AN EMPIRICAL STUDY OF SIGNIFICANT VARIABLES FOR TRADING STRATEGIES

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Abstract: Nowadays, stock market investment is governed by investment strategies. An investment strategy consists in following a fixed philosophy over a period of time, and it can have a scientific, statistical or merely heuristic base. No method currently exists which is capable of measuring how good an investment strategy is either objectively or realistically. Through the use of Artificial Intelligence and Data Mining tools we have studied the different investment strategies of an important Spanish management agency and extracted a series of significant characteristics to describe them. Our objective is to evaluate and compare investment strategies in order to be able to use those which produce a peak return in our investment.

1 INTRODUCTION

Stock market trading is one of the most popular forms of investment both on a corporate and individual level. Despite the vast number of studies which exist (Baba, 2002; Chapman, 1994; Liu, 1997; Skabar, 2001), the “stock exchange world” is so complex that there is still no universally accepted method for optimizing purchase management in terms of profits. We are faced with a very complex, and at times chaotic and unpredictable problem and one which also has a number of restrictions common to the real world (capital available, maximum share volume, liquidity, etc.) which make it yet more difficult. The objective of this work is to establish a procedure based on significant variables in order to characterise the results of a strategy’s behaviour according to a series of performance measures.

1.1 Stock Market Indexes

A stock market index corresponds to a statistical compound, usually a number, which attempts to reflect variations in the average value or profitability of the shares comprising it. Generally speaking, the shares which comprise the index have common characteristics: they belong to the same stock market, they have a similar stock market capitalization, or they belong to the same industry. These are usually used as the reference point for different portfolios, such as mutual funds.

The oldest index is the Dow Jones Industrial Average or the Dow Jones in short. This index was created to measure economic activity in the United States of America. It currently comprises 30 companies.

There are also other indexes throughout the world, and examples of these are the Ibex 35 in Spain, NIKKEI 225 in Japan, FTSE 100 in Great Britain, and CAC 40 in France.
1.2 Investment Strategies

An investment strategy is a behaviour routine devised by investors to enable them to make decisions in view of the different situations which may arise. This basically entails following a fixed strategy over a period of time, while in technical terms, it is a predefined set of rules to be applied.

Strategies are normally based on micro/macroeconomic data, on statistical indicators, or on technical analysis of the historical evolution of the share price. Investment strategies receive share prices in real time and include trading orders which are automatically executed in the market. Investors use investment strategies as tools to help in the decision-making process and to eliminate the emotional factor which an investment involves.

The strategy operates by using various parameters defined by the user and which have been adjusted from historical analysis and studies of the real market.

There are strategies which are ideal in certain circumstances but which fail where others triumph. Therefore, the choice of the ideal strategy to apply in the immediate unknown future is a very difficult task. In order to know the true potential of a strategy it is necessary to calibrate a multitude of factors which affect its behaviour as we shall see in the following sections.

A variety of procedures can also be found in the literature for evaluating and recommending strategies. Fung and Hsieh (Fung and Hsieh, 1997), for example, classify the strategies empirically according to their behaviour into the following 5 groups: “Systems / Trend-following”, “Systems / Opportunistic”, “Global / Macro”, “Value”, and “Distressed”. Schittenkopf’s work (Schittenkopf, 2000) is similar in some ways to that presented here in that it analyzes the relationship between volatility and profit variables, although it only analyses a single investment strategy on a single stock market index. Our work, on the other hand, attempts to be more general by analyzing a set of variables, for a series of strategies, on a wide range of stock market prices.

In the second section of this article, we will describe the strategies used, and how they may be optimized and evaluated. Section 3 analyzes the selected variables and explains why they were chosen. We will end the article with our conclusions and future lines of research.

2 METHODOLOGY

The first step in our study was to obtain a series of investment strategies and also the parameters for each strategy with their respective levels. For that we will use the records from Gaesco Bolsa.

Gaesco Bolsa S.A., one of the largest capital management companies in Spain, is constantly analysing automatic stock market investment strategies. We were given access to the 500 best strategies. While some come from their R&D department, others come from specialist journals (Stocks & Commodities, Trader) and others are proposed by their own clients. Each strategy is studied on a wide battery of scenarios by means of a demanding and exhaustive procedure which only a few strategies survive.

When the investment strategy is not based on human decisions, it can be simulated in time by what is known as an automatic system. A simulation is an execution of a strategy on a stock market index over a period of time.

