposed through OpenGL extensions (OpenGL Architecture Review Board, 2008) but it has limited support and availability only on very recent GPUs. Current GPUs are designed with several vertex and fragment processor units enabling them with high levels of parallelism.

The vertex processor has scatter capabilities (indirect writing) and also gather capabilities (indirect reading) with the latter with some lack of support and performance issues. The fragment processor has only gather capabilities, through texture fetching.

More recently, the so-called Unified Architec-
turers (UA), were made available. The UA paradigm comprises indistinct processors and features such as global load-store memory, shared memory, and synchronization mechanisms. However, these features have restricted support as they are not currently exposed to programmers but by proprietary APIs.

This paper presents original work on parallel stream compaction algorithms for programmable GPUs and compares them to state-of-the-art algorithms. The algorithms are intended to be implemented using widely supported features, such as the exposed by OpenGL (Segal and Akeley, 2006; Kessenich, 2006). We assume that the GPU has programmable vertex processors with scatter and (potentially limited) gather abilities and programmable fragment processors with gather abilities but without scatter.

The rest of the paper is organized as follows. The next section reviews relevant prior work on scan primitives and stream compaction. Following (Section 3) introduces the original algorithms alongside with a more detailed description of the tested algorithms. The implementation and experimental setup are described alongside with the achieved results in Section 4. At last, Section 5, outlines our major conclusions alongside with possible directions to future work.

2 RELATED WORK

Stream compaction is an operator that takes a data stream as input, uses a discriminator to select a valid subset of elements, and outputs a compacted stream of the selected elements, discarding the rest. Sequential stream compaction is trivially implemented in $O(s)$ with a single pass over the data.

While seeming an inherently sequential computation, stream compaction can be parallelized using the all-prefix-sum (aka scan). The all-prefix-sum operation (Blelloch, 1990) takes a binary associative operator $\oplus$ and an ordered set of elements with size $s$ (e.g. an array or stream): $[a_0, a_1, \ldots, a_{s-1}]$; and returns an ordered set: $[a_0, (a_0 \oplus a_1), \ldots, (a_0 \oplus a_1 \oplus \cdots \oplus a_{s-1})]$.

The parallel prefix-sum can be computed using a recursive doubling algorithm, as described by Hillis & Steele (Hillis and Steele JR, 1986) and used by Horn (Horn, 2005) in a GPU implementation. The recursive doubling has a total work of $O(s \cdot \log(s))$. Hensley et al. (Hensley et al., 2005) also used the recursive doubling algorithm to devise fast GPU generation of Summed Area Tables (Crow, 1984) which can be thought as a 2D prefix-sum.

Sengupta et al. (Sengupta et al., 2006) implemented a prefix-sum based on a balanced tree approach, as described by Blelloch (Blelloch, 1990), with a computational complexity of $O(s)$. They also proposed a GPU work-efficient algorithm that switches between the recursive doubling and balanced tree based algorithms, in order to optimize the work amongst the available parallel processors. More recently, their approach was improved (Harris et al., 2007) by making use of an optimized segmented prefix-sum approach targeted to the new NVIDIA CUDA API (Nickolls et al., 2008). By the same time, Greß et al. (Greß et al., 2006) also devised a GPU implementation with $O(s)$ running time targeted to 2D data and making use of a quadtree data structure.

The fundamental idea to achieve parallel compaction using the all-prefix-sum is to discriminate the data using a value of one to mark invalid elements and zero to mark valid elements. Then, the algorithm proceeds by computing the all-prefix-sum of the discriminated data. The resulting stream stores, for each position, the number of invalid elements to the left. This value corresponds to the displacement to the left that each valid element has to undertake in order to build the compacted stream (see Figure 1).

If scatter capabilities are available, the compaction process can be implemented in a single pass. As scatter is not widely available at the fragmenting processing level, it has to be converted into gather. Horn (Horn, 2005) devised a binary search mechanism in order to enable stream compaction under such circumstances.

Roger et al (Roger et al., 2007) described a hierarchical stream compaction strategy that splits the data into regular blocks, compacts them and finally concatenates the compacted substreams. A higher level prefix-sum is used to compute the displacements of each compacted block. They suggest making use of the scatter abilities of the geometry processors (or alternatively the vertex processor), to avoid a block-level gather-search and, therefore, enabling savings on the total parallel work.

