

AN ECoG BASED BRAIN COMPUTER INTERFACE WITH SPATIALLY ADAPTED TIME-FREQUENCY PATTERNS

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Abstract: In this paper we describe an adaptive approach for the classification of multichannel electrocorticogram (ECoG) recordings for a Brain Computer Interface. In particular the proposed approach implements a time-frequency plane feature extraction strategy from multichannel ECoG signals by using a dual-tree undecimated wavelet packet transform. The dual-tree undecimated wavelet packet transform generates a redundant feature dictionary with different time-frequency resolutions. Rather than evaluating the individual discrimination performance of each electrode or candidate feature, the proposed approach implements a wrapper strategy to select a subset of features from the redundant structured dictionary by evaluating the classification performance of their combination. This enables the algorithm to optimally select the most informative features coming from different cortical areas and/or time frequency locations. We show experimental classification results on the ECoG data set of BCI competition 2005. The proposed approach achieved a classification accuracy of 93% by using only three features.

1 INTRODUCTION

Brain-computer interfaces (BCIs) use the electrical activity of the brain for communication and control. Since the muscles are bypassed, a BCI can be used by people with motor disabilities to interact with their environment. Electroencephalogram (EEG) is widely used in BCIs due to its non-invasiveness. However, the low signal to noise ratio (SNR) and spatial resolution of EEG limit its effectiveness in BCIs. On the other hand invasive methods such as single neuron recordings have higher spatial resolution and SNR. However, they have clinical risks. Furthermore, maintaining long term reliable recording with implantable electrodes is difficult. On the other hand, an electrocorticogram (ECoG) has the ability to provide long term recordings from the surface of brain. Furthermore, ECoG signals also provide information about oscillatory activities in the brain with a much higher bandwidth than EEG (Leuthardt 2004). Therefore, existing algorithms for EEG classification are readily applicable to ECoG processing.

Various events in brain signals such as slow cortical potentials, motor imagery (MI) related sensorimotor rhythms, and visual evoked potentials were used in construction of ECoG based BCIs (Wolpaw 2000,

Pfurtscheller 2001). In MI based BCIs, the subjects are asked to perform an imagined rehearsal of either hand/finger or foot movement without any muscular output. Related events in sensorimotor rhythms such as alpha (7-13Hz) and beta (16-32Hz) bands are processed to recognize the executed task using only brain waves. Several methods have been proposed to extract relevant features for BCI classification from rhythmic activities. Methods such as autoregressive modeling and sub band energies in predefined windows are widely used in single trial ECoG classification (Schlogl 1997, Prezenger 1999). When used with multi channel recordings, all of these methods need to deal with the high dimensionality of the data. Selecting the most informative electrodes and adapting to subject specific oscillatory patterns is critical for accurate classification. However, due to the lack of prior knowledge, selection of the most informative electrode locations can be difficult. Furthermore, it is well known that there exists a great deal of inter subject variability of EEG and ECoG patterns in spatial, temporal, and frequency domains (Ince 2006, Ince 2007, Leuthardt 2004, Prutscheller 2001 and Schlogl 1999). In (Ramoser 2000), the common spatial patterns (CSP) method was proposed to classify multichannel EEG recordings. The CSP

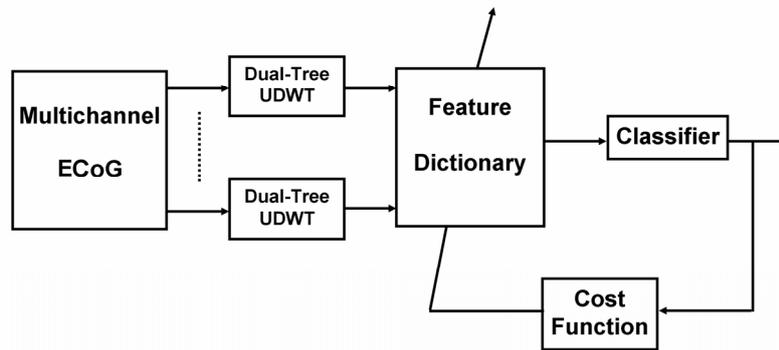


Figure 1: The block diagram of the proposed feature extraction and feature subset selection technique.

