REAL-TIME DEFORMABLE OBJECTS FOR COLLABORATIVE VIRTUAL ENVIRONMENTS

Selcuk Sumengen, Mustafa Tolga Eren
Faculty of Engineering and Natural Sciences, Sabanci University, Tuzla, Istanbul, Turkey

Serhat Yesilyurt, Selim Balcisoy
Faculty of Engineering and Natural Sciences, Sabanci University, Tuzla, Istanbul, Turkey

Keywords: Deformable objects, real-time simulation, cloth modelling, Distributed and Network Virtual Environments, Collaborative Virtual Environments.

Abstract: This paper presents a method for physical simulation of deformable closed surfaces over a network, which is suitable for realistic interactions between users and objects in a collaborative virtual environment (CVE). CVE’s are being extensively used for training, design and gaming for several years. To demonstrate a deformable object in a CVE, we employ a real-time physical simulation of a uniform-tension-membrane, based on linear finite-element-discretization of the surface yielding a sparse linear system of equations, which is solved using the Runge-Kutta Fehlberg method. The proposed method introduces an architecture that distributes the computational load of physical simulation between each participant. Our approach requires a uniform-mesh representation of the simulated structure; therefore we designed and implemented a re-meshing algorithm that converts irregularly triangulated genus zero surfaces into a uniform triangular mesh with regular connectivity. The strength of our approach comes from the subdivision methodology that enables to use multi-resolution surfaces for graphical representation, physical simulation, and network transmission, without compromising simulation accuracy and visual quality.

1 INTRODUCTION

Collaborative Virtual Environments (CVE)’s are being extensively used for training, design and gaming for several years. They enable participants to get immersed into a Virtual Environment where they can perform a task or experience a story together. In most use cases such as gaming and education, current CVE’s are sufficient to address user expectations related to visual realism, animations and networking. However, CVE’s also involve substantial amount of interaction between the users and the objects in synthetic worlds, which should be visually appealing and physically realistic as well. Current CVE’s are mostly limited to avatar-avatar interaction or the object interactions are animated using offline techniques and they are commonly hard-coded into the application. Another recent approach is to use rigid body simulations together with inverse kinematics engines (Jorissen and Maarten Wijnants, 2005). Real-time physical simulation of deformable bodies in CVE’s will enable accurate replication of interaction with real world deformable objects and open a vast array of possible applications. One example is medical and engineering applications which require accurate simulations in real-time.

In this paper, we are presenting a method for deformations on closed surfaces over a peer-to-peer network architecture (Figure 1.1).
2 RELATED WORK

2.1 Collaborative and Distributed Network Virtual Environments

DIVE (Hagsand, 1996) is one of the first Distributed Virtual Environments that allows participants to collaborate in a 3D virtual world which facilitates audio, video and text transmission for communication and interaction within the VE. Similarly, NPSNET (Macedonia, Zyda et al., 1994) is designed for military training and simulation for networked environments using Distributed Interactive Simulation Standard (DIS). MASSIVE is a VR conferencing system especially used for public participation and performance (Benford, Greenhalgh et al., 2001). VLNET allows multiple users represented by 3D virtual human actors to interact with each other and enables third parties to view the shared virtual environment from the Web using VRML (Thalmann, Babski et al., 1997).

There are only a few systems that in particularly deal with the significance of physical simulation in collaborative virtual environments. A recent work by Jorissen (Jorissen and Maarten Wijnants, 2005), gives a detailed survey on state of the art of dynamic interactions and physical simulations in CVE’s. Jorissen et al. introduces a collaborative virtual environment, where the object-object interaction is allowed in addition to avatar-object and avatar-avatar interactions using a non-commercial physics engine.

There are few attempts to introduce deformable objects into CVE’s: Dequidt et al. (Dequidt, Grisoni et al., 2005) propose a system based on ghost objects to handle network latency. Ghost objects are associated to objects manipulated over the network and introduced into the client side to perform physical simulations asynchronously at each user.

Collaborative Haptics Environments are also introduced to handle surgical training and simulations (Xiaojun, Bogsanyi et al., 2003). As haptic rendering must be performed at simulation rates higher than 1 KHz, most systems require dedicated hardware running on real-time operating systems (Zhou, Shen et al., 2004). Goncharenko et al. (Goncharenko, Svinin et al., 2004) report a distributed and collaborative haptic visualization of a 1-DOF crank model only possible on Intranets. They used a dedicated haptic communication library to satisfy real-time communication requirements of haptic rendering on a client-server architecture connected through Ethernet.