Ziegler et al. (Ziegler et al., 2006) introduced the Histo-Pyramids algorithm, devoted to 2D data which, which similarly to the work of Greß et al. (Greß et al., 2006), uses a quadtree to encode the valid elements.
and then extracts them into a compacted stream (actually a 2D texture) by means of a guided tree traversal. This approach avoids the explicit computation of the all-prefix-sum for all elements. Though not changing the asymptotical complexity of prior algorithms, the algorithm effectively reduces the total work, as there are, in parallel, a number of tree traversals that equals the number of valid elements.

In the following section we will introduce a new algorithm (Section 3.3), the Run-Lengths of Zeros (RLZ), that operates on an alternative domain than the all-prefix-sum. We also describe the Binary-Tree algorithm (Section 3.4) supported on ideas originally described by Greß (Greß et al., 2006) and Ziegler (Ziegler et al., 2006).

We tested these algorithms together with the Jumping Jack algorithm (Section 3.2) devised by (Moreira et al., 2009) and with (Horn, 2005) gather-search algorithm (Section 3.1). In order to efficiently handling large data streams, we adopted a block based compaction framework, as introduced by (Roger et al., 2007), and described in (Moreira et al., 2009). For the parallel all-prefix-sum, we have implemented the recursive doubling all-prefix-sum (Hillis and Steele JR, 1986), (Horn, 2005)) and the balanced tree approach ((Blelloch, 1990; Sengupta et al., 2006)).

3 ALGORITHMS

This section introduces original work and also describes current state-of-the-art algorithms for stream compaction.

3.1 Gather-Search (Horn, 2005)

Daniel Horn (Horn, 2005) introduced a compaction algorithm based on a binary-search procedure allowing conversion of scatter into gather. Horn observed that the all-prefix-sum is an ascending stream and therefore a parallel search can be conducted in order to find the data elements that have to displace to each position in order to create the compacted stream. The original algorithm computes the all-prefix-sum based on the recursive doubling algorithm proposed by Hillis & Steele (Hillis and Steele JR, 1986), but any other method can be used.

Given a stream $data[i]$ with size $s$, and its corresponding all-prefix-sum $pSum[i]$ of invalid elements, with a total number of $z$ invalid elements ($z = pSum[s - 1]$) and $v = s - z$ valid elements, a binary search is conducted in parallel for all output positions $c \in [0, v]$. The search goal is to find a valid element displaced $d$ positions to the right from the current position $c$, such as $pSum[c + d] = d$ (refer to 1). The possible displacements can take values on the range $d \in [0, z]$. The binary search proceeds until $d = pSum[c + d]$ is satisfied and $data[c + d]$ is a valid element. The search solution has a computational complexity of order $O(log(s))$ and total work of order $O(s \cdot log(s))$.

3.2 Jumping-Jack (Moreira et al., 2009)

Jumping Jack was recently introduced by Moreira et al. (Moreira et al., 2009) as a non-monotonic compaction algorithm. Non-monotonic compaction does not preserve the relative order of the original data at the output. Monotonicity is not a requirement for many applications.

The algorithm is very simple to implement, and is specifically devoted to not very sparse data sets. For very sparse streams the algorithm has a drop in performance due to its imbalanced behavior. Therefore, in order to handle large amounts of data, and to bound the effect of the potential load imbalance, the algorithm is proposed to operate over small-sized streams, under a hierarchical compaction scheme (e.g. as introduced by (Roger et al., 2007)).

For a stream with size $s$ with $v$ valid elements, the main idea is to keep unchanged all the valid elements positioned within the first $v$ indexes, and fill the other positions, originally occupied by invalid elements, by finding the remaining valid elements. This can be achieved by conducting a search on the named MAS (maximum-allowable-size stream) which can be computed straightforwardly from the all-prefix-sum as $MAS[i] = s - pSum[i]$. The search is conducted using the MAS as pointer stream and recurrently inspect the data at the pointed position until a valid element is found. The algorithm has a total linear work of $O(s)$ and the total work is bounded by $O(s \cdot v)$.

