SCALABLE UPDATE PROPAGATION IN PARTIALLY REPLICATED, DISCONNECTED CLIENT SERVER DATABASES

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Abstract: Modern databases allow mobile clients, that subscribe to replicated data, to process the replica forgoing continuous connectivity, and to receive the updates while connected to the server. Based on the overlap in client interest pattern, the server can do update processing for manageable number of data-groups instead of per-client basis, and hence decouple the update processing cost from the client population. In this paper, we propose an efficient update propagation method that can be applied to a relational database system irrespective of its inherent data organization. We present computationally efficient algorithms for group design and maintenance based on a heuristic function. We provide experimental results that demonstrate that our approach achieves a significant increase in overall scalability over the client-centric approach.

1 INTRODUCTION

In Intermittently Connected Database (ICDB) systems, clients maintain a replica of some subsets of the global database schema in their local databases to improve performance and availability, and reduce cost. Updates in the local database are logged and propagated to the server upon resumption of the connection which is intermittent in nature. The server keeps track of updates in the primary copy of the global database and disseminates the updates relevant to the clients based on the knowledge of their subscriptions. Typically, the server propagates the updates to clients on an individual basis: for each client, the server scans through the whole log of updates and selects updates relevant to the client. In this way, the server propagates a “client specific” set of updates. This client-centric approach is simple and straightforward but expensive in terms of server processing, as the server load is on the order of the number of clients. So, this approach limits the scalability of the system.

In (Yee et al., 2001), the authors propose a data-centric approach that, based on client interests, organizes updates into limited and controllable number of groups shared by the clients, and allows the server to manage update processing, irrespective of the number of clients, only for those groups. Instead of a customized set of updates, each user receives the updates for the relevant groups. This decoupling of the client population from server workload in propagating updates leads to better server scalability (Mahajan et al., 1998) (Yee et al., 2001).

The data-centric approach in (Yee et al., 2001) is based on a database management system (DBMS) architecture, where the database is organized as logical/physical fragments (Badrinath, 1999). Organizing a database as logical/physical fragments by partitioning the server data set requires additional features in traditional DBMS to manipulate and realize fragments. In this approach, clients subscribe to a subset of fragments, and groups are formed according to the overlap in the client interest pattern. The grouping problem, that can be modelled as an NP-complete mathematical programming problem, is very complex which makes the heuristic algorithm in (Yee et al., 2001) computationally inefficient and, hence, time consuming. And, mapping new client subscriptions to datagroups, being an NP-complete weighted set covering problem, is also computationally inefficient. Hence, activities related to maintaining datagroups—redesign and datagroup mapping—affect the scalability of the system.

Moreover, recognizing or realizing numerous fragments, and specifying interest as a subset of fragments, appear cumbersome. It is convenient to specify the interest using query in the way similar to specifying a view. Such a query restricts the data volume using a few predicates over one or more selected attributes. Also, the previous approach (i.e., specifying interest as a subset of fragments) doesn’t utilize the locality of client data access while forming datagroups: the fragments relevant to a particular
client might be contiguous logically (based on some attributes); hence, they are not always random.

In this paper, we propose an update propagation method forgoing the assumption about data organization of the server database. In forming datagroups, we exploit the locality of client data access. A client specifies its interest by imposing bound on the Replica Selection (RS) Attribute(s). We divide the range of each RS-attribute into equal length consecutive fragments, and associate these fragments with the nodes of a path graph in order. As the subscription of a user maps to the consecutive nodes, the problem of forming groups reduces to the problem of cutting each path graph (one for each RS-attribute) independently along few properly selected edges. This splitting of every path graph creates several connected components, that specify the regions of datagroups. This technique reduces the complexity of forming datagroups, and maintaining groups with the changes in ICDB configuration; it eliminates the computational overhead of mapping new client subscriptions to datagroups: for fixed number of RS-attributes, this mapping can be done in constant time. Also, motivated by the above example, we allow a portion of client-centric processing to eliminate redundant updates for the clients. To eliminate unnecessary updates and hence to save disk space, we introduce the mechanism of pruning update logs. All these simplifications enhances the scalability of the system.

The rest of the paper is organized as follows: Section 2 describes related work in this area. Section 3 outlines the model. Section 4 presents the mechanism for developing and maintaining datagroups in case of single attribute replication. Section 5, based on grid structure, provides a solution for the generalized case. Section 6 compares our work with intuitive grouping methods, and demonstrate that our approach provides significantly greater scalability in client population. Section 7 provides critical assessment. Finally, section 8 concludes the paper and outlines possible future work.

2 PREVIOUS WORK

Replication in distributed database system is studied in (Diener et al., 1985) (Demers et al., 1994) (Pacitti et al., 1999) (Pacitti and Simon, 2000). In the BAYOU system (Demers et al., 1994), that uses an epidemic (Demers et al., 1987) approach to maintain replica consistency, the whole database is replicated among multiple servers that remain disconnected from each other most of the time. Any read/write operation on the database, by the clients, is performed on any available server. Using a peer-to-peer anti-entropy protocol, that allows update propagation among servers that are able to communicate, the servers propagate updates among copies of the database (Peterson et al., 1997). Anti-entropy ensures that in the absence of new updates all the replicas of the database will converge to identical state provided the servers don’t remain disconnected forever.

