PARTICLE SWARM FEATURE SELECTION FOR FMRI PATTERN CLASSIFICATION

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Abstract: The application of pattern recognition to functional magnetic resonance imaging (fMRI) data enables exiting possibilities, including mind-reading and brain-machine interfacing. This paper presents a novel brain state identification approach, which, using an algorithm based on particle swarm optimization (PSO) in conjunction with a classifier of choice, identifies important brain voxels – thus both maximizing the classification performance and identifying physiologically relevant areas of the brain. For classifiers, we have investigated simple multiple linear regression (MLR) with thresholding and linear support vector machines (SVMs). Applying the PSO algorithm to single-subject, 2D data from a pleasant touch study, originally containing 5650 voxels, voxel subsets of mean size 64.8 and 132.6 voxels with classification accuracies of 73.1% and 77.0%, respectively for MLR and SVMs, was obtained. Similarly, on group level 3D data from a fingertapping study, with a total volume of 61078 voxels, a classification score of 83.5% was achieved on 89 voxels using the linear regression approach. For both datasets, the identified voxels agreed well with both general linear model T-maps and physiologically expected regions of activation. The PSO is thus effective in the identification of high-performing voxel subsets for fMRI volume classification, and also provides physiological information about brain processing related to the experimental conditions. Moreover, the PSO is a user-friendly algorithm, requiring little input from the user in terms of parameter specification.

1 INTRODUCTION

The identification of instantaneous cognitive states based on physical measurements has recently proven not only feasible, but also highly useful to basic neuroscience research as well as clinically. It has, for example, been shown that it is possible to recognize the spatial pattern of blood flow changes in the brain, registered using functional magnetic resonance imaging (fMRI) using machine learning techniques (Norman et al., 2006). These methods typically involve the training of a classifier, such as support vector machines (SVM; Suykens et al., 2002), to identify and label patterns of brain activity.

This kind of multivariate analysis, where groups of voxels are analyzed collectively, have several advantages over conventional, univariate general linear model (GLM; Friston et al., 1994) methods, where each voxel is analyzed individually. Weak information contained in single locations can be accumulated and brain regions that do not individually carry relevant information might do so when jointly analyzed, and the multivariate approach is thus more sensitive (Björnsdotter Åberg and Wessberg, 2008). Moreover, a trained classifier can be utilized in the identification of real-time brain states which offers numerous exciting possibilities (see e.g Norman et al., 2006 for a review).

Due to practical considerations a restricted number of fMRI volumes (in the order of hundreds) can be obtained per scanning session. However, the dimensionality of fMRI data is exceedingly high (typically tens of thousands of brain volume voxels per time unit), warranting feature reduction to alleviate the curse of dimensionality (Bellman, 1961). Feature selection, that is, the explicit identification of a limited number of informative voxels (Blum and Langley, 1997), allows for both the localization of involved brain areas and the use of classifiers which can handle non-linearites.

We therefore propose an approach to fMRI brain state classification which includes the detection of a number and combination of voxels that, directly in conjunction with a classifier, optimally carry informa-
Data acquisitions were made with three volumes of fingertapping, where the subjects were instructed to tap their right hand fingers to the thumb, and three volumes of rest alternating according to visual cues for 120 volumes.

All data was motion corrected. In order to compensate for hemodynamic delay, the first of each three subsequent volumes of stimulus or rest was omitted and an average was formed from the remaining two, resulting in a total of 160 volumes the tactile stimulation, and 40 volumes per individual for the finger-tapping. For comparison, a standard general linear model analysis was performed on spatially smoothed (6mm Gaussian kernel) data (Friston et al., 1994).

In the tactile, single-subject dataset the 2D slice (5650 voxels) containing the secondary somatosensory cortex, highly involved in the processing of tactile stimulations, was extracted (Olausson et al., 2002). The fingertapping data was transformed to standard MINI-space. From the resulting 91 slices, the 20 most dorsal, containing the primary motor cortex and supplementary motor area, were extracted. The subject data was then pooled, resulting in a dataset containing 360 volumes and 61078 voxels.

The resulting data was randomly divided into three sets: 70% in the training set, and 15% each in the test and validation sets. In all datasets there were equal numbers of each category, and the classification task was distinguishing between stimulus (fingertapping or brushing) and rest. The training dataset was used for particle fitness computation, whereas the performance over the iterations was monitored using the testing data. The final classification performance result was computed on the validation data, using the particle with the highest performance on the testing data.

For data visualization, the program MRICron (by Chris Rorden, www.sph.sc.edu/comd/rorden/mricron/) was used, and all subsequent analysis was implemented in Matlab (The Mathworks, Massachusetts, USA).