2.2 Deformable Objects

Visualization of object deformations is an important research area for over two decades with a large span of applications such as cloth, tissue modeling and virtual surgery. One set of approaches on the visualization of deformable models is non-physical and purely geometric techniques, most of which is classified as Free-Form-Deformations (Sederberg and Parry, 1986). Physics based approaches gained a popular attention by enabling cloth animations (Terzopoulos, Platt et al., 1987). Cloth animation is an extensive research area covering wide range of issues from physical simulation to collision detection (Volino and Magnenat-Thalmann, 2006). Early examples of cloth animation using a linear model based on energy minimization, and continuing approaches using explicit integration schemes, are suffering from stability issues for large body deformations. Baraff and Witkin (Baraff and Witkin, 1998), introduced an implicit integration scheme for stable simulations using large time steps.

On the other hand, real-time simulation of deformable models is an other challenge, and linear mass-spring models introduced at first (Desbrun, Peter Schröder et al., 1999). As an alternative, Boundary Element Method is introduced, which is inspired by Finite Element Method (FEM), however, considers only the surface of the model (James and Pai, 1999). Non-linear FEMs are not suitable for real-time simulations since they are computationally intensive, so deformable object simulations in virtual environments continued to use improved mass-spring models (Kang and Cho, 2002). Also, pre-computed models for real-time dynamic deformations are considered (Nikitin, Nikitina et al., 2002). Since medical applications require real-time and accurate simulations some approaches used FEM to parameterize the mass-spring model to improve accuracy (Choi, Sun et al., 2004).

3 NETWORK DEFORMABLE OBJECTS

Our method applies a collaborative deformation on a linear membrane model over network, which can be used for simulation of deformable objects (tissue, organ, cloth) in CVEs.

3.1 Geometric Model

The proposed approach requires a uniform representation of the simulated structure. Restriction
on the genus of the model allows us to construct a regular 2D grid that corresponds to the surface of the model.

The surface of any convex polyhedron is homeomorphic to a sphere and has Euler characteristic of two. Homeomorphic spaces are identical from the viewpoint of the topology therefore genus zero surfaces preserve their topological properties under spherical parameterization and can be mapped onto a convex regular polyhedron.

### 3.1.1 Mesh Representation

We have chosen Tetrahedron as the Domain for our mesh representation, since it has four equilateral triangular faces that can be represented as a 2D grid having \((2^n + 1) \times (2^{n+1} + 1)\) nodes where, \(n\) is positive integer determining the number of vertices and will be referred as detail level (Figure 3.1).

![Figure 3.1: 2D Grid representation of a tetrahedron.](image)

### 3.1.2 Mesh Generation

We propose an algorithm that converts irregularly triangulated genus zero surfaces into a uniform mesh with regular connectivity. Previous approach for constructing regular meshes with fixed and simple topology by Hoppe (Praun and Hoppe, 2003), generates a spherical parameterization of the surface and the domain. Surface, projected on the sphere, mapped onto the domain, and unfolded to generate the geometry image. We apply a similar procedure, but we introduce a different technique for spherical parameterization and model re-meshing. It allows adjusting the tradeoff between face area uniformity of the generated mesh, and preserving the accuracy with the original mesh.

Given a triangle mesh \(M\), the problem of spherical parameterization is to form a continuous invertible map \(\varphi: S \rightarrow M\) from the unit sphere to the mesh (Praun and Hoppe, 2003). Spherical parameterization of both a regular tetrahedral domain \(D\) and an irregular input mesh \(M\) are necessary to generate Sphere to Mesh (\(S \rightarrow M\)) and Sphere to Domain (\(S \rightarrow D\)) mappings that will allow us to perform Mesh to Sphere and Sphere to Domain (\(M \rightarrow S \rightarrow D\)) transformation.

Any convex polyhedron can easily be projected onto a unit sphere (Figure 3.2) by switching to spherical coordinate system \((\Theta, \Phi, r)\) and setting a unit radius for all vertices (Gnomonic Projection), however translation between each mesh triangle and spherical triangle might introduce a certain amount of distortion.