In (Rabinovich et al., 1996), the authors, addressing the scalability issues in epidemic replicated databases—to be specific, endeavouring to eliminate performance degradation due to increase in database size, propose an epidemic protocol of update propagation that imposes overhead that is linear in the number of data items to be copied during update propagation.

Update propagation methods proposed in (Daudjee and Salem, 2004; Pacitti and Simon, 2000; Pacitti et al., 1999) consider the freshness of data, and ensure the serializable execution of transactions. However, the techniques assumes persistent connections among the sites holding the primary and secondary copies of a database. So, these approaches are not suitable for ICDB where the server should store updates and propagate these updates to the clients upon resumption of the connections.

ICDB is an instance of distributed computing system where clients are mobile and commonly suffer long period of disconnection with the server. Due to these properties, traditional concurrency control protocols are not applicable in this system. To help ensure the ACID properties of transactions (Bernstein et al., 1987), traditional distributed database systems use the two-phase-commit protocol which is communication intensive and requires all participants to be simultaneously connected; therefore this protocol is impractical in a disconnected environment. To ameliorate this problem, researchers have proposed replicating data among the clients and allowing independent operation on the replicas (Breitbart and Korth, 1997). Two-tier replication model, proposed in (Gray et al., 1996), though relaxes the ACID properties, provides high availability, reduces the possibility of deadlock, reduces the need for continuous communication with the server, and allows mobility resistant to network outage. In (Yee et al., 2001), the authors propose an update propagation algorithm to make the server workload in update propagation independent of client population.

The architecture and goal of CODA file system (Satyanarayanan et al., 1993) is similar to those of ICDB: it allows clients to form replicas while disconnected, and re-integrate the updates while connected to the server. However, contrary to ICDB systems, latency in this re-integration is not observed to be a limiting factor in CODA.

Update propagation in ICDB systems bears similarity with view maintenance (Gupta and Mumick, 1995). The difference is that in view maintenance the resultant view should match the expected query as
Figure 1: The Update Manager maintains the update log and distributes updates to the intermittently connected clients that maintain a replica of the global database.

closely as possible with disk space consumption being the cost factor, whereas in group design, the updates for each client should be generated as quickly as possible (Yee et al., 2001). Moreover, modification of a view by using only view is not always possible.

3 SYSTEM MODEL

The ICDB architecture consists of a database server, a network and several clients. The global database is stored in the database server. Closely tied with the DBMS is the update manager which can either be a module in a server incorporated with the DBMS, or be a process running in a stand-alone update server. This Update Manager stores updates in the database, keeps track of the client subscriptions, and propagates updates to the clients when they are connected to the server via a network (Figure 1). The client is composed of a client update agent, and a local DBMS. The update agent receives updates from the server and applies these updates to the replica stored in the local DBMS.

The update manager stores updates separately for all datagroups. Updates in a group are removed as soon as all the clients subscribing to that group connect to the server and, therefore receive the updates. The time elapsed between successive update removal of a group is denoted as pruning interval \( T \). This pruning interval of a group is dependent on the frequency of connection resumption by the clients relevant to that group. For the sake of simplicity of our analysis, we assume that this interval is fixed, and same for all groups. Designing datagroups without this assumption is straightforward, but complicates the cost equations.

We don’t make any assumption about the transaction processing protocol that maintains replica consistency. To maintain replica consistency transaction processing protocols based on precedence graph (Davidson, 1984) can be applied in this environment.

In our model, the representation of datagroup, and fragment (in single attribute replication) or grid-block (in multi attribute replication) is simple; hence, this information can be stored in main memory. As no redundant update is sent to the client via wireless link, the update transmission time play no role in the datagroup formation. This implies, we don’t make any traded between server side delay (i.e., disk I/O) and transmission delay. However, this “scanning” demands CPU time. But, as the scan time is quite insignificant compared to disk I/O time, we eliminate this scan time from our cost model.

Each client specifies its desired data, and hence create replica, using attribute(s) of a relation. We identify such attribute as Replica Selection (RS)-attribute of the relation. For example, consider schema (Badrinath, 1999):

\[
\text{SUPPLY}(\text{SNUM}, \text{PNUM}, \text{DEPTNUM}, \text{QUAN})
\]

The domain of DEPTNUM is \([1 \ldots 30]\) and that of PNUM is \([1 \ldots 400]\). Now, a client can create a replica of this relation using the following expression:

\[
11 \leq \text{PNUM} \land \text{PNUM} \leq 20
\]

Here, PNUM is the RS-attribute of the relation. As can be observed, if there is only one RS-attribute of a relation then datagroups can be managed efficiently. But, if there are multiple RS-attributes then the process of managing datagroups becomes complex. We consider these two scenarios in the subsequent part of this paper. A In section 4, we consider replication with single RS-attribute, that is linearly ordered; in section 5, we consider multiple RS-attribute replication, where RS-attributes are not necessarily linearly ordered.