2.2 Particle Swarm Optimization

Particle swarm optimization (PSO) is a stochastic optimization method (Kennedy and Eberhart, 1995), loosely based on the behavior of swarming animals such as birds and fish. A number of particles, representing potential solutions to the problem, are released in the search space of potential solutions. Each particle has a position and a velocity, and is free to fly around the search space. The movement is controlled, however; the particles accelerate towards the the position of the best performing particle as well as towards...
each particle’s personal best previous position. The PSO algorithm, described in Table 1, is governed by a set of rules describing how each particle’s position and velocity changes over time.

### 2.2.1 Standard Particle Swarm Optimization

The functions which update each particle’s position and velocity are fundamentally important. In a standard PSO with an \( N \)-dimensional search space, the particle velocity (1) and position (2), respectively, are manipulated thus:

\[
v_{id} = w \times v_{id} + c_1 \times r_1 \times (p_{id} - x_{id}) + c_2 \times r_2 \times (p_{gd} - x_{id})
\]

\[
x_{id} = x_{id} + v_{id}
\]

where \( v \) signifies the velocity of particle \( i \), \( x \) the corresponding position, and \( d \), ranging from 1 through \( N \), represents the optimization dimension. \( c_1 \) is the so-called cognitive parameter, determining the degree of acceleration towards the particle’s personal best position \( p_{id} \), and \( c_2 \) is a social parameter, determining the acceleration towards the global best position \( p_{gd} \).

\( w \) is an inertia parameter, regulating the overall rate of change. The stochastic nature of the velocity equation is represented by \( r_1 \) and \( r_2 \), which are random numbers in the range \([0,1]\).

To maintain coherence in the swarm, the maximum velocity is regulated by a parameter \( v_{\text{max}} \). In standard PSO implementations, a typical value is \( v_{\text{max}} = \|x_{\text{max}} - x_{\text{min}}\| \).

### 2.2.2 Particle Swarm Optimization for Feature Selection

In the case of feature selection, the standard PSO must be modified. The present algorithm is an implementation of the feature selection method proposed by Wang et al. (Wang et al., 2007).

Given \( N \) as the total number of features, the search space is binary (any feature is ‘on’ or ‘off’) and \( N \)-dimensional. The particle position represents those features (voxels) which are selected. In the approach suggested by Wang et al., the position is encoded as a binary array of length \( N \), where a ‘1’ represents that the corresponding feature is selected, and, conversely, ‘0’ indicates that the feature is not selected. Due to the excessive dimensionality of fMRI data, however, we have chosen to sparsely encode particle positions as arrays of integers containing indices of selected features.

The velocity of the particles represents how many features will be changed from ‘selected’ to ‘not selected’ or vice versa during the update of the position.

The velocity is thus an integer in the range \([1, v_{\text{max}}]\), and, in this implementation, the parameter \( v_{\text{max}} \) was set to \( N/3 \).

In accordance with equation 1, the velocity of a particle is dependent on the distance between two positions, for example \( p_{id} \) and \( x_{id} \). Let \( a \) denote the number of features that are selected in position \( p_{id} \) but not in position \( x_{id} \). Let \( b \) denote the number of features that are selected in position \( x_{id} \) but not in position \( p_{id} \). The distance between these two positions, \( p_{id} - x_{id} \), is then expressed as \((a - b)\). Additionally, the velocity can only be positive, wherefore the absolute value of the result of equation 1 is taken.

The modified equation for updating a particle’s velocity in this application is thus:

\[
v_i = \text{abs}(w \times v_i + c_1 \times r_1 \times (p_i - x_i) + c_2 \times r_2 \times (p_{gd} - x_{id}))
\]

(3)

However, if the number of features that differs between the particle’s current position \( x_i \) and the global best position \( p_{gd} \) is \( \Delta \), two different situations are possible when updating the position with the new velocity \( v_i \):

1. \( v_i \leq \Delta \): \( v \) features that differ between \( x_i \) and \( p_{gd} \) will be selected/unselected. That is, particle \( i \) will ‘fly’ towards \( p_{gd} \) in a random manner.
2. \( v_i > \Delta \): All features in \( x_i \) will be set equal to \( p_{gd} \), and \( v - \Delta \) features will be randomly selected/unselected. The particle will thus pass by the global best position and continue exploring the search space with the velocity \( v - \Delta \).

To promote initial exploration of the search space, and, conversely, convergence and exploitation of ‘good’ neighbourhoods towards the end of an algorithm run, the inertia parameter \( w \) is set to decrease linearly over time according to the following equation:

\[
w = w_{\text{max}} - (w_{\text{max}} - w_{\text{min}}) \times \frac{\text{iter}}{\text{iter}_{\text{max}}}
\]

(4)

where \( \text{iter} \) is the current iteration and \( \text{iter}_{\text{max}} \) is the maximum number of iterations. The parameters \( w_{\text{max}} \) and \( w_{\text{min}} \) are specified maximum and minimum \( w \)-values respectively.