In order to simplify our explanation as far as possible, we will present an example of a basic investment strategy, consisting of three behaviour rules:

* Entry rule: Purchase if the current share price exceeds the maximum of the last \( N \) days
* Exit rules: Sell if an \( X\% \) profit is obtained on the entry point
* Sell if a \( Y\% \) loss is obtained in relation to the entry point

The underlying philosophy behind this strategy tells us that the fact of exceeding the maximum (frequently called resistance) in the last \( N \) days is normally an indication of the start of an upward movement. We will sell after earning a certain amount of profit, although we will make sure that we do not lose more than a certain limit. This strategy has three adjustable parameters:

* \( N \): number of days which are considered in the calculation of the entry point
* \( X\% \): percentage of profits required before liquidating positions
* \( Y\% \): maximum percentage loss permitted

The code for the strategy implemented by means of Visual Basic to be used directly on the Visual Chart platform would be:

```vbnet
' ! Parameters
Dim N As Integer
Dim X As Double
Dim Y As Double
' ! Parameters !!
Public Sub OnCalculateBar(ByVal Bar As Long)
```
With APP
Dim Resistance As Double
Dim Benefit As Double
Dim Loss As Double

Resistance = .GetHighest(PriceHigh, N)
Buy AtStop, 1, Resistance

Benefit = .GetEntryPrice + (.GetEntryPrice * X / 100)
Loss = .GetEntryPrice - (.GetEntryPrice * Y / 100)
ExitLong AtLimit, 1, Benefit
ExitLong AtStop, 1, Loss

End With
End Sub

This strategy on the Nasdaq-100, establishing the values \( N=5, X=4, Y=3 \) as parameters, is shown in Figure 1. Each vertical bar determines the range of values covered during a day’s trading. The small horizontal bar on the left-hand side represents the initial value of the day and the small right-hand bar the final value. Two trades can be observed. A trade is defined as the fact that it starts when a value/good is purchased and ends when it is sold. The first trade is positive, since it is purchased at 9440 and sold at 9818, a result of +4%. The second trade, meanwhile, is negative since it is purchased at 9919 and sold at 9621, a result of -3%. The line which joins the entry point and the exit point of a trade is a visual tool which enables the strategy to be monitored.

Figure 1: Example of a strategy’s performance.

Taking the session closing price of each trading day as a reference, and knowing the entry and exit points of the investment strategy, it is possible to calculate a strategy’s daily percentage profit. This leads to a time series of daily profits which will be used in the following stages of our study.

2.1 Genetic Optimization of Strategies

A typical strategy has several adjustable parameters (permitted tolerance, reaction speed, profit, loss, etc.). Each parameter is defined with the following quadruple: [name, minimum value, maximum value, scale]. For example, our previously presented strategy comprises three parameters:

- [Days, 0, 250, 1]
- [Profit, 0, 250, 0.1]
- [Loss, 0, 100, 0.1]

The previous example would give us a set of 250,000,000 possible combinations of parameters, making impossible to analyse and evaluate all of them. We are interested in optimising a strategy’s parameters and searching for those which produce the best performance. For that we resort to a genetic algorithm (Holland, 1975; Goldberg, 1989) which enables us to obtain an acceptable combination in a feasible period of time. In the following section, we will briefly describe the genetic algorithm used.

2.1.1 Definition of the Individual

Each individual in the population corresponds to a certain combination of parameters and the associated chromosome is the binary codification of that combination. From each parameter’s range, it is possible to obtain the number of bits necessary for its codification. Certain ranges require preprocessing prior to codification:

1) If the range starts at a value other than 0, a value will be added or subtracted to move the start of the range to 0.
2) If the range includes decimal values, these will be multiplied by 10 until they become integer values.

In order to code a chromosome in our example strategy, 32 bits would therefore be necessary:
- [Days, 0, 250, 1] needs 8 bits.
- [Profit, 0, 100, 0.1] needs 12 bits.
- [Loss, 0, 100, 0.1] needs 12 bits.

The combination – 36, 1.5, 2.5 – will be coded: 00100100 000000001111 000000011001

2.1.2 Fitness Function of the Individual

Each individual in the population has an associated fitness value. For our problem, an individual’s fitness is the performance obtained when the strategy is applied on a certain index with the set of parameters represented in its chromosome. As a result of this simulation, a series of trades is obtained. The fitness is equal to the sum of the percentage profits of each trade once administration expenses and commissions have been deducted:

\[ f = \sum_{i=1}^{N} \left( \frac{O - I - \text{Commission}}{I} \right) \] (1)

where \( N \) is the total number of trades, \( I \) is the purchase price, and \( O \) is the sale price.