4 SINGLE RS-ATTRIBUTE REPLICATION

In this section, we consider replication with single RS-attribute; we denote the RS-attribute common
to all clients as a common replica selection (CRS) attribute. We assume that clients form a replica by specifying a bound on a particular CRS-attribute, that spans an interval in the range of this attribute. We call this interval a replication interval of that attribute. The range \( R = [crs_{min}, crs_{max}] \) of a CRS-attribute is divided into a set of non-overlapping intervals or fragments \( F = (F_1, F_2, \ldots, F_n) \) where,

\[
F_i = \begin{cases} 
[crs_{min} + (i-1)l, crs_{min} + il], & 1 \leq i < n \\
[crs_{min} + (i-1)l, crs_{max}], & i = n
\end{cases}
\]

Here, \( l \) denotes the length of fragment other than the last one. We present a method of estimating a suitable value of \( l \) based on limiting the percentage of redundancy (\( r \)) while mapping a replication interval to a number of consecutive fragments.

Let \( R_{avg} \) be the average replication interval. As shown in Figure 2, while mapping the replication interval \( R_{avg} \) to fragments \( F_i, F_{i+1}, F_{i+2} \) and \( F_{i+3} \), the redundant intervals on the left and the right end are \( r_l \) and \( r_r \) respectively. These redundant intervals arise, as a replication interval is mapped to an integral number of consecutive fragments. Here, as a replication interval starts and ends at random location within a fragment, the expected value of both \( r_l \) and \( r_r \) is \( l/2 \). (Although the length of the last (nth) fragment is different from the rest, for the simplicity of the calculation we consider all fragments to be of length \( l \).) So, the total expected redundant interval is \( l \) or one fragment length. So,

The percentage of redundancy, \( r = \frac{l}{R_{avg} + l} \times 100\% \)

Given the value of \( r, l \) can be calculated from the above equation. Having the value of \( R_{avg} \) fixed, lower \( r \)-value results in lower \( l \)-value and therefore larger number of fragments. The value of \( r \) (0 < \( r < 100 \)) is set to a particular value (say, 10%) by the system administrator.

The portion of updates applied to a fragment \( F_i \) during a pruning interval is estimated by its weight \( W_i \). This weight can be determined as a function of fragment size and the number of clients \( n_i \) subscribing to it. Here, the number of clients subscribing to a fragment is regarded as the subscription level of the fragment. The size of fragment \( F_i \) refers to the number of tuples in the database spanned by the fragment.

\[
W_i = \frac{\text{size}(F_i) \times n_i}{\sum_{i \in F} \text{size}(F_i) \times n_i}
\]

The server forms a set of datagroups \( G = \{G_1, G_2, \ldots, G_M\} \) where each datagroup consists of a set of consecutive fragments. Updates to the fragments of each datagroup are stored in a separate update log file.

Having described the details of the system, our goal is to cluster the set of fragments into a set of datagroups \( G \) that minimizes the total cost function as described in the following subsection.

### 4.1 Cost Model

Though our model assumes a portion of client-centric processing to remove redundant updates, our cost model estimates only the disk I/O time, as CPU time is negligible compared to the disk I/O time. In our approach, fragment definition is simple and update to fragment mapping is also a simple operation. Moreover, each group can be defined simply as a list of consecutive fragments. Hence, we can store the group definition table in the main memory because of its insignificant space requirement.

Updates of each datagroup are stored in separate update log file. As the size of the update log file increases, additional disk space is assigned to it in chunks of sectors called allocation units or blocks (Ng, 1998). In this scenario, it is highly improbable that the allocation units of a log file be contiguous (Tanebaum, 1996). So, total seek time and rotational latency, experienced in retrieving a log file, increases linearly with the number of allocation units spanned by it. We take this into consideration while developing the cost function in the subsequent part of this subsection. We assume that each block except the first one in a log file imparts delay equivalent to the disk latency.

The total cost, that represents server processing within a pruning interval \( T \), consists of the four server activities: update mapping (mapping of updates to the corresponding datagroups), update storage (storage of all updates onto disk), update propagation (retrieval and transmission of update logs), and update pruning (elimination of unnecessary updates from the disk). Here, the cost of each activity is measured by time delay experienced in it. The total cost is therefore:

\[
\text{Total Cost} = \text{Update Mapping Cost} + \text{Storage Cost} + \text{Propagation Cost} + \text{Pruning Cost}
\]

The variables used in the cost function and in the subsequent analysis are given below:

**Replication Interval**

![Figure 2: Mapping a replication interval](image-url)

- \( F_i \) to \( F_{i+3} \)
- \( r_l \) and \( r_r \) are the redundant intervals.
- The range of CRS-attribute is represented as the straight line.
content is written to disk. Each datagroup, and whenever a buffer is filled, its store all the update logs onto disk at the server. We Update storage cost indicates the time needed to any disk access. So, For each update, arrives, it can be mapped to the relevant update without the updates to the datagroups. While an update arrives, the right term indicates the actual transfer time. dumping the content of datagroup buffer to the disk, retrieval cost of the updates. To the client. As stated earlier, we include only the required to load the updates into main memory, scan the updates and transfer the appropriate update logs to the client. As stated earlier, we include only the retrieval cost of the updates. Update propagation cost measures the time required to load the updates into main memory, scan the updates and transfer the appropriate update logs to the client. As stated earlier, we include only the retrieval cost of the updates.