3.3 Run-Lengths of Zeros - RLZ

The design of the herein presented algorithm was based on the observation that in the algorithm proposed by (Horn, 2005) (Section 3.1), and when in presence of large runs of invalid elements, the displacement criterion is valid for the desired valid element and for all the subsequent sequence of invalids. Notice that the valid element is always positioned just before (to the left) the sequence of invalid elements. In such situation, the binary search process has often to iterate (to lower indexes) until the desired element is found.
The main idea was to use an alternative search domain, than the regular all-prefix-sum of invalid elements, that better captures the structure of the data. We have designed the algorithm to operate on the all-prefix-sum of the run-lengths (denoted from now as \( pRLSum \)) of invalid sequences. This sequence is constructed by summing the lengths of the runs of invalid elements. The run-lengths are positioned at the start position of each run (from left to right). Figure 3 visually illustrates the concept, which will be detailed in the next subsection. We will subsequently refer this algorithm as Run-Lengths of Zeros, or RLZ for short.

The \( pRLSum \) stream has interesting properties when compared to the regular all-prefix-sum stream. The streams have value correspondence for valid elements and the number of invalid elements can be found at the last position. Distinctively, the \( pRLSum \) only retains the interesting values, i.e. is composed by the displacements values (until the last valid element).

We used these properties to devise a search to find the desired displacements, in order to obtain a compacted stream. We observed empirically that these displacements can be quickly found using a recursive forward search approach. Particularly, this forward search is very quick for the first elements and for moderate sized streams (e.g. in the order of hundreds or thousands of elements).

The search is quite simple and proceeds as follows (Algorithm 1). For a given index \( i \) of the output stream, one has to find the first displaement such: \( \text{displacement} = pRLSum[i + \text{displacement}] \). Actually we observed that evaluating the condition \( pRLSum[i + \text{displacement}] = pRLSum[i + pRLSum[i + \text{displacement}]] \) results more optimized and performs about 20\% faster.

Algorithm 1: Compaction using Run-Lengths of Zeros.

```python
begin
  forall positions \( i \in [0, v] \) in parallel do
    curr ← \( pRLSum[i] \)
    next ← \( pRLSum[i + curr] \)
    while curr ≠ next do
      curr ← \( pRLSum[i + next] \)
      next ← \( pRLSum[i + curr] \)
    compact[i] ← data[i + curr]
  end
end
```

Computing the \( pRLSum \) is costlier than computing the all-prefix-sum. Although, it is expected a faster search process resulting in an overall performance competitive with prior algorithms. It is also expected that the algorithm performs better for data with low frequency of change between valid and invalid elements, i.e. with medium to large sized runs of valid / invalid elements.

3.3.1 Computing Run-Lengths

We devised a three stage parallel algorithm for computing the all-prefix-sum of run-lengths. The overall process is illustrated in Figure 3.

![Graphical trace of the Run-Lengths of Zeros algorithm.](image)

![Computation of the all-prefix-sum of run-lengths, \( pRLsum \).](image)

The first stage Run-Length Computation computes, for each invalid element (marked as one), the number of consecutive invalid records, to the right, until a valid element is reached (or the end of the stream). This value might be interpreted as the distance to the next valid element and the problem can be thought as list-ranking within a list of lists. Positions corresponding to valid elements store a zero. Notice that the run-length of invalid elements is stored at the leftmost position of the sequence.

For this stage, we developed a variation of the recursive doubling algorithm to enable finding the run-lengths. The algorithm is similar, except that it operates in reverse direction and the addition is conditioned by the value of the current position. The explanation is as follows. A given position stores a value corresponding to the number of consecutive elements from its own position to offset positions to the

---

**Stage 1: Run Length Computation**

**Stage 2: Run-Length Extraction**

**Stage 3: All Prefix Sum**
right. Accordingly, if this value is below the current offset, the sequence is doubtlessly interrupted somewhere within that range. Hence, for each iteration, the value stored offset positions away is added to the current position, if and only if, the value in the current position equals the offset. Pseudo-code for the algorithm is given in Algorithm 2 and a visual trace is illustrated by Figure 4. The algorithm has a parallel computational complexity of $O(\log_2(s))$ with total work of $O(s \cdot \log_2 s)$.