2.1.3 Crossover Operator

We will pair two individuals from the population in order to generate two new individuals, and we have
applied the crossover operator on 1 point (see Figure 2). This operator takes 2 parents from the population, pairs them and obtains 2 children. To do so, it randomly chooses a crossover point which divides the father’s and mother’s chromosomes into two halves. The first child is formed with the first half of the father and the second half of the mother, and the second child with the first half of the mother and the second half of the father.

Figure 2: One point crossover.

2.1.4 Mutation Operator

The chromosome is taken and is mutated by randomly changing some of its bits. It is necessary to bear in mind that after the cross or mutation operation, the descendants might not be valid population individuals, and it might therefore be necessary to repeat the process until the desired number of individuals is obtained.

2.2 Evaluation Method

Many investors design their investment strategies, optimise their parameters, and apply them to the real world, trusting the optimisation results. In the majority of cases, these strategies inevitably fail and fail dismally. The reason for this failure is very simple: they fail because while the strategy has learned to behave excellently in a specific period of time, it has not been able to generalise its parameters to act in a different period.

In our study, once the investment strategies have been calibrated, they are evaluated by means of a blind test on different periods of time to those used in optimisation in order to carry out as realistic a simulation as possible. The subsequent evaluation of the investment strategy will not take into account the results obtained in optimisation, but will only work with the test results.

An evaluation method has been followed based on the sliding window technique to carry out the set of optimisations-tests.

As genetic algorithms are probabilistic methods, the results of a simple execution can be inadequate. In order to avoid this as far as possible, the evaluation method is repeated 5 times, and a series of daily profits is obtained from each iteration. The final series used to calculate the variables will be the average of the 5 previous series.

The number of iterations of the genetic algorithm varies according to the strategy. As is logical, the strategies with the greatest number of parameters require a greater number of iterations. By default, the number of iterations is fixed to a tenth of the number of possible combinations.

Following the evaluation method described in this section, the 500 available strategies were evaluated on six stock market indexes: four European ones (CAC-40, DAX-30, IBEX-35 and EUREX-50) and two American ones (NASDAQ-100 and RUSSELL-1000). We obtained a database of 3000 entries on which we will extract the significant variables.

3 OBTAINING SIGNIFICANT VARIABLES

Once the strategy has been perfectly calibrated, we can proceed to extract the variables which characterise its behaviour. As we have already mentioned, the result of the previous tests is a set of 3000 daily profit time series. The profits are expressed in terms of percentages and perfectly match reality, i.e. they take into account the commissions of the different national stock markets and of their respective brokers, and also the slippages which occur when entering or exiting a trade.

Since almost every agent uses his/her own descriptive variables about a strategy’s behaviour, there might currently be thousands of operative variables. We, meanwhile, are looking for a series of significant variables which cover all aspects of a strategy’s behaviour and which describe it univocally.

After studying the semantics of hundreds of variables, we reached the conclusion that they could be grouped into four categories. The first and largest of these covers performance-related variables: absolute profit, percentage profit, annualised profits, Sharpe ratio, Sortino ratio, Treynor ratio, swing, capital asset pricing model (CAPM), etc. The second group contains the variables which, in some way, measure the risk, such as for example volatility, loss series, consistency, monthly risk, risk-adjusted return, risk-free return, alpha, systematic risk (beta), Jensen’s measure, etc. The third group consists of the variables associated with trading, Variables belonging to this group would be: activity, reliability, average profit per trade, average profit per positive trade, average profit per negative trade, etc. Finally, the fourth group comprises variables
which globally measure the quality of a strategy in comparison with the remaining strategies. Basically, this consists in ranking the strategies according to a series of criteria and allocating 5 stars to the best strategies, 4 stars to the next ones, and so on. The strategies with 1 star are those with the worst assessment.

We have detected that many variables are equivalent to each other or simply change scale or nomenclature. In collaboration with the experts, the authors have extracted a series of significant variables which describe how good the strategies are. After our initial selection, the most indicative and suitable variables are selected on the basis of the results of a survey carried out among experts. From each times series, a group of numerical variables is extracted which will help us to describe a strategy’s behaviour:

**Profit:** This annualised performance takes into account commissions and slippages:

$$G = \sum R_i / \# \text{years}$$  \hspace{1cm} (2)

where $R_i$ is a strategy’s performance in percentage terms.

**Volatility:** Volatility is the standard deviation of the change in the value of a financial instrument with a specific time horizon. It is frequently used to quantify the risk of the instrument during this time period. Volatility is expressed in annualised terms. The annualised volatility $\sigma$ is proportional to the standard deviation $\sigma_{SD}$ of the returns of the instrument divided by the square root of the time period of the returns:

$$\sigma = \sigma_{SD} / \sqrt{P}$$  \hspace{1cm} (3)

where $P$ is the period of the returns in years.