Update Mapping Cost = 0

Update storage cost indicates the time needed to store all the update logs onto disk at the server. We assume that a main memory buffer is maintained for each datagroup, and whenever a buffer is filled, its content is written to disk.

Update Storage Cost
\[ \sum_{j=1}^{M} \left[ C_D \left( \frac{\lambda T S_U}{B} \sum_{i | F_i \in G_j} W_i \right) + C_R \lambda T S_U \sum_{i | F_i \in G_j} W_i \right] \]

The left term indicates the disk access time while dumping the content of datagroup buffer to the disk, and the right term indicates the actual transfer time.

Update propagation cost measures the time required to load the updates into main memory, scan the updates and transfer the appropriate update logs to the client. As stated earlier, we include only the retrieval cost of the updates.

Update Propagation Cost
\[ \sum_{k=1}^{N} \left[ C_D |S_k| + \sum_{G_i \in S_k} \left( \frac{\lambda T S_U}{D_C} \sum_{j | F_j \in G_i} W_j \right) - 1 \right] C_L + C_R \lambda T S_U \sum_{G_i \in S_k} \sum_{j | F_j \in G_i} W_j \]

Here, the first term in the parentheses stands for the disk access time, the second term for the latency, and the last one for transfer time, while retrieving log files of the datagroups relevant to client \( k \).

Pruning cost includes the time necessary to scan the log files to eliminate the unnecessary updates. As this activity is performed at the end of each pruning interval (\( T \)), each log file contains the updates stored in time period \( 2T \). So,

Pruning Cost
\[ = MC_D + \sum_{k=1}^{M} \left( \left[ \frac{\lambda T S_U}{S_C} \sum_{i | F_i \in G_k} W_i \right] - 1 \right) C_L + C_R \lambda T S_U \sum_{i | F_i \in G_k} W_i \]

Here, the first term stands for the total access time for all datagroups. Within the summation, the first term indicates the latency for a datagroup, and the second term indicates the transfer time.

4.2 Datagroup Design and Maintenance

4.2.1 Preliminaries

A path graph \( P \) is a simple connected graph with \( |V_p| = |E_p| + 1 \) that can be drawn so that all of its vertices lie on a single straight line (Gross and Yellen, 1999). An \( n \)-vertex path graph is denoted as \( P_n \). While deleting a node \( v_i \) from \( P_n \) we add an edge \( (v_{i-1}, v_{i+1}) \) if \( i \neq 1 \) and \( i \neq n \). Similarly while deleting a set of connected nodes \( \{v_i, \ldots, v_j\} \), \( i < j \), we add an edge \( (v_{i-1}, v_{j+1}) \) if \( i \neq 1 \) and \( j \neq n \). To insert a node \( v' \) in \( P_n \) at position \( i \), \( 1 \leq i \leq n + 1 \) we:

- add edge \( (v_{i-1}, v') \), if \( i > 1 \),
- add edge \( (v', v_i) \), if \( i \neq n + 1 \) and
- remove \( (v_{i-1}, v_i) \), if \( 1 < i \leq n \).

We map the set of fragments \( F = \{F_1, \ldots, F_n\} \) to the set of nodes \( V = \{v_1, \ldots, v_n\} \) of path graph \( P_n \) in order so that \( F_1 \) maps to \( v_1 \), \( F_2 \) to \( v_2 \) and so on. All the nodes in \( P_n \) with zero subscription level are deleted resulting in a path graph \( P_{m_n} \) \((m \leq n)\). We call this resulting path graph \( P_{m_n} \) as truncated path graph. Associated with each node \( v_i \) of this truncated path graph \( P_{m_n} \) is the following information:

1. \( f(v_i) \) fragment which \( v_i \) corresponds to,
2. \( f_i \) number of clients subscribing to node \( v_i \), and
3. \( f_i, i+1 \) number of clients accessing \( v_i \) and \( v_i+1 \) \((1 \leq i < m)\) simultaneously.

To split the path graph along edges, we calculate the redundancy factor \( RF_{i,i+1} \) associated with each of the edges \( (v_i, v_{i+1}) \), \((1 \leq i < m)\). This redundancy factor indicates the ratio of cumulative redundant updates to cumulative update volume — both of the two terms consider the updates from fragments corresponding to \( v_i \) and \( v_{i+1} \) only — accessed by clients subscribing to fragments corresponding to \( v_i \) and/or \( v_{i+1} \). This parameter can be calculated as follows.
Let, $f_{i,t+1}$ denote the total number of clients subscribing to $v_i$, but not to $v_{i+1}$; and $f_{i,t+1}$ the number of clients subscribing to $v_{i+1}$, but not to $v_i$. Now,

