Reliable Biometrical Analysis in Biodiversity Information Systems

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Abstract. The conservation and sustainable utilization of global biodiversity necessitates the mapping and assessment of the current status and the risk of loss of biodiversity as well as the continual monitoring of biodiversity. These demands in turn require the reliable identification and comparison of animal and plant species or even subspecies. We have developed the Automated Bee Identification System, which has not only been successfully deployed in several countries, but also supports taxonomical research as part of the Entomological Data Information System.

Within this framework our paper presents two contributions. Firstly, we explain how we employ a model-driven extraction of polymorphic features to derive a rich and reliable set of complementary morphological features. Thereby, we emphasize new improvements of the reliable extraction of region-induced and pointinduced features. Secondly, we present how this approach is employed to derive new important results in biodiversity research.

1 The Role of Identification in Biodiversity Research

Genera and species with ecological or economical use are a very relevant topic in biodiversity research. The bees, *Apoidea*, are of special interest, because about 70% of the world's food crops are pollinated by them. The annual value of this pollination service has been reported to be about 65 billion US-\$, cf. [6]. Since there is an alarming extinction of crop pollinating bees due to diseases, parasites, and pests, as well as due to human interventions like clearing, pesticides, etc., bees are specially focused by biodiversity research.

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Drauschke M., Steinhage V., Pogoda de la Vega A., Stephan Müller S., Maurício Francoy T. and Wittmann D. (2007). Reliable Biometrical Analysis in Biodiversity Information Systems. In Proceedings of the 7th International Workshop on Pattern Recognition in Information Systems, pages 25-36 DOI: 10.5220/00024303300250036 Copyright © SciTePress Due to the worldwide lack of bee exerts (less than 50 experts, so-called bee taxonomists, worldwide) on the one hand and the urgency of monitoring and protecting endangered pollinating bee species, the Automated Bee Identification System ABIS has been developed. After training, ABIS performs a fully automated analysis of images taken from the forewings of bees. This fully automated analysis is the outanding quality of ABIS compared with all other approaches, which demand for intensive interactive processing of each specimen, e.g. [2] or [7]. Compared with these interactive approaches ABIS has been reported to be at least 50 times more effective since there is no need to adjust the wings into an exact position of the camera field. The fully automated approach provides together with the ABIS database an information system for the surveillance and management of biometrical data of one of the most important pollinating group worldwide. It has been successfully deployed for monitoring purposes in Germany, Brazil and the United States, cf. [12]. ABIS is also part of Entomological Data Information System (EDIS), a co-operative research project jointly undertaken by a number of leading German natural history museums and university institutions in the area of biodiversity informatics.



Fig. 1. Left: classification on demand: Bee experts use ABIS during their excursions. Middle: input image of an Africanized bee. Due to the image aquisition, the scale of all wings is in a small range. The wing's position and orientation does not impact the feature extraction. Right: detected cells and vein net of wing image.

The success of ABIS on identifying bee species leads now to a new challenge: the identification within the next taxonmical levels, i.e. subspecies and races, which are far more similar and therefore more difficult to separate. To face this difficult task of subspecies identification, we improve the extraction algorithms of morphological features, especially of the region-induced and point-induced features, i.e. cells and vein junctions. We demonstrate our improved approach within a fascinating taxonomical (oder biodiversity) research project on the so-called *killer bees*. In 1957, swarms of the African honey bee *Apis mellifera scutellata* accidentally escaped near Rio Claro, Brazil, and initiated a series of crosses and backcrosses with the pre-introduced European honey bee races, cf. [5].

This hybridization process resulted in the Africanized honey bee, which is better adapted to the tropics and broadly more productive than the European bees. Nevertheless, many beekeepers abandoned their activities in Brazil at the beginning of the Africanization process, because these bees presented undesirable traits like a high swarming rate and a strongly defensive behaviour (which led to their popular, but actually wrong name *killer bees*). In the meanwhile, the beekeepers have learnt how to work with these aggressive bees. Thus, the Africanized honey bee has spread throughout the (sub)-tropic Americas.