**Loss series (Drawdown):** this is the greatest loss sequence, or rather, the greatest drop between the peak of accumulated profit and the lowest point. Measurement begins when the fall starts and ends when a new maximum is reached, since the lowest point is not known until a new maximum is reached. More formally, if $X(t)$ gives the accumulated profit at a moment in time $t$, the loss series at a moment $T$ would be:

$$X(0) = 0, t \geq 0$$

$$DD = Min[0, X(t) - Max_{t=0,T}[X(t)]]$$  \hspace{1cm} (4)

**Sharpe ratio:** the Sharpe ratio is a measure of risk-adjusted performance of an investment asset, or a trading strategy, and is defined as:

$$S = G / \sigma$$  \hspace{1cm} (5)

where $G$ is the strategy return and $\sigma$ is the volatility of the strategy return. The Sharpe ratio is used to characterize how well the return of an asset compensates the investor for the risk taken.

**Potential:** this is a measurement of the performance in relation to the maximum loss series:

$$P = G / DD$$  \hspace{1cm} (6)

**Consistency:** in general terms, the consistency refers to the property of maintaining the same form over time. In our case in particular, it indicates the frequency of negative results over time:

$$C = \sum_{R_i R_j < 0} \frac{R_i}{\# R} + SD(R_i R_j < 0)$$  \hspace{1cm} (7)

where $SD$ is the standard deviation of the negative return values.

**Reliability:** this is the number of winning trades expressed as a percentage of the total number of trades:

$$F = \frac{\text{winning trades}}{\text{total trades}} \times 100$$  \hspace{1cm} (8)

**E01:** one-year stars following Standard & Poors’ method. By dividing the strategy’s average relative performance by the volatility of its relative performance, we are measuring not only its ability to outperform its peers but also to do so in a consistent way; the higher the ratio, the greater the strategy’s ability to outperform its peers consistently.

$$RR = \frac{\text{relative return}}{\text{relative volatility}}$$  \hspace{1cm} (9)

Let us suppose we have 100 strategies, then the strategy stars will be:

- 5 stars: top 10%, 10 strategies
- 4 stars: top 11-30%, 20 strategies
- 3 stars: top 31-50%, 20 strategies
- 2 stars: next 25%, 25 strategies
- 1 star: bottom 25%, 25 strategies.

**E04:** we follow the same procedure as the one-year stars (E01), but considering four years.

**Number of Trades (Activity):** this is the number of entries-exits per day.

$$A = \frac{\# \text{trades}}{\# \text{days}}$$  \hspace{1cm} (10)
4 CONCLUSIONS AND FUTURE WORK

One interesting conclusion was obtained from the optimization process, and this is that the most elaborate and complex strategies, and therefore those with the greatest number of parameters, obtained excellent values in optimization but disastrous ones in the test. On the other hand, while more basic and simpler strategies with a lower number of parameters did not perform particularly well in optimization they did in tests. This is due to the fact that very complex strategies are capable of perfectly adjusting to the particular characteristics of the optimization period, but overlearn and do not know how to act when the conditions change. However, simpler strategies abstract and generalize better and their behaviour is similar in both optimization and test periods.

The extracted data are extremely valuable since they can be used to carry out a large number of scientific studies. A first study would consist in representing the previous data in a data warehouse and applying different data mining techniques in order to extract patterns between the different variables. Taking into account that the values of the variables can easily be transformed into fuzzy variables by means of linguistic labels, it would be possible to carry out a similar study to the previous one by using a fuzzy data warehouse capable of extracting fuzzy association rules (Delgado, 2007). Similarly, it would be advisable to find the results with the greatest significant interest (Shekar, 2004).

The portfolio selection problem (Schlottmann 2004) can also be studied by using the methodology in this work. This problem consists in looking for the combination of strategies which, by acting jointly, increase profits and reduce risk. This is a typical multiobjective optimisation problem. The data can also be studied with clustering techniques which search for the groupings between strategies or variables.

It would also be interesting to devise an expert system for stock market investment, and one possibility might be to achieve an expert assessment of each strategy. By applying neural networks or some other artificial intelligence technique, expert knowledge could then be abstracted and represented for implementation on the expert system’s knowledge base.

The information obtained is subject to changes according to time. An analysis could be carried out to search for values which have undergone changes, thereby obtaining new knowledge and eliminating part of the previous knowledge (Chen, 2005).

REFERENCES