method weighs each electrode location for classification and uses the correlation between channels to increase the SNR of the extracted features. Although the performance is increased with CSP, it has been shown that this method requires a number of electrodes to improve classification accuracy and that it is very sensitive to electrode montage. Furthermore, since it uses the variance of each channel, this method does not account for the spatiotemporal differences in distinct frequency subbands. Recently, time-frequency methods have been proposed as an alternative strategy for the extraction of MI related patterns in BCI's (Wang 2004, Ince2006 and Ince 2007). These methods utilized the entire time-frequency plane of each channel and integrate components with different temporal and spectral characteristics. Promising results were reported on well known data sets while classifying multichannel EEG. One of the main difficulties with these methods is once again dealing with the high dimensionality of the data collected. Furthermore, the adaptation to important patterns is implemented either by only accounting for the discrimination power of individual electrode locations or simultaneous processing of a large number of electrodes.

In this paper we tackle these problems by implementing a spatially adapted time-frequency plane feature extraction and classification strategy. To our knowledge this is the first time that an approach implements a joint processing of ECoG features with different time and frequency resolution coming from distinct cortical areas for classification purposes. The algorithm proposed in this paper requires no prior knowledge of relevant time-frequency indices and related cortical areas. In particular, as a first step, the proposed approach implements a time-frequency plane feature

extraction strategy on each channel from multichannel ECoG signals by using a dual-tree undecimated wavelet packet transform (UDWT). The dual-tree undecimated wavelet packet transform forms a redundant, structured feature dictionary with different t-f resolutions. In the next step, this redundant dictionary is used for classification. Rather than evaluating the individual discrimination performance of each electrode or candidate feature, the proposed approach selects a subset of features from the redundant structured dictionary by evaluating the classification performance of their combination using a wrapper strategy. This enables the algorithm to optimally select the most discriminative features coming from different cortical areas and/or time-frequency locations. A block diagram summarizing the technical concept is given in Figure 1. In order to evaluate the efficiency of the proposed method we test it on the ECoG dataset of BCI competition 2005.

The paper is organized as follows. In the next section we describe the extraction of structural time-frequency features with dual-tree undecimated wavelet transform. In the following section we discuss available feature selection procedures and details of our proposed solutions. We describe the multichannel ECoG data in section 4. Finally we provide experimental results in section 5 and discuss our findings in section 6.

2 FEATURE EXTRACTION

Let us describe our feature dictionary and explain how it is computed from the wavelet-based dual-tree structure. A schematic diagram of the dual tree is shown in Figure 2. As indicated in the previous sections, the ECoG can be divided into several

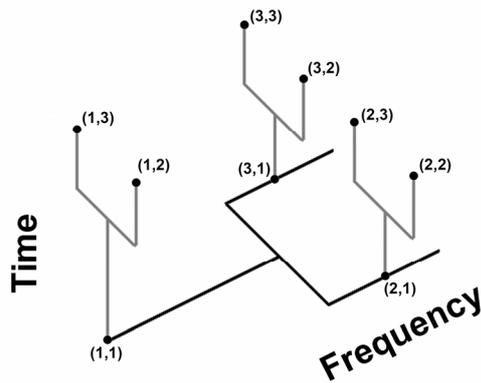


Figure 2: This dual tree uses 1-level in both planes. Each node of the horizontal tree is a frequency subbands. Node {1,1} represents unfiltered original signal, node {2,1} represents low pass filtered signal and node {3,1} high pass filtered. Each of these subbands is segmented in time into 3 segments, as shown in the vertical tree. Segment {1,1}, {2,1} and {3,1} covers the whole subband, segment {1,2}, {2,2} and {3,2} covers the first and segments with time indices three the second half of it.

frequency subbands with distinct and subject depended characteristic. In order to extract information from these rhythms, we examine subbands of the ECoG signal by using an undecimated wavelet transform. In each subband, a second pyramidal tree is utilized to extract the time varying characteristics of the subband.