**Algorithm 2**: Parallel run-length computation (based on recursive doubling).

```plaintext
begin
  output: RL[] : the output stream, initialized with the discriminated data
  for $p \leftarrow 1$ to $\log_2(s)$ do
    offset = $2^{p-1}$
    forall $i < s - offset$ in parallel do
      if $RL[i] = offset$ then
        $RL[i] \leftarrow RL[i] + RL[i+offset]
      end
  end
end
```

![Figure 4: Illustration of the modified recursive doubling algorithm to compute run-lengths of consecutive elements.](image)

In order achieve the run-lengths computation with a total work of order $O(s)$, we have also developed a variation to the all-prefix-sum algorithm proposed by Blelloch (Blelloch, 1990). A visual illustration of the overall algorithm operation is depicted in Figure 5. The process comprises two fundamental steps. The first, referred as the up-sweep (Algorithm 3), performs as a conditioned binary reduction. For each level, each node takes the value stored in its left child. The value stored in its right child is added, if and only if, the left child corresponds to a full node (i.e. all leaves under it are ones). Therefore, each node will store the length of the sequence (run of ones) starting at the leftmost leaf of the corresponding subtree (e.g. the root node stores the length of the run starting at the first stream element). The second step, referred as down-sweep (Algorithm 4), uses the values from the up-sweep to hierarchically build the run-lengths stream. The fundamental idea is to check if the runs extend across subtrees and update the run-lengths accordingly. The root node is initialized with the identity value (zero). At each subsequent level, each right child takes the value stored by its parent. Each left child takes the value, computed in the up-sweep phase, of its right sibling. If the sibling node corresponds to a full node, then it also adds the value stored by its parent. A final adjustment step shifts the values one position to the right and adds to the leftmost element the leftmost element of the original discriminated stream, in order to obtain run-lengths at the desired positions (possibly embedded in the last level of the down-sweep). Notice that, as the given pseudo-code assumes a start index of zero, right and left child nodes correspond to odd and even indexes, respectively. A GPU implementation, making use of a double buffer (one to read and the other to write), and switching the buffer roles after each pass, allows to store alternate hierarchical levels of the up-sweep and down-sweep at each buffer.

**Algorithm 3**: Up-Sweep stage of run-length computation (based on balanced-tree).

```plaintext
begin
  input : US[0][ ] discriminated data
  output: US[ ][ ] all levels of the up-sweep
  for $p \leftarrow 1$ to $\log_2(s)$ do
    offset = $2^{p-1}$
    forall $i$ from $0$ to $\frac{s}{2^p} - 1$ in parallel do
      if $US[p-1][2i] = offset$ then
        $US[p][i] \leftarrow US[p-1][2i] + US[p-1][2i+1]
      else
        $US[p][i] \leftarrow US[p-1][2i]
      end
  end
end
```

The second stage comprises a fast (potentially embedded in the previous or the next stage) filtering stage designed to extract / filter the desired run-lengths. As it can be observed, these elements are all those that being non-null have a null element at his left.

The third stage computes the desired all-prefix-sum of the run lengths, e.g. using (Hillis and Steele JR, 1986) or (Blelloch, 1990) or any other method.

Computing the $pRLsum[ ]$ stream has the same order of computational complexity as the all-prefix-sum, but it doubles the passes over the data, doing nearly twice the work.
The design of the herein presented algorithm is founded on ideas originally described by (Greß et al., 2006) and by (Ziegler et al., 2006). The referred works are mainly devoted to compaction of 2D data (with potential extensions to 3D) and use a quadtree as the fundamental data structure. Despite the similarities, instead of a quadtree, our proposal uses a binary tree as a fundamental data structure, and so, it can be straightforwardly used to compact both linear and 2D data. Furthermore, we propose the combination of its operation with a block based compaction strategy.

The main idea behind the design of the algorithm is to avoid the prior computation of the all-prefix-sums. This can be achieved by encoding the data stream into a binary tree where each node stores the number of valid elements under it. Extraction of the compacted stream is achieved by tree traversal.

The first step of the algorithm is to discriminate the valid elements. In the following discussion it is assumed that valid elements are flagged as true (ones) and invalid elements are flagged as false (zeros).

The next step, binary tree encoding, comprises encoding the number of valid elements into a binary tree. This is similar to a stream reduction operation using addition as the reduction operator and preserving the intermediary results (i.e. preserving the overall reduction tree structure). At each level (pass), each node computes the number of valid elements under it, i.e. the sum of valid elements stored by its child nodes. This process continues until the root level is reached.