![Figure 3.2: Gnomonic Projection of a tetrahedron.](image)

Previous approaches define a stretch norm to measure the stretch efficiency and conclude that minimizing the stretch norm is a non-linear optimization problem (Sander, Snyder et al., 2001; Praun and Hoppe, 2003). We attack this problem by a modification of a well known technique used for graph drawing. Graph drawing using force directed placement methods, which are also called spring-embedders, distributes vertices evenly in the frame and minimize edge crossings while favoring uniformity of the edge lengths (Fruchterman and Reingold, 1991). Since we implemented a deformable physics engine that can handle mass spring systems efficiently, we introduce a variant of spring-embedders for stretch optimization.

A spring-embedder model is generated from the gnomonic projection of the domain. Every vertex has a constant mass, and springs are introduced between neighboring vertices. An external force field (3.1) is applied from the center of the domain that limits displacements of vertices on the unit sphere.

Springs between the vertices tend to preserve initial edge lengths and resist movements that change the topology; however we need to establish a tension on these springs to perform stretch optimization.

We scale down the positions of the vertices that are projected onto unit sphere (3.2), and an external force which is applied continuously expands the vertices onto the unit sphere again while producing a tension on the springs. Stiffness parameters are
updated continuously to achieve an area uniform tessellation over the unit sphere (Figure 3.3).

![Figure 3.3: (a) Gnomonic Projection of Tetrahedron. (b) Stretched Gnomonic Projection of Tetrahedron.](image)

\[
x_i = \sum_{j=1}^{\text{nNeighbors}_i} \frac{x_j}{\text{nNeighbors}_i}, \quad \forall i, \ 0 \leq i \leq \text{nNodes},
\]

(3.3)

Our proposed force model is a feasible stretch optimization technique for domain to sphere mapping; however, it is insufficient for mesh to sphere mappings where the projection of non-convex polyhedron into a unit sphere results in edge crossings and does not preserve initial surface topology. We use a vertex displacement procedure (3.3) which is similar to the relaxation method of previous spherical parameterization approaches (Alexa, 2002) to overcome this problem (Figure 3.4).

![Figure 3.4: (a) Irregular Input Mesh. (b) Stretched Gnomonic Projection of Input Mesh.](image)

3.1.3 Model Re-meshing

Combining the spherical mappings mesh to sphere (M→S) and sphere to domain (S→D) to derive mesh to domain mapping (M→D), requires intersection of the sets on the sphere. However, transformed vertex coordinates of the mesh and domain might not intersect on the sphere, and vertices of the domain might fall inside of a mesh facet. For each vertex of the domain, intersecting face of the parameterized mesh should be found out and 3D coordinates of domain vertex should be computed by interpolating the vertices of the intersecting face (Figure 3.5).

Since computing the interpolated coordinates is costly, we introduce a fast method taking advantage of recent advances in graphics hardware using the GPU and frame buffer objects.

![Figure 3.5: Intersecting Spherical Projections of Tetrahedral Domain and Input Mesh.](image)

Using OpenGL and programmable shaders (GLSL), we render the faces of the parameterized mesh onto the frame buffer using the two dimensional spherical coordinates (\(\Theta\) and \(\Phi\)) of the transformed vertices. Initial Cartesian coordinates (x, y, and z) of the parameterized mesh vertices are attached to color attributes (r, g, and b) at the vertex shader, and inside of each face is filled with the interpolated Cartesian coordinates at the fragment level (Figure 3.6). Rendered image is then fetched from the frame buffer as a 2D texture and used like a lookup table to generate 3D coordinates of the domain vertices.

![Figure 3.6: Spherical projection of input mesh is, (a) rendered as 3D wireframe, (b) 3D colored surface, (c) 2D colored surface, and (d) 2D colored surface, where the original positions of vertices are used as color components.](image)

Figure 3.7: Final comparison of (a) the input mesh with 1444 vertices, and (b) the resulting regular mesh with 8385 vertices.
3.1.4 Subdivision Scheme using Convolution Kernels

Subdivision methodology is appropriate for our approach since it allows multi-resolution representation of a surface and fast switching between detail levels. It also favors numerical stability, so it is highly suitable for physical simulation of deformations using finite element and finite difference methods.