2.1 Undecimated Wavelet Transform

Discrete Wavelet Transform (DWT) and its variants have been extensively used in 1D and 2D signal analysis (Vetterli 2001). However, the downsampling operator at the outputs of each filter produces a shift variant decomposition. In practice, a shift in the signal is reflected by abrupt changes in the extracted expansion coefficients or related features. In (Unser 1995) the undecimated wavelet transform is proposed to extract subband energy features which are shift invariant. This is achieved by removing the downsampling operation. The output at any level of pyramidal filter bank is computed by using an appropriate filter which is derived by upsampling the basic filter.

A filter $g(n)$ with a z-transform $G(z)$ that satisfies the quadrature mirror filter condition

$$G(z)G(z^{-1}) + G(-z)G(-z^{-1}) = 1 \quad (1)$$

is used to construct the pyramidal filter bank (Figure 3). The high-pass filter $h(n)$ is obtained by shifting

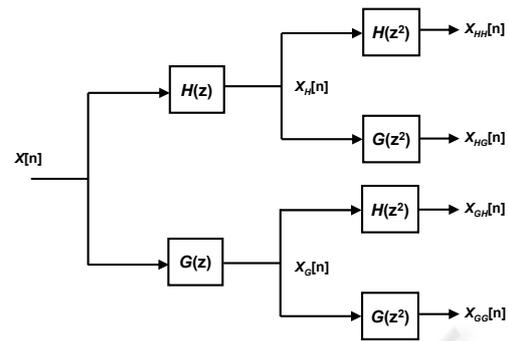


Figure 3: The pyramidal undecimated wavelet tree.

and modulating $g(n)$. Specifically, the z transform of $h(n)$ is chosen as

$$H(z) = zG(-z^{-1}). \quad (2)$$

The subsequent filters in the filter bank are then generated by increasing the width of $f(n)$ and $g(n)$ at every step, e.g.,

$$\begin{aligned} G_{i+1}(z) &= G(z^{2^i}) \\ H_{i+1}(z) &= H(z^{2^i}), \quad (i=0,1,\dots,N). \end{aligned} \quad (3)$$

In the signal domain, the filter generation can be expressed as

$$\begin{aligned} g_{i+1}(k) &= [g]_{\uparrow 2^i} \\ h_{i+1}(k) &= [h]_{\uparrow 2^i} \end{aligned} \quad (4)$$

where the notation $[\]_{\uparrow m}$ denotes the up-sampling operation by a factor of m .

The horizontal pyramidal tree of Fig.2 provides subband decomposition of the ECoG signal. Next, we segment the signal in each subband with rectangular time windows. Such an approach will extract the temporal information in each subband. As in the frequency decomposition tree, every node of the frequency tree is segmented into time segments with a pyramidal tree structure. Each parent time window covers a space as the union of its children windows. In a given level, the length of a window is equal to $L/2^t$ where L is the length of signal and t denotes the level. The time segmentation explained above forms the second branch (vertical) of the double tree. After segmenting the signal in time and frequency, we retain the energy of each node of the dual-tree as a feature. By using a dual tree structure we could calculate a rich library of features describing the ECoG activities with several

spectro-temporal resolutions. From now on we keep the index information of the dual tree structure to be used in the later stage for dimension reduction via pruning.

To summarize this section the reader is referred to the double tree structure in Fig. 2. Note that the dual tree structure satisfies two conditions:

- For a given node in the frequency tree, the mother band covers the same frequency band width (BW) as the union of its children

$$BW_{Mother} \supset (BW_{Child1} \cup BW_{Child2}) \quad (5)$$

- This same condition is also satisfied along the time axis. For a given node, the number of time samples (TS) of the mother window is equal to that of the union of its children.

$$TS_{Mother} \supset (TS_{Child1} \cup TS_{Child2}) \quad (6)$$

These two properties allow us to prune the tree structure. When a particular feature index is selected, one can remove those indices from the dual tree structure that overlap in time and frequency with the selected index. Let T be the number of levels use to decompose the signal in time and F be the number levels use to decompose the signal in the frequency domain, there will be $2^{(F+1)}-1$ subbands (including the original signal) and $2^{(T+1)}-1$ time segments for each subband. This will make the total number of potential features $NF=(2^{(F+1)}-1)(2^{(T+1)}-1)$.