However, the evolution of the genetic and morphometric profiles of the bees from the beginning of the Africanization process in Brazil till now is still unknown. The results of comparing these profiles are not only important in taxonomic terms of biodiversity research, but may also show important practical implications for pollination management and beekeeping.

2 Robust Extraction of Reliable Features

2.1 Basic Steps

The traditional and manual classification approach of bees by taxonomists uses morphological characteristics of their whole body. If a subset of these features enables an automated, efficient recognition process, we call it a fingerprint. We derive such a fingerprint from a highly resolved digital image of a bee's wing as shown in Fig. 1. The images of the wings typically show under backlight illumination light regions, the transparent cells, which are surrounded by a dark net: the opaque veins and their junctions. We call the polymorphical features, i. e. the region-induced cells, the line-induced veins, and the point-induced junctions, *primary* features. From these primary features, we compute a set of *derived* features as listed in Table 1. The set of derived features forms one part of the fingerprint. On basis of the extracted features, we normalize the position and orientation of the wing and determine selected grayvalues for the second part of the fingerprint. The combination of both feature types, the derived features and the grayvalues, returns the best classification results, cf. [9].

derived from	feature
cells	area, circumference,
	distance of centers
	(absolute and relative values).
	eigenvalues and eccentricity
veins	length of curvature
junctions	distances and angles (along
	adjacent cells)

Table 1. List of derived features of the fin-



Fig. 2. Demonstration of clusters formed by fingerprints. Therefore, each feature vector is projected into a 2D-plane. The samples of the same subspecies of honey bees are colored identically.

The expert knowledge is inserted into ABIS within a training step, where genus specific *wing models* have to be learnt under supervision of a taxonomist. The wing models contain the expected cell contours including their variance as well as the expected positions of the vein junctions. Then, ABIS performs a fully automated feature extraction which consists of the following steps:

1. edge detection using gradient information and

- 2. cell extraction based on grouping of cell border segments until an initial substructure of cells could be verified by the system, cf. section 2.2,
- 3. adjusting the trained wing model to the present wing by an affine transformation T,
- 4. model-driven cell extraction for difficult cells and
- 5. precise location of the vein junctions and vein detection, cf. section 2.3,
- 6. derivation of rotational stable and translation invariant features from extracted cells and vein net, cf. Tab. 1,
- 7. statistical analysis of feature vector for bee species classification, cf. [9].

Before starting the classification, we perform a PCA to reduce the dimension of our feature vector and eliminate redundant information, i.e. if some features are highly correlated. Then, the classification can be operated by various discrimination algorithms. We gained the best results by using the kernel discriminant analyis as proposed by [8]. The integration of the expert knowledge will be done in an offline training step, which is necessary only once for each classification project. The following tasks must be done manually within the training step:

- 1. naming of the extracted cells,
- 2. identification and naming of the junction positions,
- 3. fine tuning of classification parameters.

Then, the identification of bee species and subspecies is able to run in a fully automated way.

In this section, we want to point out the improvements of our feature extraction. Firstly, star-shaped polygons form an appropriate model of all possible cell shapes. This model ensures a reliable cell detection, which is based on the grouping of extracted edges. Secondly, we model the localization of the junctions more precisely. The junctions are of special importance, because identification by bee experts and by ABIS relays heavily on the junction positions, i. e. many fingerprint features are derived from them.

2.2 The Use of Star-Shaped Regions for Cell Extraction

Since the border of the cells appear much darker than their inner points, the cell detection starts with an edge detection algorithm, which is based on an approach to line detection proposed by [11]. This approaches estimates the first and second derivatives of the image intensity by convolving the image with the derivatives of the Gaussian smoothing kernel, since this smoothing kernel makes the inherently ill-posed problem of estimating derivatives of noisy images well posed. In contrast to the line detection task tackled by Stegers approach, the line-shaped veins of the wing images show lines with highly variable width - even degenerating into region-shaped areas near the vein junctions. Therefore, we modify the line detection approach into an edge detection approach by searching for zero-crossings of the second derivative instead of the first derivative.