We used a variant of butterfly subdivision scheme (Zorin, Peter Schröder et al., 1996) that generates a $C^1$ smooth triangular mesh. Modified Butterfly Scheme is an interpolating subdivision scheme, where the original vertices (control points) are also the vertices of the refined surface and surface is interpolating to a limit surface. This behavior makes it possible to use surfaces with different resolutions for graphical representation, physical simulation, and network transmission, without compromising the integrity of simulation accuracy and the rendered image.

Figure 3.8: Modified 2D Grid Structure.

Given that we have a regular mesh representation as a grid structure, we introduce some modifications (Figure 3.8) to apply a fast and robust refinement strategy using modified butterfly scheme. Taking advantage of having a regular domain, we have no boundary or crease vertices, but there are four extraordinary vertices of valances three on the corners of the tetrahedral domain. However, if we duplicate the edges of these vertices, they can be treated as regular vertices. Since the duplicate edges are symmetric to existing edges, resulting odd vertices will have same values. This modification allows us to use the mask for interior odd vertices with regular neighbors for all the grid nodes. We also introduce offsets to 2D grid representation. Offsets are the copies of grid nodes, assuring existing neighboring properties and they are kept updated before the convolution process.

Figure 3.9: (a) Modified 2D Grid Structure. (b) Application of mask for interior odd vertices with regular neighbors. (c) Equivalent convolution kernel. (d) Three convolution kernels generated for three edges.

Having a 2D grid representation and a mask with constant coefficients, odd vertices can be generated by consecutive convolutions with three kernels created by rotating the subdivision mask three times (Figure 3.9).

Figure 3.10: Comparison of resulting mesh refined by subdivision and rendered at different level of details: (a) 8335 vertices, (b) 33153 vertices, (c) 131841 vertices.

Necessity for the grid offsets arises from the application of the mask to the grid boundaries, and modified subdivision scheme requires first neighbors of even vertices that are next to generated vertex. Offset width does not change according to the grid dimensions and time required for the update of the offsets is negligible. After the convolution of the $n$th level subdivision surface three times, resulting 2D grids are merged to generate $(2^{n+1} + 1) \times (2^{n+2} + 1)$ nodes (Figure 3.10).

3.2 Physical Model

Physical simulation of deformable objects is an extended research area, where several methods are
present, varying from fast and simple methods favoring speed and scalability, to much more complex methods favoring accuracy and stability. Linear methods such as mass-spring models for dynamic deformations are suitable for use in real-time applications; however, they are not capable of handling large deformations and small time steps which are required to guarantee stability (Desbrun, Peter Schröder et al., 1999; Georgii and Westermann, 2005). On the other hand, non-linear models incorporating large viscoelastic and plastic deformations are computationally intensive (Reddy, 2004), and despite their physical accuracy, real-time simulation of large deformations is only possible with massively parallel computers.

For the demonstration of the deformable object on a collaborative virtual environment, we use a real-time physical simulation of a uniform-tension-membrane, based on linear finite-elements. We introduced finite element discretization to form the global stiffness matrix, which is updated frequently to handle large deformations with enhanced accuracy and we used Runge-Kutta-Fehlberg method for integration to achieve bigger time steps and improved stability (Baraff and Witkin, 2003).

### 3.2.1 Linear Finite-Element Model

Application of the finite-element method for the wave equation (Bathe and Bathe, 1996; Reddy, 2004), describing the time-dependent small deformations of a uniform-tension membrane results in a standard system of equations (Hughes, 1987):

\[
M \ddot{x} = -B \dot{x} - Kx + f_{\text{external}} \tag{3.4}
\]

where, \( x \) is the normal deformation of each node, \( M \) is the diagonal mass matrix, \( f_{\text{external}} \) is the external force vector due to user interactions, \( B \) is the diagonal damping matrix, and \( K \) is the stiffness matrix. In our implementation, we separate normal deformation and the velocity of each node to improve the stability of the Runge-Kutta method used to solve the linear system. Namely, we have

\[
\dot{x} = \dot{\psi} \tag{3.5}
\]

and the resulting equation of motion:

\[
M \ddot{\psi} = -B \dot{\psi} - Kx + f_{\text{external}} \tag{3.6}
\]

The finite element method works well with an arbitrary triangulation of a surface as well as proposed regular grid structure. In our implementation we apply the damping matrix directly on the nodal velocities, so as to model a permeable membrane placed in a liquid. In some standard formulations, the damping is applied to relative nodal velocities. The two yields in similar solutions, however our implementation results in simpler sparse structures and faster simulation times via improved stability of nodal damping.