3 SUBSET SELECTION

Calculating the dual-tree features for each electrode location forms a redundant feature dictionary. The redundancy comes from the dual tree structure. As explained in the previous section the dual tree has total $NF=(2^{(F+1)}-1)(2^{(T+1)}-1)$ features for each signal where F is the total number of frequency levels and T the total number of time levels. In a typical case, $T=3$, $F=4$ and over 64 electrodes are used resulting in a dictionary with around thirty thousand features. In such a high dimensional space ($NF=29760$) the classifier may easily go into over-learning and provide a lower generalization capability.

Here, we incorporate the structural relationship between features in the dictionary and use several feature subset selection strategies to reduce the dimensionality of the feature set. Since the features are calculated in a tree structure, efficient algorithms were proposed in the past for dimensionality reduction. In (Saito 1996) a pruning approach was proposed which utilizes the relationship between the mother and children subspaces to decrease the

dimensionality of the feature set. In particular, each tree is individually pruned from bottom to top by maximizing a distance function. The resulting features are sorted according to their discrimination power and the top subset is used for classification. Although such a filtering strategy with pruning will provide significant dimension reduction by keeping the most predictive features, it does not account for the interrelations between features in the final classification stage. Here, we reshape and combine the pruning procedure for feature selection with a wrapper strategy. In particular, we quantify the efficiency of each feature subset by evaluating its classification accuracy with a cost measure and we use this cost to reformulate our dictionary via pruning.

Four different types of methods are considered for feature selection in this study. The structure in Figure 1 is general representation of each of the four methods. The left most box in Figure 1 is the rich time-frequency feature dictionary. On the right end a linear discriminant (LDA) is used both for classification and extracting the relationship among combinations of features. This output is fed to a cost function to measure the discrimination power for that combination of features. This measure will be used to select the best among all other feature combinations. Furthermore, depending on the selected feature index, a pruning operation will be implemented to reduce the dimensionality in the rich feature dictionary.

In this particular study, the Fisher Discrimination (FD) criterion is used as a cost function.

$$FD = \frac{(\mu_1 - \mu_2)^2}{\sigma_1^2 + \sigma_2^2}. \quad (7)$$

The four different strategies mentioned above are: Sequential forward feature selection (SFFS), SFFS with pruning (SFFS-P), Cost function based pruning and feature Selection (CFS), and CFS with principal component analysis (PCA) post processing.

3.1 Sequential Forward Feature Selection: SFFS

The SFFS is a wrapper strategy which selects a subset of features one by one. A cost function is used on classifier output to measure the efficiency of each feature. By using LDA, the feature vectors are projected on a one dimensional space. Then the FD criterion was used to estimate the efficiency of the projection. After this search is done over all feature vectors, the best feature index is selected by

comparing the cost values of each feature vector. In the next step the feature vector which will do the best in combination with the first selected ones is identified by searching over the remaining feature vectors. This procedure is run until a desired number of features is reached. Note that SFFS uses all the boxes and connections in Figure 1 except for the feedback from the cost function to the dictionary. Since no dimension reduction is implemented on the entire feature space, this approach has high computational complexity.

3.2 SFFS with Pruning: SFFS-P

The SFFS-P is also a wrapper strategy with an additional pruning module for dimension reduction. Once a feature index is selected, the corresponding frequency tree and time tree indexes are calculated on the dual-tree. Then the nodes that overlap with the selected feature index in time and frequency are removed. Next, the feature which will do best in combination with the first selected feature is identified by searching the pruned dictionary. In other words, the dictionary is pruned based on the last selected feature. This procedure is run until the desired number of features is reached. Therefore, the only difference between SFFS and SFFS-P is that pruning is done on the dictionary based on the selected features. This provides a fast decrease in the number of candidate features and complexity is much smaller than SFFS.