Generally, the detected edge pixels, so-called edgels, do not yield in continuous region borders. Pseudo veins and disturbances due to hairs and polls on the wings lead to locally positive false hypotheses of cell borders. Furthermore, mutations and low contrasts lead to locally negative false hypotheses of cell borders. Therefore, we developed

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Fig. 3. Left: all detected edge pixels. Middle: all detected straight edges of a minimum length. Right: all detected cell hypotheses.

a *domain specific grouping strategy*. Firstly, we determine all straight edgels of a minimum length, secondly, we classify all other edgels into left and right curved edgels, cf. Fig. 3.

If some straight edgels are directly connected to right curved edgels at their ends, we join them to construct cell hypotheses for our cell detection. Our iterative grouping strategy focuses on the gaps between the current hypotheses on the one hand and the remaining edgels on the other hand, cf. Fig. 3.

Bee taxonomists can tell us, that the cells in the bee wings are convex or star-shaped. Hence, we derive the following strategy. Thus, we call a set H of concatenated border edgels a *cell hypothesis*, if these concatenated edgels are clockwise ordered around their center, the mean of all edgels, and if they do not contain a cycle. \overline{H} denotes the closed cell hypothesis, where both endings of the cell hypothesis have been connected by a straight line. The grouping algorithm enlarges each hypothesis H until the closed border of a region is constructed by the edgels. Two constructive elements of the cell hypotheses are of interest for the cell detection: the center c(H) and the kernel ker(H)with

$$ker(H) = \left\{ p \in \overline{H} \mid \forall x \in \overline{H} : \overline{xp} \in \overline{H} \right\},\tag{1}$$

where \overline{xp} encodes all points on the straight line between x and p.

The grouping of the border edgels is comparable to a best first search: the algorithm is looking for the best aggregation with another cell hypothesis for closing the border of the original cell hypothesis. If the best fitting cell hypothesis does not close the hypothesis, it must reduce the gap between its endings. The gap size is measured by the angle α , which is defined by the end point, the center and the start point of the cell hypothesis.

More precisely, let H_s be the current cell hypothesis, which has a gap size of α_s . Then, in the next iteration step, we determine the new cell hypothesis from H_s by concatenation with an other appropriate cell hypothesis H_i , i.e. which has a nearly smooth transition to H_s . If there is no such cell hypothesis that closes H_s to a completely closed cell border, we append the candidates to resulting hypotheses H_{s+1} at either the beginning or the ending of the start hypothesis, respectively:

$$H_{s+1} = H_i \circ B \circ H_s \text{ or } H_{s+1} = H_s \circ B \circ H_i, \tag{2}$$

where B encodes the bridging pixels, which form a smooth transition between H_i and H_s . The gap sizes α_{s+1} of the resulting hypotheses H_{s+1} are determined with the old

center $c(H_s)$ of the start hypothesis, because we want to ensure a decreasing gap size. We do not recompute the center $c_{H_{s+1}}$ until we have decided for the best fitting cell hypothesis for aggregation.

When the centers of the cell hypotheses lie in the kernel of the reconstructed cell, this local inspection works very well. Then, the gap size α_i decreases monotonously, since all border points of the region are visible from the center, cf. the corollas on visibility polygons discussed by [3]. For convex cells, the center of each hypothesis lies in the kernel of the cell. Since several cells of a bee's wing are only star-shaped, we need to shift the center of a cell hypothesis iteratively with each hypothesis update towards the also iteratively changing kernel of the cell. This task can only be done in a heuristic way, combining the following two steps:

- 1. We compute the grayvalue gradient $\nabla g_{c(H)}$ from the neighborhood of center c(H) and shift c(H) in the direction of the maximum gradient, until a minimal distance to the cell border is reached. Especially, this is necessary to move the centers away from nearly straight hypotheses.
- 2. The shifted center (from step 1) gets replaced again, now by the mean of the center itself and both hypothesis's endings. This step has almost no impact on smaller, straight hypotheses, but a big one on hypotheses which already form a big part of a cell. Then, the center of such a hypothesis is pulled towards the opening of the hypothesis and is now much closer to the center of the extracted cell.