$$f_{i,t+1} = f_i - f_{i+1},$$
$$f_{i+1} = f_{i+1} - f_{i+1}$$

Average number of updates accessed by a client from the fragment $f(v_i)$ associated with $v_i$ can be given as $\lambda Wf(v_i)$. When nodes $v_i$ and $v_{i+1}$ belong to the same datagroup, total volume of redundant updates ($R_{i+1}$) accessed by all clients from the fragments corresponding to these nodes can be written as follows:

$$R_{i+1} = f_{i+1} + f_{i+1} - f_{i+1} + f_{i+1}$$

Now, total update volume ($C_{i+1}$) accessed by all clients from the fragments corresponding to nodes $v_i$ and $v_{i+1}$ can be derived as:

$$C_{i+1} = \lambda (f_i + f_{i+1} - f_{i+1}) (Wf(v_i) + Wf(v_{i+1}))$$

So, Redundancy factor, $RF_{i+1} = \frac{R_{i+1}}{C_{i+1}}$ (1)

4.2.2 Datagroup Design

We design the datagroup by splitting the truncated path graph $P_m(V,E)$ along edges (termed as split edge) selected in the decreasing order of their values (i.e., redundancy factor). We carry on the splitting until no cost-effective split operation is possible.

Algorithm Datagroup-Design
begin
  While TRUE do
    select an edge $e \in E$ with maximum value
    if split along $e$ is not cost-reducing, then quit.
    delete $e$ from $E$.
  end
end

4.2.3 Operators for Redesigning Datagroups

**Merge** operation involves replacing two datagroups by their union. While merged, clients subscribing to both the datagroups have to access one datagroup instead of two, reducing the delay due to disk latency. But, redundant updates for the clients subscribing to only one of the datagroups increase. We try to apply merge operation when redundancy factor of a split edge connecting two datagroups becomes less than that of an edge within one of these groups.

**Split** operation involves dividing a datagroup, along the split edge, into two datagroups. We apply split operation after merging two or more datagroups.

4.2.4 Redesign

As time passes, the configuration of the ICDB changes. New clients may be added periodically. Moreover, existing clients may change their subscriptions. Hence, the number of nodes and value of the edges change in the truncated path graph.

In our approach, the redesign of the groups, that is performed periodically after a time interval, is simple. For this purpose we merge two groups pairwise if the precondition of merge holds, and in the merged groups we apply split operations. Edges in the merged group are considered in the decreasing order of the weight until no cost benefit splitting is possible. So, redesign is performed locally keeping the remaining groups un-affected.

Example: In Figure 3, two datagroups $G_i$ and $G_{i+1}$ with three and four fragments respectively are shown. Weights of the edges at time $t_0$ are shown above in the figure. After certain interval (at time $t_1$) the weights are as shown below in the figure. At time $t_1$, delete $d$ from $E$. So, these two groups are merged, and the merged group is splitted, if feasible, along edges $d, s, e$ in that order.

5 MULTI-ATTRIBUTE REPLICATION

The datagroup design described in the previous section is based on a single linearly ordered RS-attribute: all the clients must form their replicas using that attribute. In this section, we consider the design and maintenance of datagroups in an ICDB environment where replicas can be specified using multiple RS-attributes; and all of these RS-attributes may not necessarily be linearly ordered. In forming replicas, clients, instead of specifying bounds, may specify discrete values for some RS-attributes, which we call
**discrete RS-attributes.** Here it should be noted that the RS-attributes are generally identified as discrete based on the application semantics: for example, it is desirable for the clients to specify the department (using RS-attribute DEPT-NAME) as discrete point in the domain of DEPT-NAME rather than as bounds on that RS-attribute.

To design and maintain datagroups with multiple RS-attributes, we use the notion of grid partition of tuple space and of grid directory, which are keys to a dynamic multi-key file structure called the grid file (Nievergelt and Hinterberger, 1984). While the notions are used in (Nievergelt and Hinterberger, 1984) to provide both efficient processing of range queries and fast access to individual records, we apply the notions to increase the performance of ICDB system in storing and retrieving updates for a group of clients. The design of datagroup requires us to divide the range of RS-attributes into fragments, and thus obtain the grid partition; form path graph corresponding to RS-attribute on each axis; divide the grid partition into k-dimensional rectangles by greedily splitting along the axes: each of the rectangles corresponds to a datagroup. Thus we divide the tuple space into grid blocks.

The attribute fragments can be constructed in two ways depending on the type of the attribute (i.e., linearly ordered or discrete). For a linearly ordered RS-attribute, the range of the attribute can be fragmented using the technique described in section 4. For a discrete RS-attribute, we use the vertical partitioning algorithm (Chakraborty et al., 2002) to cluster the attribute values. The attribute values are clustered based on the affinity between attribute values (we measure the affinity between two values by the number of clients, that explicitly specify both of these two values using the corresponding RS-attribute). Upon partitioning the range of the RS-attribute, each cluster of the attribute values corresponds to a fragment of the corresponding attribute.