3.3 Cost Function based Pruning and Feature Selection (CFS)

The CFS is a filtering approach that uses the structure in the feature dictionary for pruning. After finalizing the pruning procedure for each electrode location, it uses a cost function to rank the features. In particular, it uses the FD criterion to rank the features. It does not use either the LDA or the feedback path in Figure 1. Instead, using the FD measure, a cost value is computed for each node on the double tree individually. Then a pruning algorithm is run on the double tree by keeping the nodes with maximum discrimination. Once a node is selected all nodes overlapping with the selected one are removed. This procedure is iterated until no pruning can be implemented. After pruning the dual-trees for each electrode location, the resulting feature set is sorted according to their corresponding discrimination power and input to the classifier. In this way the most predictive features were entered to the classification module. Since no feedback is used from the classifier, the CFS has lower computational complexity than the other two methods.

The CFS method works as a filter on the electrodes by only keeping those indices with maximum discrimination power. However, since features are evaluated according to their discrimination power individually, such a method does not account for the correlations between features. In (Ince 2006 and Ince 2007) PCA analysis is performed on a subset of top sorted features to obtain a decorrelated feature set. The PCA post processed features are sorted according to their corresponding eigenvalues in decreasing order and used in classification. Here we will also use the PCA as a post processing step with the CFS to obtain a decorrelated feature set. We will refer this method as CFS-PCA.

4 MULTICHANNEL ECoG DATA

In order to evaluate the performance of the proposed method we used the multichannel ECoG (Lal 2005) dataset of BCI competition 2005 (ida.first.fraunhofer.de/projects/bci/competition_iii/). During the BCI experiment, a subject had to perform imagined movements of either the left small finger or the tongue. The ECoG data was recorded using an 8x8 ECoG platinum electrode grid which was placed on the contralateral (right) motor cortex as shown in Figure 4. All recordings were performed with a sampling rate of 1000Hz. Every trial consisted of either an imagined tongue or an imagined finger movement and was recorded for 3 seconds duration. To avoid visually evoked potentials being reflected

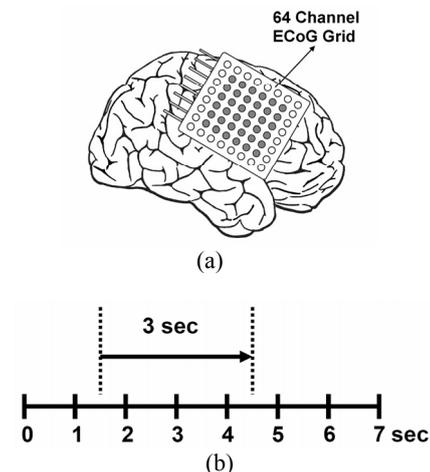


Figure 4: The 8x8 electrode grid was placed on the right hemisphere over the motor cortex (Modified from Lal 2005). For surface Laplacian derivation only marked electrodes are used. (b) The timing diagram of the experimental paradigm. The go cue for motor imagery is given at second one. A three second time window starting after 500ms of go cue is used to classify ECoG data.

by the data, the recording intervals started 0.5 seconds after the visual cue had ended. Each channel was filtered with a low pass filter in 0-120Hz band. The filtered data was down sampled by a factor 4 to 250Hz. Each trial was expanded from 750 samples into 768 samples by symmetric extension on the right side to enable segmentation in a pyramidal tree structure. Besides monopolar data, we also consider ECoG data that is processed using a surface Laplacian derivation. More specifically, each electrode data is subtracted from the weighted average of the surrounding 6 electrodes. The electrodes on the border are eliminated from the analysis resulting in a total of 36 electrodes (See Figure 4). For monopolar data all 64 electrodes were used for analysis. We used 278 trials for training and 100 trials for testing. The training and test data were recorded from the same subject and with the same task, but on two different days with about 1 week in between.

5 RESULTS

To extract the dual tree features we select $T=3$ and $F=4$. For a 125 Hz bandwidth, the frequency tree provided around 8Hz resolution at the finest level. Along the time axis, the time resolution was 375ms. The 12 tap Daubechies filter (db6) was used in constructing the frequency tree of the UDWT. In order to learn the most discriminant time-frequency indices and the corresponding cortical areas we utilized a 10 times 10 fold cross validation in the training dataset. The optimal feature number at which the classification error is minimal is selected from the averaged cross validation error curves. Then, the learned feature indices are used in testing the classifier on the test set. The results obtained with the different methods are presented in Table.1.