Fig. 4. Five cell hypotheses are shown as black lines, their centers are visualized by black dots. Finally, these cell hypotheses should be arranged together to build the cell. To show the importance of shifting the centers, we depict the kernel of the finally reconstructed cell by the gray filled polygon. The left image shows the original centers, which are all outside the kernel - the cell extraction fails in such a case. The right image shows the centers of the same cell hypotheses after their transformation - the cell extraction performs well.



Fig. 5. Wing Model as created in the training step. The average cell contours are shown by the darker lines which are surrounded by the minimum and maximum bounds of the cell contours. The junctions are set manually into the wing model.

We show an example in Figure 4, where we need to construct the cell shape from five cell hypotheses. None of the centers of those hypotheses lies in the kernel of the cell (left). Our closing procedure originally failed in these cases. Then we extended our approach and improved the positions of the centers of the cell hypotheses (right). If the centers were shifted towards the kernel, we were successful with reconstructing the cell. Nevertheless, in almost all cases, there is a cell hypothesis, whose center lies in the cell's kernel after the shifts have been done.

We tested our algorithms on about 25,000 cells. Due to the improvements on closing in the case of non-convex, but star-shaped cells, we are now able to detect all cells of a bee's wing in over 99.9% of all tested samples. Fig. 1 shows all detected cells of a wing image.

The extracted cell borders of all specimens of the training set form the basis for computing the wing model a genus or a group of genera. The wing model describes the expected cell borders as well as their geometric variances as learnt from the traing set, cf. Fig. 8. After training the wing model will be employed as a "road map" for the extraction of cell borders to identify the species or subspecies of speciemens of the trained genus or group of genera.

2.3 Positioning of the Vein Junctions Using the Wing Template

Classical biometrical approaches show that the appropriate junction positioning is crucial for the successful identification, because a large number of fingerprint features (i.e. distances, lengths, angles) will be derived from the junction positions, cf. Table 1. Thus, we have to place the junctions after the complete cell detection.

Therefore, during the training of a wing model, the taxonomist defines exactly the positions of the junctions into the model, cf. Fig. 5. These positionings will be aligned to the wing under investigation by the affine transformation T from step 3 of the feature extraction process in section 2. If p is the position of the j-th junction in the wing model, then p' = Tp is the estimated position of the junction in the wing.

We estimate the parameters of the affine transformation T from the centers of the cells in the wing model and the centers of initially extracted cells. These initially extracted cells are quite robustly to detect without the help of a wing model. They form the basis for the model-based extraction of the remaining cells together with the generic wing model. Intutionally, one might say that the inner cells of the wing image are the initially extracted cells, while the outer cells are the cells, which are more difficult to extract and therefor we need the wing model. Although, this estimation proved to be locally precise enough for our purpose, there is a need for readjusting the junction's coordinates, as seen in Figure 6. The final position is shown in the right part of Figure 6.



Fig. 6. Left: inprecise localization of junctions by affine transform. Right: final positions of the junctions after local rearrangements.

The localization of the junctions is improved with the use of explicit, spherical *junction templates*, which the bee expert defines also in the wing model. These templates do not

only contain the predicted position of a junction, but also its local neighbourhood

$$E_{r_1}(p) := \{ x \mid d(x, p) = ||x - p||_2 \le r_1 \},$$
(3)

and a analogously defined uncertainty area of a junction $U_{r_2}(p)$. A junction's environment shows the information about the adjacent cells and veins, see Figure 5, Fig. 6, and Figure 7. Its uncertainty area encodes all valid positions for the junction.



Fig. 7. Visualization of junction templates: E_{r_1} contains the adjacent cells in black. The information of the veins is derived from the the extruded cells (dilation with a circle, marked in light gray). Pixels outside of these extruded cells are unknown and marked in dark gray. The examples show (f.l.t.r.) one, two or three adjacent cells. Thereby, the values of the radii (f.l.t.r. 17, 19 and 23 [pxl]) are chosen by the taxonomic expert and encode the expert knowledge about the relevant local feature neighbourhood for placing the junctions.