The root node stores the total number of valid elements, i.e. the size of the compacted stream, \( s \). This binary reduction is achieved in \( \log_2(s) \) passes, being \( s \) the size of the original stream. Notice that as for each pass (tree level) the number of nodes is halved, the total work has a linear order \( O(s) \), in respect to the stream size.

### 3.4 Binary-Tree

The design of the herein presented algorithm is founded on ideas originally described by (Greß et al., 2006) and by (Ziegler et al., 2006). The referred works are mainly devoted to compaction of 2D data (with potential extensions to 3D) and use a quadtree as the fundamental data structure. Despite the similarities, instead of a quadtree, our proposal uses a binary tree as a fundamental data structure, and so, it can be straightforwardly used to compact both linear and 2D data. Furthermore, we propose the combination of its operation with a block based compaction strategy.

The main idea behind the design of the algorithm is to avoid the prior computation of the all-prefix-sums. This can be achieved by encoding the data stream into a binary tree where each node stores the number of valid elements under it. Extraction of the compacted stream is achieved by tree traversal.

The first step of the algorithm is to discriminate the valid elements. In the following discussion it is assumed that valid elements are flagged as true (ones) and invalid elements are flagged as false (zeros).

The next step, binary tree encoding, comprises encoding the number of valid elements into a binary tree. This is similar to a stream reduction operation using addition as the reduction operator and preserving the intermediary results (i.e. preserving the overall reduction tree structure). At each level (pass), each node computes the number of valid elements under it, i.e. the sum of valid elements stored by its child nodes. This process continues until the root level is reached.

The root node stores the total number of valid elements, i.e. the size of the compacted stream, \( s \). This binary reduction is achieved in \( \log_2(s) \) passes, being \( s \) the size of the original stream. Notice that as for each pass (tree level) the number of nodes is halved, the total work has a linear order \( O(s) \), in respect to the stream size.

### Algorithm 4: Down Sweep stage of run-length computation (based on balanced tree).

```plaintext
begin
    input : US[i] all levels from the up-sweep
    output: DS[log_2(s)] run-lengths
    DS[0] = 0
    for p = log_2(s) - 1 downto 0 do
        offset = 2^p
        for all i from 0 to \( \frac{s}{2^p} - 1 \) in parallel do
            if isEven(i) then
                DS[p][i] = offset then
                    DS[p][i] = US[p][i] + DS[p + 1][2^p]
                else
                    DS[p][i] = US[p][i + 1]
                else
                    DS[p][i] = DS[p + 1][2^p]
            end
end
```

### Algorithm 5: Binary Tree Traversal (monotonic).

```plaintext
begin
    forall i < v do in parallel
        currnode = root
        minR = 0
        maxR = valueAt(root)
        while not isLeaf(currnode) do
            currnode = firstChild(currnode)
            maxR = minR + valueAt(currnode)
            if i \( \notin \) [minR, maxR] then
                currnode = nextSibling(currnode)
                minR = minR + valueAt(currnode)
            compact[i] = data[indexOf(currnode)]
        end
end
```

To extract the valid elements, a search traversal is conducted in the binary tree. This is done in parallel for a number \( v \) of valid elements found on the original stream. Each traversal takes as input the in-
New Algorithms for GPU Stream Compaction - A Comparative Study

dex (order) of a valid element. Based on the information stored by each tree node, the algorithm dynamically maintains the range of valid indexes under each node. This information is used to guide the tree traversal as follows. Beginning at the root node, and searching for the $i^{th}$ element, the range of valid indexes $[minR, maxR]$ is set to $[0, v]$. The traversal then makes a first-child move and updates this range by setting its bounds to $[minR, minR+n]$, being $n$ the number of valid elements under the current node. If $i$ is not within the range, the traversal moves to the next-sibling node and the valid range is updated to $[minR+n, maxR']$. This process is repeated until a leaf node is reached for which the valid range comprises the index of the sought element, i.e. $[i, i+1]$. The data is then copied from that position into the $i^{th}$ position of the compacted stream. Algorithm 5 presents the pseudo-code of this process. An example of its operation is depicted in Figure 6. The figure illustrates the search of the $5^{th}$ element of the stream ($i = 4$). The bounds of the valid index range are shown next to upper-left corner of each node. The path of the search is obtained by following the (red) arrows. At the illustrated example, the desired element is found at index 5 of the data stream which is copied to the corresponding position of the compacted stream (index $i = 4$).