We note that the SFFS and SFFS-P provided the highest classification accuracy with only three features on the test set using the Laplacian derivation. Although a lower error rate was achieved by CFS with the training data, interestingly, the testing error rate of the CFS was higher than those of the other methods. We also note that a large number of features were used by CFS to achieve 9.9% error rate in the training set. In contrast, the SFFS and SFFS-P algorithms used only 3 features to achieve the minimum 10.2% error rate. The cross validation error curves versus the number of features are given in Figure 5. Since the results using Laplacian derivation outperformed those obtained with

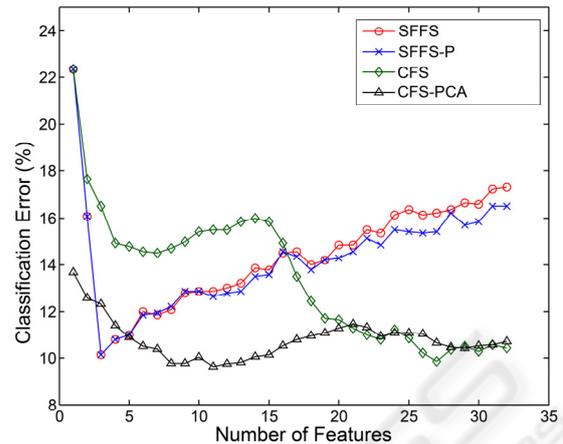


Figure 5: The cross validation error curves for the different methods in the training data.

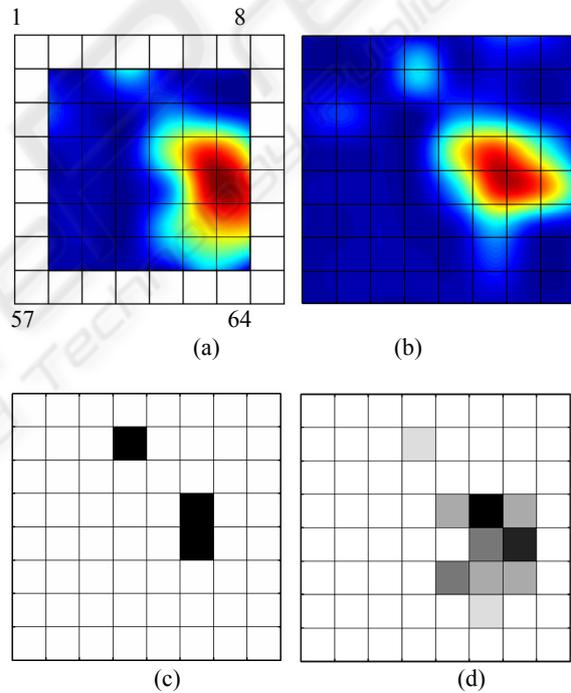


Figure 6: Discriminant cortical areas (a) Laplacian (b) Monopolar. The number of selected features from different electrode locations in Laplacian derivation for SFFS-P (c) and for CSF(d) are given. The darker areas indicate a higher number of features are selected from these regions. Note that SFFS-P provides a balanced feature distribution. The CSF selected most of 27 features from the same region.

monopolar data, only the results corresponding to the former are provided.

As can be seen clearly from these curves, SFFS and SFFS-P select the best combination of features and achieve the minimal error with only three features.

Table 1: The cross validation (CV) and test error rates of different methods and related number of features (NoF) used for final classification.