### 2.2.3 Fitness Measure

With each iteration, a fitness measure indicating the goodness of that particular solution, is computed for each particle as follows:

\[
f_i(M_e) = \frac{M_e}{M} - \epsilon d_e
\]

(5)
Table 1: Algorithm for PSO with \( n \) particles. \( x_i \) denotes the position for particle \( i \), and \( v_i \) the corresponding velocity.

1. Initialize random positions and velocities for particles, \( x_i, v_i, i = 1...n \)
2. Evaluate each particle in the swarm, \( x_i \rightarrow f(x_i) \)
3. Update the best position for each particle and the global best position.
   - if \( f(x_i) > f(p_i) \) \( \Rightarrow p_i = x_i \)
   - if \( f(x_i) > f(p_g) \) \( \Rightarrow p_g = x_i \)
4. Update velocity and position for each particle, according to equation 1.
5. Return to step 2 unless the termination criterion has been met.

where \( M_c \) is the number of correctly classified patterns out of the total \( M \) patterns, \( d_i \) is the average deviation for correctly classified samples from the class labels '0' or '1', and \( \varepsilon \) is a constant small enough that a particle with a higher \( M_c \) is always receives higher fitness than a particle with a lower \( M_c \). This measure ensures a good fitness distinction, especially for patterns that are near the separating hyperplane.

For classifiers, we used both linear support vector machines (Suykens et al., 2002), popularly used in fMRI classification and simple least squares multiple linear regression with thresholding.

### 2.2.4 Feature Ranking

In order to reduce the time required for the PSO algorithm to filter out highly irrelevant voxels, a univariate feature ranking method was employed. For each feature \( f_i \) a ranking value was calculated thus:

\[
    f_i = \text{abs}(\frac{\mu_0 - \mu_1}{\sigma_0 + \sigma_1}) \tag{6}
\]

where \( \mu_0 \) and \( \mu_1 \) is the mean value of feature \( i \) over the volumes belonging to class 0 and 1 respectively, and \( \sigma_0 \) and \( \sigma_1 \) are the standard deviations within each class. The feature ranking value is thus a measure of how stable a feature is over the volumes, as well as how distinctly it can separate the data classes.

The features are ranked accordingly in ascending order. Any feature \( i \) has the following probability \( P_i \) of being selected in the position update function:

\[
    P_i = \frac{n_i}{\sum_{i=1}^{N} n_i} \tag{7}
\]

given the feature position \( n_i \), where \( N \) is the total number of features. This approach acts as a mild filter, prioritizing features that are univariately differentiating yet does not dominate multivariately important voxels.

### 3 RESULTS

All classification results plotted as a function of the number of PSO algorithm iterations refer to the performance on the testing dataset, which is used to monitor performance over time. All other results represent the classification performance using the classifier with the highest performance on the testing dataset as applied once to the unseen validation dataset. 50% corresponds to chance. The social and cognitive parameters of the PSO were empirically set to 2.

#### 3.1 Single-Subject Data

On the individual level 2D tactile data, we applied the PSO algorithm using both the fast least squares multiple linear regression with thresholding and the slower, more complex (linear) support vector machines for classification. The PSO algorithm was applied to the single-subject dataset 100 times, for 30 iterations of the algorithm.

The PSO algorithm proved highly successful in increasing the classification performance on the testing data with both classifiers (see figure 1). However, where there was a substantial increase in performance for the MLR classifier (from 58.1% to 73.3%), the increase for the SVM-based approach was more moderate (from 68.4% to 74.2%). At peak performance, the MLR achieves similar classification accuracies as the SVM: 73.3% vs. 74.2%. Also, the MLR appeared to over-train, showing a reduction in performance at 20 iterations, whereas the SVM generalizes better and reaches a plateau after 10 iterations. Moreover, the average final feature subset size using the MLR approach was 64.8 voxels, whereas with the SVM noticeably more voxels, 132.6, were obtained. However, the time requirements also differ substantially: the time required for one run is more than 10-fold longer for SVM (132.8s) than for MLR (12.6s). On unseen validation data, the percentage correctly classified volumes was 73.1% for MLR and higher at 77.0% for the SVM.

Interestingly, the voxel selection maps, illustrating the location and selection frequency (in the fi-
Performance (%)

Figure 1: Classification performance on the testing data as a function of the number of PSO algorithm iterations on the 2D single-subject tactile dataset, using multiple linear regression (MLR) and support vector machines (SVM).