![Figure 6: Graphical trace of the Binary Tree algorithm.](image)

Each search is independent and can be conducted in parallel. The complexity of the search equals the depth of the binary tree, i.e. $\log_2(s)$. Note that the search is only conducted for the $v$ valid elements, accounting a total number of search steps of $v \cdot \log(s)$.

4 RESULTS

All the described algorithms in Section 3 were implemented, tested and analyzed. A block based compaction mechanism, based on (Roger et al., 2007) and with implementation details described by (Moreira et al., 2009), was used in order to allow efficient handling of large data streams.

Implementation was done under OpenGL 2.0, making use of frame buffer objects (FBO) with single component 32-bit float texture formats for the input and output data and, as well, for intermediary memory buffers. Four component (RGBA) 32-bit float formats were used for the described block compaction mechanism. The presented results were taken using a nVidia GeForce 7300 Go (G72M) GPU. Fragment programs were coded using the Cg language (Fernando and Kilgard, 2003), but are straightforwardly convertible to the OpenGL Shading Language (Kessenich, 2006). All timings were taken the OpenGL GL_EXT_timer_query extension.

We implemented and measured the time to perform the all-prefix-sums using the algorithms described by (Hillis and Steele JR, 1986) and (Blelloch, 1990) and verified that, for block sizes under 128, the recursive doubling approach performs faster than the balanced tree. For larger block sizes, the balanced tree performs faster.

As the prefix sum is being done in relatively small substrings, the overall timings are directly proportional to the data-set. For instance, we verified that for streams with 1M elements (we use the M and K suffixes to denote stream sizes orders of $\times 2^{20}$ and $\times 2^{10}$, respectively) and 256K elements ($512 \times 512$) the overall timings were for all methods 1/4 and 1/16 with a deviation not greater than 5%.

To enable a better understanding of the relative weight of each step comprised by the compaction algorithms, times were taken separately as depicted in Figure 7. The presented results were taken for a 4M stream ($2048 \times 2048$) using a block size of 256. Results demonstrate that the binary search process of Horn’s algorithm dominates the overall process. The weight of the search is larger for dense (low percentage of invalids) data. For sparser data, the relative weight of the search tends to be smaller. Jumping Jack (JJ) spends the same amount of time on the prefix-sums, but performs faster for dense data, outperforming Horn’s algorithm in such circumstances. RLZ spends twice the time on the prefix-sum, but its faster search leads to outperform Horn’s algorithm for dense data and to be competitive for sparse data. Finally, the Binary Tree (BT) has a very fast first stage (reduction). The extraction (search) process depends on the tree depth and on the number of valid elements and has a worse performance than JJ and RLZ algorithms for dense data. However, due to the quicker first step, the BT algorithm is able to outperform all the other, particularly from mid to high data sparseness. We no-
noticed that the concatenation step is comparatively very fast, except for very small block sizes where the large number of blocks leads to increased effort on the computation of the inter-block prefix sum and on the line rendering mechanism. As it can be observed, the concatenation also depends on the data distribution, but for the used block size this has no significant impact on the overall performance.

Figure 7: Times (in milliseconds) needed to perform the several stages of compaction with three different data densities, using the four tested algorithms. Stream and block sizes were 4M and 256, respectively.

Experiments using different block sizes were conducted with results reported in Figures 8 to 10. A first conclusion is that algorithms behave distinctively for different block sizes. For dense data, Horn’s algorithm takes advantage by using smaller blocks. On the contrary, when operating with sparse data, it performs faster using a larger block size. This is also the case of the BT algorithm. The JJ and RLZ algorithms have a more regular behavior, taking benefits, in general, from adoption of a larger block size.

Jumping Jack algorithm can be very fast for mid to low data densities, performing better than Horn’s for densities of invalid elements below densities of 70% to 80%, depending on the block size. RLZ presents a competitive behavior, particularly for large block sizes. Results analysis also exposes an interesting characteristic of RLZ as it exhibits the less data dependent behavior, being the more stable algorithm, with less performance variance for the different data densities. Such characteristic can be of importance if, for instance, in the context of an interactive application, a sustained and predictable frame-rate is desired. The Binary Tree Algorithm is generally the best and, particularly for sparse data, it outperforms all the others, independently of the block size, exception made to very dense data. However, different block sizes has to be chosen a priori, depending on the data density, in order to obtain an optimal setting. In practical settings these knowledge may not be available in order to optimally tune the compaction parameters.