The information about the grid partition is maintained using a data structure called grid directory. A grid directory consists of two parts: a k-dimensional array called grid array, and index information associated with each dimension of the grid array. Elements in grid array are in one-to-one correspondence with the grid blocks of the partition. Each of these elements is either a structure or pointer to a structure that contains the following information about the corresponding grid block:

1. **size** of the grid block (in number of tuples)
2. **number** of clients subscribing to the grid block
3. **weight** of the grid block

The index information associated with each axis of grid array provides the representation of attribute fragment corresponding to each possible index value along that axis—the relevant attribute being obvious from the axis. As noted earlier, this index information for a linearly ordered attribute can be represented by the range and the fragment length (l) of the attribute. Using this information the fragment corresponding to an index value can be derived, and, on the other hand, for an attribute value the corresponding fragment or index can also be calculated. However, the index information is no longer simple for discrete attributes, as each fragment of these attributes should have explicit representation. In this case, we use an one dimensional array, where each location points to the corresponding fragment definition structure. We assume that the number of distinct values of a discrete RS-attribute is not prohibitively high; so that the index information consumes insignificant memory, and partitioning attribute values remains simple.

The index information of an axis should store the list of **redundant index locations** along the axis; marking an index location of an axis **redundant** we virtually eliminate a (k − 1)-dimensional subsection of the grid array. We call an index location **redundant** if the subscription level of the fragment corresponding to the index value is zero and, while forming replica, the corresponding attribute is explicitly specified by all clients (we don’t consider `PNUM=*` an explicit specification of PNUM). However, elimination of these redundant index locations doesn’t remove all the **redundant blocks** \(^1\) in the grid array. There may remain some redundant blocks or holes (Figure 4) that should be identified, and be excluded.

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\(^1\)A grid block that is not replicated by any client is referred to as **redundant block**; otherwise a grid block is called **replicated block**
Datagroup Design

While forming datagroups, the axes corresponding to different types of attributes are treated differently. For linearly ordered RS-attributes, the corresponding axes of the grid array are split at various suitable locations. To determine these locations we maintain a path graph for each of such attributes or axes. On the other hand, for discrete RS-attributes, the index values of the corresponding axis are clustered together. To cluster these index values, for such attributes, we maintain a minimum spanning tree. In case of discrete RS-attributes is similar to that developed in section 4. However, we introduce here minor changes in parameters, and in update storage cost. In this case, \( F_i \) should represent grid blocks instead of fragments.

As outlined earlier, the index information (associated with grid array), the datagroup array and its index information are stored in main memory. But, datagroup records associated with each datagroup reside in disk. In this respect, updates from the redundant blocks within a datagroup can’t be filtered out without these datagroup records. So, some redundant updates should be stored in the datagroup buffers. Hence, the update arrival rate (from the point of view of datagroup buffers) is no longer \( \lambda \). We denote this update arrival rate of blocks within datagroups (redundant or replicated) as \( \lambda_d \), and estimate it as follows:

\[
\lambda_d = \lambda \times \frac{S_d}{S_r}
\]  

Here, \( S_d \) is the size of all the grid blocks (replicated or redundant) within a datagroup, and \( S_r \) is the size of all the replicated grid blocks.

Update Storage Cost

\[
= \sum_{j=1}^{M} \left[ (2C_D + C_R S_D) \left( \lambda_d TS_U \sum_{i | F_i \in G_j} W_i \frac{1}{B} \right) + C_R \lambda TS_U \sum_{i | F_i \in G_j} W_i \right]
\]

Here, \( S_D = \text{average datagroup record size} \)

5.1 Cost Model

The cost function for replication with multiple attributes is similar to that developed in section 4. However, we introduce here minor changes in parameters, and in update storage cost. In this case, \( F_i \) should represent grid blocks instead of fragments.

As outlined earlier, the index information (associated with grid array), the datagroup array and its index information are stored in main memory. But, datagroup records associated with each datagroup reside in disk. In this respect, updates from the redundant blocks within a datagroup can’t be filtered out without these datagroup records. So, some redundant updates should be stored in the datagroup buffers. Hence, the update arrival rate (from the point of view of datagroup buffers) is no longer \( \lambda \). We denote this update arrival rate of blocks within datagroups (redundant or replicated) as \( \lambda_d \), and estimate it as follows:

\[
\lambda_d = \lambda \times \frac{S_d}{S_r}
\]  

Here, \( S_d \) is the size of all the grid blocks (replicated or redundant) within a datagroup, and \( S_r \) is the size of all the replicated grid blocks.

While storing updates, as a datagroup buffer becomes filled, the corresponding datagroup records are retrieved from the disk; redundant updates are then removed, and relevant updates are stored in the disk. So, updates arrive on disk side at the rate of \( \lambda \). Now,

Update Storage Cost

\[
= \sum_{j=1}^{M} \left[ (2C_D + C_R S_D) \left( \lambda_d TS_U \sum_{i | F_i \in G_j} W_i \frac{1}{B} \right) + C_R \lambda TS_U \sum_{i | F_i \in G_j} W_i \right]
\]

Here, \( S_D = \text{average datagroup record size} \)

5.2 Datagroup Design

While forming datagroups, the axes corresponding to different types of attributes are treated differently. For linearly ordered RS-attributes, the corresponding axes of the grid array are split at various suitable locations. To determine these locations we maintain a path graph for each of such attributes or axes. On the other hand, for discrete RS-attributes, the index values of the corresponding axis are clustered together. To cluster these index values, for such attributes, we maintain a minimum spanning tree.