With adjusting of the cells of the wing model to the investigated wing, we also transform the junction templates. So, we work with affine stable templates for deriving the optimal positions of the junctions. The two radii r_1 and r_2 , which are chosen by the bee expert, do not change much by this transformation, so we approximate r'_1 by r_1 and r'_2 by r_2 , respectively.

Considering each pixel in the uncertainty area of a junction $z \in U_{r_2}(p)$ as a candidate for the junction's position, we perform a template matching by determining the weighted correlation between the environment $E_{r_1}(z)$ and the transformed junction template. Thus, we shift the junction template such that its center maps to z. Since E and the template have the same size, we are able to compare them pixel-wise. We define the following three sets:

- C contains all pixels of E(z), which have been classified as points of cells in the wing,
- R contains all pixels of E(z), which are marked as points of cells in the shifted junction template,
- V contains all pixels of E(z), which are marked as points of veins in the shifted junction template.

Then, we evaluate two functions ρ and ω which are defined on E(z) by

$$\rho(x) := \begin{cases}
1 , \text{ if } x \in R \text{ and } x \in C \\
0 , \text{ if } x \notin R \text{ and } x \notin V \\
-1 , \text{ if } x \in V \text{ and } x \in C,
\end{cases}$$
(4)

$$\omega(x) := \begin{cases} 1 & \text{, if } x \in V \text{ and } x \notin C \\ 0 & \text{, else.} \end{cases}$$
(5)



Fig. 8. Selectable derived features: The bee expert has inserted the three junctions a, b and c into the genus model, e.g. the model for the honey bees. The positions of the three junctions in the current wing have been placed automatically during the feature extraction. Various fingerprint features could be derived from these junctions. In a training step for the classification, the bee expert may select different sets of the derived features. Here, one may choose between two sets of distances to perpendicular point x for subspecies identification of *Apis* bees, \overline{ax} and \overline{bx} , or \overline{ab} and \overline{cx} . The feature selection may vary between distinct bee genera.

A correspondence between the prediction of the junction template and the classification of the pixels as cells yields a positive response of $\rho(x)$. Since we do not have any information on the vein course, we can only consider wrongly classified pixels, where the template predicts a vein instead of a part of the cell. Then, $\rho(x)$ returns a negative value for these pixels. The response of $\rho(x)$ is zero, if no information of the pixel is given by the template.

We obtain the similarity between E and the junction template by

$$s(z) = \sum_{x \in E(z)} I(x)^2 \rho(x) + \overline{I}(x)^2 \omega(x), \tag{6}$$

where I(x) is the intensity value and $\overline{I}(x)$ is its inverted value. Thus, we combine the intensity information of the image with ρ - and ω -responses of the template matching.

2.4 Vein Detection

When the detection of the cells succeeded and the placing of the junctions is well done, the extraction of line-induced veins is relatively simple. As the detected cells and their shapes have impact on the positional precision of the junctions, they together also influence the peculiarity of the veins. So, the veins form the complementary space of the other two feature types. Each vein starts from a junction, runs along the cell borders, and it ends at a junction. Thus, the thinning approach, which was already proposed in [9], combined with the idea to connect adjacent junctions around a cell, leads to a highly reliable detection of the veins.

2.5 Selection of Reliable Fingerprint Features

The classification of bees is based on the fingerprint features, which we derive from the primary features, i.e. the extracted cells, veins and junctions. Our approach to feature selection is flexible to cope on different opinions and approaches on relevant feature sets for morphological identification within the community of taxonomists. Therefore, we are generally able to derive different fingerprints from the same set of primary morphological features. Fig. 8 illustrates such a case where we allow the bee expert to derive different feature sets concerning the honey bees *Apis*.



Fig. 9. Data quality inspection: result of the cell extraction of an image with a big pollen intersecting a vein. With help of the visualisation, errors like this can be found very easily.

Within the last years, ABIS proved to work successfully using the proposed fingerprint features as shown in Table 1. Furthermore, the fingerprints are confirmed by our recent results in subspecies identification.