To enable a better perception of the data distri-
NEW ALGORITHMS FOR GPU STREAM COMPACTION - A Comparative Study

Table 1: Time (in milliseconds) achieved for compaction of the image data set. The $i_-$ prefix denotes the negative version.

<table>
<thead>
<tr>
<th>block Algorithm</th>
<th>Hand</th>
<th>256K</th>
<th>1M</th>
<th>4M</th>
<th>Finger</th>
<th>256K</th>
<th>1M</th>
<th>4M</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>5</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mem</td>
<td>11.24</td>
<td>50.27</td>
<td>166.56</td>
<td>14.15</td>
<td>54.90</td>
<td>180.63</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ji</td>
<td>11.21</td>
<td>43.31</td>
<td>128.49</td>
<td>12.05</td>
<td>40.85</td>
<td>180.62</td>
<td></td>
<td></td>
</tr>
<tr>
<td>RLZ</td>
<td>12.66</td>
<td>53.61</td>
<td>173.98</td>
<td>13.52</td>
<td>56.05</td>
<td>183.19</td>
<td></td>
<td></td>
</tr>
<tr>
<td>BT</td>
<td>4.55</td>
<td>31.39</td>
<td>96.08</td>
<td>11.68</td>
<td>45.46</td>
<td>147.78</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>7</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mem</td>
<td>12.83</td>
<td>43.79</td>
<td>161.40</td>
<td>13.77</td>
<td>49.07</td>
<td>178.84</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ji</td>
<td>9.08</td>
<td>35.83</td>
<td>131.01</td>
<td>9.69</td>
<td>31.44</td>
<td>109.14</td>
<td></td>
<td></td>
</tr>
<tr>
<td>RLZ</td>
<td>10.21</td>
<td>38.55</td>
<td>154.62</td>
<td>11.13</td>
<td>42.26</td>
<td>166.62</td>
<td></td>
<td></td>
</tr>
<tr>
<td>BT</td>
<td>7.22</td>
<td>25.77</td>
<td>97.27</td>
<td>11.67</td>
<td>49.35</td>
<td>150.96</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>9</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mem</td>
<td>11.49</td>
<td>44.41</td>
<td>158.03</td>
<td>12.72</td>
<td>68.70</td>
<td>217.57</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ji</td>
<td>10.85</td>
<td>40.15</td>
<td>160.83</td>
<td>11.91</td>
<td>44.85</td>
<td>173.98</td>
<td></td>
<td></td>
</tr>
<tr>
<td>RLZ</td>
<td>7.47</td>
<td>25.77</td>
<td>97.27</td>
<td>11.67</td>
<td>49.35</td>
<td>150.96</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>block Algorithm</th>
<th>Bunny</th>
<th>256K</th>
<th>1M</th>
<th>4M</th>
<th>Finger</th>
<th>256K</th>
<th>1M</th>
<th>4M</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>5</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mem</td>
<td>10.31</td>
<td>37.86</td>
<td>130.35</td>
<td>11.72</td>
<td>43.08</td>
<td>134.03</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ji</td>
<td>9.77</td>
<td>34.14</td>
<td>100.04</td>
<td>9.27</td>
<td>36.70</td>
<td>115.59</td>
<td></td>
<td></td>
</tr>
<tr>
<td>RLZ</td>
<td>11.75</td>
<td>49.33</td>
<td>162.55</td>
<td>12.92</td>
<td>54.05</td>
<td>187.88</td>
<td></td>
<td></td>
</tr>
<tr>
<td>BT</td>
<td>6.93</td>
<td>26.29</td>
<td>99.39</td>
<td>11.68</td>
<td>49.35</td>
<td>150.96</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>7</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mem</td>
<td>9.60</td>
<td>32.75</td>
<td>115.49</td>
<td>11.81</td>
<td>43.86</td>
<td>159.19</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ji</td>
<td>10.33</td>
<td>32.63</td>
<td>102.05</td>
<td>11.11</td>
<td>45.08</td>
<td>171.04</td>
<td></td>
<td></td>
</tr>
<tr>
<td>RLZ</td>
<td>9.62</td>
<td>36.59</td>
<td>141.94</td>
<td>11.21</td>
<td>48.32</td>
<td>171.04</td>
<td></td>
<td></td>
</tr>
<tr>
<td>BT</td>
<td>5.38</td>
<td>17.65</td>
<td>57.87</td>
<td>11.11</td>
<td>45.08</td>
<td>171.04</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>9</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mem</td>
<td>8.51</td>
<td>31.55</td>
<td>112.12</td>
<td>15.91</td>
<td>57.20</td>
<td>187.88</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ji</td>
<td>10.04</td>
<td>37.33</td>
<td>145.76</td>
<td>11.72</td>
<td>44.88</td>
<td>176.55</td>
<td></td>
<td></td>
</tr>
<tr>
<td>RLZ</td>
<td>4.38</td>
<td>15.35</td>
<td>52.96</td>
<td>10.01</td>
<td>51.08</td>
<td>202.12</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 1: Time (in milliseconds) achieved for compaction of the image data set. The $i_-$ prefix denotes the negative version.