For each linearly ordered RS-attribute, we maintain a path graph the same way as described in section 4. In case of discrete RS-attribute \( r \), each index location \( (k) \) of the corresponding axis in grid

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**Figure 5:** Datagroup array represents the datagroup formed by partitioning the grid array (Figure 4). The index information stores the locations of grid array corresponding to each index value of the respective axis (of datagroup array). A datagroup record stores the list of redundant blocks within each datagroup.

from the datagroups.

Datagroups are formed by partitioning the grid array into non-overlapping \( k \)-dimensional rectangular regions. This partitioning involves choosing few suitable locations on each axis, and cutting the grid array with hyperplanes orthogonal to the axis on the selected locations. The boundaries of these planes define the datagroups. Figure 4 shows datagroup formation for the case \( k = 2 \), from which the general case \( k > 2 \) can easily be inferred. Here, datagroups are formed by splitting the grid array by lines perpendicular to \( x \)-axis on \( x_1 \) and \( x_2 \), and by that perpendicular to \( y \)-axis on \( y_1 \). Three of the six datagroups formed contain redundant blocks, that don’t fall within any redundant index of any of the axes.

To represent the datagroups we use an array, that we call datagroup array \( D \), and the associated index information. Size and shape of this datagroup array depends on the number of splits across each of the axes. As shown in Figure 5, the shape of the datagroup array derived from the grid array of Figure 4 is \((2 \times 3)\). Each element in the datagroup array corresponds to a datagroup, and it points to a record that stores the list of redundant blocks within that datagroup. The index information associated with the datagroup array is maintained the same way as with the grid array: a one dimensional array is maintained for each axis; and this array stores the range of index locations of the grid array spanned by each index value of the corresponding axis of the datagroup array.

In reality, there will be only few datagroups; so the datagroup array and its associated index information are stored in main memory, but the records pointed to reside in the disk.
array corresponds to a cluster of values of that attribute (i.e., attribute fragment \( p_i^j \)). In this clustering operation the cost factor is not considered. So, further grouping of these clusters is attempted taking the cost factor into consideration. For such an attribute \( i \), we form a redundancy graph \( (G_i) \) with vertex set \( V_i = \{v_i^1, v_i^2, \ldots, v_i^n\} \), where each vertex corresponds to a fragment of attribute \( i \). Each node \( v_i^j \) of this graph stores \( f_{ijk} \), which is the number of clients subscribing to corresponding fragment \( p_i^j \). Initially, the value of each edge \((v_i^j, v_i^k)\) is the number of clients \((f_{j,k}^i)\) subscribing to both of the fragments corresponding to \( v_i^j \) and \( v_i^k \) (i.e., \( p_i^j \) and \( p_i^k \) respectively). We calculate the redundancy factor \( RF_{j,k}^i \) for each edge \((v_i^j, v_i^k)\) and associate this with the respective edge.

\[
RF_{j,k}^i = \frac{(f_j^i - f_{j,k}^i) W_k^i + (f_k^i - f_{j,k}^i) W_j^i}{(f_j^i + f_k^i - f_{j,k}^i) (W_j^i + W_k^i)}
\]

Here, \( W_j^i \) and \( W_k^i \) are the sum of the weight of all replicated grid block whose \( i \)th index value is \( j \) and \( k \) respectively.

Having derived this redundancy graph \( G_i \), we obtain the minimum spanning tree of this graph \( MST(G_i) \). While forming datagroups, we use this graph to cluster the indices of axis \( i \) of the grid array. This clustering is done by splitting \( MST(G_i) \) along suitable edges, and hence forming the groups of index values.

5.3 Splitting Policy and Redesign

Several splitting policies are possible, while forming datagroups. The simplest one is to choose the dimension or axis according to a fixed schedule, perhaps cyclically. The corresponding axis is split by selecting the edge with maximum value from the path graph (in case of linearly order RS-attribute), or from minimum spanning tree (in case of discrete RS-attribute), of the corresponding axis. We carry on the splitting until no cost-effective split operation is possible.

Having finished the splitting, the datagroup array is built, where index information associated with each axis reflects the splitting done along that axis, and the datagroup records store the list of redundant gridblocks within each datagroup.

As the configuration of the ICDB changes, datagroups can be redesigned using the method described in section 4. The merge and split operation can be applied along different axes independently. Thus, in case of multiple attribute replication, it is possible to redesign datagroups without beginning from the scratch.

6 SIMULATION EXPERIMENTS

This section describes our methodology for evaluating the update propagation scheme, and presents an experiment demonstrating the effectiveness of the proposed update propagation scheme. We begin with an overview or the experimental design of the simulator and description of the ICDB environment. We then show that data-centric grouping \((dc)\) of updates using our proposed algorithm results in faster per-client refresh times than other more intuitive methods. Refresh time includes the time required for the server to store the updates in the log files, retrieve the relevant updates to propagate to the clients, and prune the update log files after each pruning interval.