3 Data Management and Visualization

All the wing images, the primary and derived features, the downsampled images, the models, identification results and georeferences are maintained with the help of the ABIS database. As an user-friendly front-end of ABIS and the ABIS-Database, the-AbisCommander, was developed for the efficient and multimedia-based support of project-related data management and quality inspection. With the help of AbisCommander, data can organized easily by drag'n'drop-operations in different projects, thereby providing the multiple usage of the same data by reference in different projects and roles (i.e. training, identification), cf. [10].

Visual inspection of input data as well as of all derived data (i.e. features and models) is important, particularly during the training of wing models. Figure 9 depicts an extracted deformed cell region caused by a big pollen intersecting one of the veins. Using this image for training of a wing model, will obviously corrupt the wing model and therefore decrease classification rates. Such errors can be found easily with help of the visualization. Generally, AbisCommander can visualize the derived results of each step in training and identification. Generally, the detection of errors will improve the quality and reliability of feature extraction and classification.

For the implementation of ABIS and AbisCommander, we paid attention to use open source software (Java, MySQL, Google Earth) only. This is important, to make ABIS achievable without great financial investments, which i.e. permits the use in locations of the third world, where the expert knowledge stored in ABIS is needed mostly.

4 Results, Conclusion, and Outlook

We will now come back to our taxonomical prominent identification project of subspecies, i.e. the taxonomical research project on the so-called *killer bees* introduced in section 1. We use the enhanced ABIS to compare the morphological profile of the Africanized honey bee population from 1965 with the corresponding profiles of the most important ancestors populations and the actual one. We work with six groups: *Apis mellifera mellifera*, *Apis mellifera ligustica*, *Apis mellifera carnica*, *Apis mellifera* *scutellata*, Africanized Bees Ribeirão Preto (1965), Africanized Bees Ribeirão Preto (2002).

The first three groups represent the most important European ancestor subspecies, while the fourth group represents the most important African ancestor subspecies. The fifth and sixth group represent Africanized honey bee populations from 1965 and 2002, respectively. While ABIS was employed successfully for species identification with about 5000 specimens, in this investigation in subspecies level about 100 individuals of each group were available. After the training ABIS reveals a recognition rate of about 94% (leave one out test), which is on the one hand "only" 94% due to the very close relationship of all six groups, but on the other hand sufficient and clearly better than results of other morphometric approaches.

Table 2. Left: confusion matrix of classification with ABIS. Right: Mahalanobis square distances between the cluster centroids in feature space. We considered the following subspecies of *Apis mellifera*: carnica (A.c.), ligustica (A.l.), mellifera (A.m.), scutellata (A.s.), and the Africanized honey bees from 1965 (A 65) and 2002 (A 02), resp.



Fig. 10. Dendrogram showing the Mahalanobis square distances between the two Africanized honey bee populations of 1965 and 2002 and the ancestor populations.

The tables in Tab. 2 show a more detailed analysis in form of a confusion matrix and the Mahalanobis square distances between the cluster centroids in feature space, resp. The very similar and very hardly separable subspecies of Apis m. carnica and Apis m. ligustica yield the least distance in feature space and the most misclassifications. On the one hand this missclassification of about 6% will motivate future work on ABIS. On the other hand the correct results on the other 94% of specimens allow a new taxonomical interpretation on the basis of the Mahalanobis distances as follows, cf. Tab. 2, and Fig. 10 and [1]:

- The African honey bee A.m. scutellata contributed most to the Africanized populations.
- A.m. mellifera is the European subspecies that contributed the most to both Africanized populations. This confirms results from allozymes,

- The "mellifera" genes were probably added to the Africanized profile only at the beginning and spread together with the population.
- The 2002 Africanized population at Ribeirão Preto acquired a *unique* morphometric profile.
- Since 1965 its distance to the A.m. scutellata and the European ancestors has increased.

The changes in wing venation indicate that the African honey bees continued to differentiate from 1965 to 2002 with the effect that the actual populations of the Africanized bees evolved a *unique* profile which will keep on changing. The fingerprint of the Africanized honey bee, which we derived by morphometric analysis of the bee's wings using ABIS, shows a significant difference to all the other introduced *Apis* subspecies in Brazil. Our results are partially in agreement with results obtained on genetic markers, e.g. [4] and are initiating further research using genetic markers to confirm our morphometric results.

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