them with three different resolutions: 512x512 (denoted as 256K); 1024x1024 (1M); and 2048 x 2048 (4M). Figure 11 depicts thumbnails of the used images, with white pixels representing valid elements, and as well the corresponding overall data density. As it is observable, the images have distinct spatial frequencies with correspondence in distinct regional data densities.

Tests were conducted using the four algorithms and three different block sizes: 32; 128; and 512, respectively. As, for the tested hardware, the maximum loop count on fragment programs is of 256, the Jumping Jack algorithm was not tested for the larger block size. The achieved results are shown in Table 1. For each data set, the overall best result is depicted with bolder font and the overall best result using a monotonic algorithm (i.e. excluding Jumping Jack) is represented with a darker background.

The most relevant fact revealed is that there are distinct settings (algorithm and block size) achieving the best performance for the different data sets. Two major conclusion can be drawn. The first is that there is not a general optimal setting, and the second is that this optimal setting can only be determined with a priori knowledge about the data distribution.

The above discussion opens an interesting avenue for research on how to explore the best of each algorithm by using an optimal meta-algorithm, which should be able to make the most appropriate choices of the basic algorithm and block size. Several options may apply in the design of such optimized meta-algorithm. A first approach could pursue an adaptation to the expectable best performing algorithm and block size, based on a local or regional evaluation of the data. Thus, for the same data set, it would be possible to choose several parameters for different regions. Another approach may comprise a more low-frequency optimization, assuming that the data may vary along the time with some coherency. Hence, it should be possible to optimize the algorithm in order to adapt to the current pattern of the data. We shall also notice that the algorithmic performance depends on the underlying architecture of the GPU as well (e.g. degree of parallelism, branch and loop control, granularity, etc.). Thus, the solution for a given hardware setting may not be the more optimized for another setting, even for identical datasets.

5 CONCLUSIONS

This paper introduces the RLZ and the Binary Tree algorithm for parallel stream compaction. We used these algorithms within a block based compaction mechanism in order to handle large streams without coordinate conversion overhead and also taking advantage from the texturing capabilities of the GPU. We tested our proposals against existent algorithms.

The achieved results demonstrate the practical usefulness of our proposal. The RLZ algorithm proved to be competitive with prior algorithms, outperforming them in some circumstances. It presents the most data independent performance which makes it the most stable and predictable algorithm.

The Binary Tree algorithm is globally the fastest, taking advantage by not doing an explicit computation of the all-prefix-sum. However, we have also observed from the experiments that, for real data-sets, an optimal choice on the algorithm and parameters is not obvious and may require some knowledge on the data distribution, not only on a global basis but also on a local or regional basis. In this context, we outlined a meta-algorithm able to adapt to the data in order to have an optimized performance. As future work, we plan to further research on this topic.

Our implementations have room to be further op-
timized. We plan to continue testing the algorithms in a broader range of hardware platforms and diversified data sets, expecting further insights that can lead to improved variations and ideas, and so, another avenue to future work focus on how these algorithms and concepts adapt to new architectures and forthcoming standards.

ACKNOWLEDGEMENTS

This work has been partially supported by European Social Fund program, public contest 1/5.3/PRODEP/2003, financing request no. 1012.012, medida 5/acção 5.3 - Formação Avançada de Docentes do Ensino Superior, submitted by Escola Superior de Tecnologia e Gestão of Instituto Politécnico de Viana do Castelo.

REFERENCES