### 3.3 Network Model

There are several network topologies used for Distributed Virtual Environments. Our approach is implemented with a peer-to-peer architecture which is operational on local and wide area networks. User Datagram Protocol (UDP) is used for communication, since speed and bandwidth requirements are essential for a real time simulation and have a greater priority over packet integrity.

Peers can run on different computers on the network or can be started in the same application as separate threads. We don’t introduce any dedicated servers, and peer nodes are functioning as both clients and servers. Every peer has a listening port and address for incoming connection requests. The peer which started to run CVE is required to act as a master for coordinating partitioning of the simulation. Partitioning occurs after sending a request by a participant which selects a face on the mesh and identifies it as the point of interest where the peer is going to introduce an external force. Participants can enter the CVE also as a viewer, where they do not interact with the model, but can observe the simulation.

### 3.4 Partitioning and Synchronization of Physical and Geometric Models through the Network

In our approach, partitioning the deformable object and synchronizing among peers is an important issue, since it enables collaboration in the virtual environments with distributed computational load. For an efficient communication and separation, we introduce a quad tree based data structure over 2D grid structure proposed on the previous sections.

![Sample tree structure for tetrahedral domain having depth of two.](image)

Quad-tree structure (Figure 3.11) is a natural formation for the tetrahedral domain, and can be divided hierarchically. Tree nodes are transferred efficiently via network since a tree node contains a
range identifier which is actually the combination of upper left and lower right node index numbers, and state information of corresponding region as a 2D array. Minimum depth level for the tree can be adjusted to keep the packaged tree node size smaller than the maximum packet size allowed by the network protocol.

Domain divisions are designed upon a quad tree based structure in the figure (Figure 3.11). While dividing the domain into sub-domains, equivalence of the number of shared grid nodes is an important criterion. However, keeping the domain boundaries shorter for an accurate synchronization of the physical simulation is essential, and keeping the fragmentation minimal for efficient network transmission is also important.

At the beginning of the simulation, each client starts to simulate the whole domain independently. When a connection invoked, domain is partitioned according to the points of interest where the forces are applied by the clients. Nodes at the domain boundaries are treated as boundary conditions, and the dynamical simulation of the local domain performed consequently at the each client.

4 RESULTS

Our graphical sub-system can efficiently handle very large meshes, taking advantage of regular-mesh and subdivision methodology as presented in the previous chapters (Figure 4.1). Our system renders meshes using the Phong shading model at interactive frame rates (25 fps) with resolution up to 100K polygons on an AMD Opteron 2.6 GHz PC equipped with NVIDIA Quadro FX4500 GPU. We implemented Phong shading model on the GPU. Vertex positions are uploaded to texture memory and vertex normals are computed on the fly using texture lookups.

The proposed network communication model can handle synchronous simulation among two peers of a surface up to 10K vertices over the local area network. This level has a bandwidth requirement of 20 M Bits per second without any compression.

We also tested the performance of the system by comparing computational load and number of simulated nodes. Our deformation engine can handle multi-resolution meshes up to 30K nodes, and maintains interactivity at less than %30 CPU utilization. Partitioning the domain between clients reduces computational load by 45% on the average, and increases the running speed by a factor of 1.8, depending on the partitioning ratio.

Figure 4.1: (a) One peer and (b) two-peers collaborative network deformation of a sample model having a regular mesh structure.

5 CONCLUSION

We have proposed a new technique for deformable body simulations in the field of collaborative virtual environments and introduced several improvements over the methods we adopted. We found that adaptive refinement and multilevel meshing strategies are promising research domains that can be further exploited for increased network efficiency and better physical accuracy for CVE’s.

Furthermore, we showed that the partitioning of physical simulation domain has a considerable effect on performance, and makes real-time simulation possible in scenarios where only one peer is incapable of handling the computational load.

As future work, we consider on the fly compression which might significantly reduce the bandwidth requirement but can degrade overall performance because of the additional computational cost. Optimization of the system for the Internet is out of the scope of this paper, but it is safe to predict that the network lag on public networks will have an impact on performance. Our method needs to be optimized for the Internet, and tested over large physical distances to overcome possible negative network effects.

REFERENCES