Figure 2: The voxel selection maps generated by 100 PSO iterations on the tactile, single-subject data, and thresholded to show only outliers. The multiple linear regression-based classifier (MLR) and support vector machine (SVM) produce similar maps, and both agree well with the univariate, standard general linear model (GLM) T-map albeit appearing substantially more specific. The approximate location of the secondary somatosensory cortex is circled.

Table 2: List of most selected voxels from figure 2. The lower ranking number, the higher the probability of inclusion of that particular feature in the PSO position update. The maximum possible selection frequency is 100.

<table>
<thead>
<tr>
<th>Feature no.</th>
<th>MLR Selection freq.</th>
<th>Rank</th>
</tr>
</thead>
<tbody>
<tr>
<td>2183</td>
<td>20</td>
<td>30</td>
</tr>
<tr>
<td>2184</td>
<td>15</td>
<td>200</td>
</tr>
<tr>
<td>2249</td>
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<td>179</td>
</tr>
<tr>
<td>1727</td>
<td>8</td>
<td>315</td>
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<table>
<thead>
<tr>
<th>Feature no.</th>
<th>SVM Selection freq.</th>
<th>Rank</th>
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</thead>
<tbody>
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<td>30</td>
</tr>
<tr>
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<td>22</td>
</tr>
<tr>
<td>2182</td>
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<td>7</td>
</tr>
<tr>
<td>2502</td>
<td>22</td>
<td>118</td>
</tr>
</tbody>
</table>

3.2 Multi-Subject Data

On the whole-volume fingertapping, multi-subject data, the PSO algorithm in combination with the MLR was also successful in identifying highly relevant voxels. Despite the substantially larger voxel pool (61,078 vs. 5650 voxels), excellent testing data classification improvement was seen, on average (over 500 runs) increasing from slightly above chance in the first iteration to near 85% in the last. High classification scores were achieved with a mean test data performance of 83.5% (corresponding mean voxel subset size of mere 89 voxels), and the resulting validation data performance was 83.5%.

The cluster of most frequently selected voxels was located in Brodmann area 4 (Talairach coordinates: -38 -20 56), containing the primary motor cortex which is highly involved in the processing of movement.

4 DISCUSSION

This study has successfully implemented an fMRI pattern classification algorithm, based on particle swarm optimization, that not only achieves high performance scores but also identifies functionally relevant brain areas. Moreover, the method is easy to use and requires little parameter specification.

The SVM classifier generally achieved higher classification results than the MLR, which is expected since the SVM is a maximum margin classifier with better (theoretical) generalization. Similarly, feature selection proved exceedingly important for the simple linear regression classifier, whereas the support vector machine, as is well established, handles large dimen-
sionalites better. The difference in PSO run time is more than 10-fold between MLR and SVM, on the other hand, resulting in a trade-off between classification performance and speed of computation. Since the PSO algorithm is iterative in nature, and thus fairly computationally intensive, the MLR alternative can be preferred during the feature selection process.

The feature selection frequency maps were thresholded by including only voxels in the outlier range (figure 2), which does not, naturally, guarantee that these voxels differ significantly between conditions. Proper significance thresholding can, however, be easily performed using non-parametric permutation testing.

When comparing the feature selection frequency with the univariate feature ranking (figure 2), it can be seen that, with both classifiers, roughly the same features have a high selection frequency. These are all located in an area that is consistent with the known anatomical location of the secondary somatosensory cortex, as confirmed by the general linear model T-map. Moreover, the voxel selection maps (figure 2) appear virtually identical, and it can thus be assumed that, for multivariate activation localization, either SVM or MLR can be used with similar results. Also, if maximal classification scores are required, the SVM can be applied on the final selected voxel subset.

The most frequently selected voxels, however, do not have the highest ranking values (table 2), showing that univariate ranking of the features influences but does not dominate the feature selection process.

The low scores achieved when using only the outlier voxels as input into a classifier, indicates that high-scoring subsets must contain a large variety of features, including some specific key voxels. These key voxels appear essential to high accuracy discrimination of conditions, but are poor as individual predictors. The key voxels can be identified by repetitions of the PSO-algorithm, and subsequent investigation of the feature selection frequency. This is evidence for a distributed nature of brain activation patterns, where optimal voxel subsets may include features that, when analyzed individually, do not indicate any significant difference between conditions. Moreover, this prompts the need for multivariate feature selection allowing for distributed voxel subsets.

5 CONCLUSIONS

Our proposed particle swarm optimization approach is effective for fMRI pattern classification, and, moreover, warrants a user-friendly implementation. Also, the algorithm can be used to localize voxels that are highly involved in processing of given conditions. Simple and fast multiple linear regression approaches appear suitable for the localization of relevant voxels, whereas for situations where high-accuracy classification is required SVMs are highly recommended.

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