6.1 Simulation Model

In our simulation, we assume that all clients connect to the server within each pruning interval \((T)\); however, the connection time of a client is uniformly distributed over that interval. The update logs are pruned at the end of each pruning interval \(^2\). Each client subscribes to a certain portion of the database, which we call the percent of replication \((p\%)\). From this percent of replication we derive the replication interval \((R_{avg})\) of the clients along each RS-attribute, and this replication interval is randomly chosen from the range of each RS-attribute. We consider the update arrival rate proportional to the number of clients. The updates are distributed to the grid blocks according to their weights. In this simulation, we consider replication of a database relation schema with two linearly ordered RS-attributes.

To compare with our scheme we consider two update propagation schemes: clients centric scheme \((cc)\) and the scheme with one giant group \((gg)\), that are described in Table 1. We show that as the client population and the per-client update arrival rate increase, the advantage of \( dc \) increases over other techniques: performance gains generally come from avoiding redundant update storage and retrieval by identifying the overlapping subscriptions.

6.2 Experiments and Results

To measure the effectiveness of our data-centric scheme \((dc)\) we measure the per-client refresh time for varying client population and per-client update arrival rate \((u_{rate})\). The experimental parameters are given in Table 2. For each setting of experimental parameters we run the simulation for 10 simulation hours.

\(^2\)Maintaining the update logs with widely varying connection intervals of the clients is a separate issue that is studied in (Chakraborty et al., 2004)
Table 1: Grouping Schemes.

<table>
<thead>
<tr>
<th>Grouping Scheme</th>
<th>comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>data-centric (dc)</td>
<td>groups generated with the grid partitioning scheme widely employed, creates one group for each client eliminates duplicate update storage by storing updates for all the clients in a single group</td>
</tr>
<tr>
<td>client-centric (cc)</td>
<td></td>
</tr>
<tr>
<td>giant-group (gg)</td>
<td></td>
</tr>
</tbody>
</table>

Table 2: Parameter values for experiments.

<table>
<thead>
<tr>
<th>Parameter Description</th>
<th>Values (control values in {})</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clients</td>
<td>1, 2, 5, 10, {50}, 100, 200, 400, 800</td>
</tr>
<tr>
<td>$u_{rate}$ (update/client/min)</td>
<td>0.1, 0.5, {1}, 2, 4, 8</td>
</tr>
<tr>
<td>Pruning interval, $T$ (min)</td>
<td>{60}</td>
</tr>
<tr>
<td>Percent of replication ($\rho$)</td>
<td>{10}</td>
</tr>
</tbody>
</table>

Figure 6 shows the effect of varying client population on per-client refresh time. Scheme $gg$ fares poorly with low population because it generates and stores update logs for a significant portion of database that is not subscribed to. Client-centric scheme performs well with very low client population, but with the increase in client population the refresh time increases drastically because of duplicate update storage (once for every relevant client) and pruning overhead for the duplicate updates. On the other hand, as scheme $gg$ stores updates only once, it doesn’t suffer from storage and pruning overhead. Hence, per-client refresh time doesn’t degenerate severely for this scheme. However, for every client the whole update log file should be retrieved that contains significant portion of irrelevant updates for that client. As is evident from the figure, within the given range of client population, the refresh time of scheme $dc$ is optimal except for the very low client population, where client-centric approach predominates.

Figure 7 shows the effect of variation of per-client update arrival rate upon per-client refresh time. In this scenario, the $dc$ approach achieves significant savings on refresh time over other methods.

7 CRITICAL EVALUATION

We propose an approach to update propagation that doesn’t assume the inherent data organization of the database. We show that efficient algorithms are possible for designing and maintaining datagroups as well as mapping clients to groups. For both single and multiple attribute replication, mapping new clients to the datagroups is simple. Maintenance of the datagroups, with the change in ICDB configuration, doesn’t require frequent recomputation of datagroups from the scratch. So, it is possible to maintain the datagroups incrementally. If the change in the configuration is not drastic, we only have to modify a few datagroups locally. Moreover, in case of multiple RS-attributes, as the splitting is carried on each axis independently, the computational complexity of datagroup formation only increases linearly with the increase in number of RS-attributes (i.e., dimension of the grid array).

8 CONCLUSION AND FUTURE WORKS

In this paper, we offer a computationally efficient solution to scalable update propagation problem in ICDB. Based on a cost model, we construct and maintain datagroups by simply splitting each path graph (one for each RS-attribute) independently along few selected edges. We address the problem of duplicate update propagation in ICDB and propose a solution
that provides a little per-client processing. We introduce the notion of pruning interval to remove the unnecessary updates from the log files and thus save both retrieval time and disk space. The replica formation time can be minimized by organizing the data as a grid file, as only the necessary grid blocks can be fetched from the disk without the need to scan (in worst case) the whole data file. Our work on ICDB is ongoing. Currently we are working on building an analytical model for estimating the savings in terms of data volume and network time resulting from eliminating duplicate update propagation. Also, we are working on a scheme for vertical partitioning the attributes of a relation to reduce the updates that need to be propagated to the clients. The objective here is to have one consistent model for data grid design that includes vertical partitioning of a relation.

REFERENCES