	<i>Method</i>	Training		Test
		<i>CV Error (%)</i>	<i>NoF</i>	<i>Error (%)</i>
<i>Laplacian</i>	SFFS	10.2	3	7
	SFFS-P	10.2	3	7
	CSF	9.9	27	18
	CSF-PCA	9.6	11	8
	SFFS	12.6	3	20
<i>Monopolar</i>	SFFS-P	10.3	4	9
	CSF	11.7	22	12
	CSF-PCA	11.2	14	8

Furthermore, using the structure of the feature dictionary, SFFS-P achieves this result with reduced complexity due to pruning. The pruning process provides a dimension reduction and feature decorrelation. CFS, on the other hand, achieves the minimal error using a large number of features. The interactions among the selected features cannot be taken into account with this approach. In addition the correlated neighbor areas may result in a duplication of information in the sorted features. In order to decorrelate the features a Principal Component Analysis (PCA) was employed on the CFS ordered features. This post processing step provided lower error rates than those achieved by CFS alone. The test error rate was 8% for the PCA post processed features. It should be noted here that CFS-PCA produced comparable results with those of SFFS and SFFS-P. However one should note that PCA induces an additional complexity. This method requires all 32 features to be extracted from ECoG which leads to a much higher computational complexity compared to three features selected by SFFS and SFFS-P.

Since the testing data was recorded on another date, the variability in the ECoG signal is expected. The results obtained indicate that the CFS algorithm is very sensitive to this type of variability. Although the cross validation error in the training set was low, the testing error rate was much higher compared to other methods. We believe that the correlated activity across cortical areas is an important reason why CFS selects the same information repeatedly. Since the SFFS and SFFS-P have the advantage of examining the interactions between different cortical areas and t-f locations, these subset selection algorithms can form a more effective subset of features for classification. In order to support our hypothesis we show the discriminatory cortical maps of monopolar and Laplacian derivations in Figure 6. In order to generate these images we used the most

discriminant feature of each electrode location and produced an image over the 8x8 grid to present the distribution of the most discriminative locations. Furthermore, we mark the electrode locations selected by SFFS, SFFS-P, and CFS for classification. After inspecting Figure 6 (a) and (b) we noticed that a large number of neighbor electrode locations carry discriminant information. The CFS method used a large number of electrodes from this region for classification. In contrast, the SFFS and SFFS-P methods selected another cortical area from upper side of the grid. Even though this electrode location does not seem to be very discriminative, it played a key role in achieving a lower classification rate on the validation data.

Since only three features are used by SFFS and SFFS-P, they are more robust to intra-subject variability of ECoG signals. Note also that the error rate in monopolar derivation is much higher than that of the Laplacian derivation. We observed large DC changes in ECoG signals in the test data set. Since the Laplacian derivation provides a differential operator, large baseline wanders affecting many electrodes are eliminated in this setup. However, for the monopolar recordings the features are very sensitive to this type of changes.

Note also that the validation accuracy of SFFS and SFFS-P in the test set is higher than the cross validation accuracy. One of the underlying reasons could be that the subject can control his/her brain patterns with a higher accuracy with the increasing number of trials. In addition the SNR of the signals might have improved over time due to tissue electrode interaction.

Finally, we compared our proposed method's test result with those of achieved at the BCI competition in 2005 using the same ECoG data. The classification accuracies and methods used in each method are presented in Table 2. Our method achieved the best result of 7% error with both SFFS

Table 2: The comparison of the proposed method with the best three methods from the BCI 2005 competition.

Features Used	Classifier	Error (%)
UDWT based subband energies	LDA	7
Common Spatial Subspace Decomposition	Linear SVM	9
ICA combined with spectral power and AR coefficients	Regularized logistic regression	13
Spectral power of manually selected channels	Logistic regression	14

and SFFS-P methods. We note that our proposed approach has outperformed both CSP and AR model based techniques.

6 CONCLUSIONS

In this paper we proposed a new feature extraction and classification strategy for multi-channel ECoG recordings in a BCI task. Rather than using predefined frequency indices or manually selecting cortical areas, the algorithm implemented an automatic feature extraction and subset selection procedure over a redundant time-frequency feature dictionary. This feature dictionary was obtained by decomposing the ECoG signals into subbands with an undecimated wavelet transform and then segmenting each subband in time successively. By combining a wrapper strategy with dictionary pruning, the method achieved 93% classification accuracy using only three features. The results we obtained show that the proposed method is a good candidate for the construction of an ECoG based invasive BCI system with very low computational complexity and high classification accuracy.

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