LOCALIZATION WITH DYNAMIC MOTION MODELS
Determining Motion Model Parameters Dynamically in Monte Carlo Localization

Adam Milstein
Department of Computer Science, University of Waterloo, Waterloo, Ontario, Canada

Tao Wang
Department of Computing Science, University of Alberta, Edmonton, Alberta, Canada

Keywords: Mobile Robots, Localization, Machine Learning.

Abstract: Localization is the problem of determining a robot’s location in an environment. Monte Carlo Localization (MCL) is a method of solving this problem by using a partially observable Markov decision process to find the robot’s state based on its sensor readings, given a static map of the environment. MCL requires a model of each sensor in order to work properly. One of the most important sensors involved is the estimation of the robot’s motion, based on its encoders that report what motion the robot has performed. Since these encoders are inaccurate, MCL involves using other sensors to correct the robot’s location. Usually, a motion model is created that predicts the robot’s actual motion, given a reported motion. The parameters of this model must be determined manually using exhaustive tests. Although an accurate motion model can be determined in advance, a single model cannot optimally represent a robot’s motion in all cases. With a terrestrial robot the ground surface, slope, motor wear, and possibly tire inflation level will all alter the characteristics of the motion model. Thus, it is necessary to have a generalized model with enough error to compensate for all possible situations. However, if the localization algorithm is working properly, the result is a series of predicted motions, together with the corrections determined by the algorithm that alter the motions to the correct location. In this case, we demonstrate a technique to process these motions and corrections and dynamically determine revised motion parameters that more accurately reflect the robot’s motion. We also link these parameters to different locations so that area dependent conditions, such as surface changes, can be taken into account. These parameters might even be used to identify surface changes by examining the various parameters. By using the fact that MCL is working, we have improved the algorithm to adapt to changing conditions so as to handle even more complex situations.

1 INTRODUCTION

Localization is the problem of determining a robot’s accurate location in an environment based on inaccurate sensor information. For most complex tasks, a robot must know its current location before it can perform any useful actions. In fact, a robot needs to know its current location in order to find a specific subsequent location where it needs to perform an action. Effective localization is fundamental to most mobile robot applications. The problem of localization arises from the fact that all physical sensors are inaccurate. If the encoders on a robot gave the exact distance moved without error, then there would be no localization problem. After any motion, the robot would be at the location given by the encoders. Unfortunately, no physical sensors are perfect. Robots commonly have some type of range sensor which is used together with a map of the environment to determine the actual motion. Of course, range sensors are also prone to error. Localization is the problem of compensating for all of these errors and producing an accurate position.

One common algorithm for localization is Monte Carlo Localization (MCL) (Thrun et al 2005). MCL combines various sensor models and a map of the environment, using a recursive Bayes filter to estimate the belief state of the robot’s location. Obviously, the quality of these models is important. Although MCL is robust to some errors in the
models and map, the combination of different errors can cause it to fail.

Since most of the time MCL works properly, finding the correct localization for the robot, it is possible to correct various errors in the models to allow MCL to converge to a correct solution even more accurately. Although improvements are unnecessary when the algorithm is already working, by making corrections the errors should not build up, and future situations may be easier to solve correctly. Since minor errors in MCL can combine to produce problems, reducing minor errors when they have no impact prevents those same errors from building up with other errors to cause localization failures.

One situation where reducing minor errors is critical is in the case of global localization. This is a special case of localization where the robot’s starting position is unknown. In this case, the entire space must be searched and minor errors can easily cause global localization to fail. If some of these minor errors can be removed during ordinary execution, then global localization in the future may be easier.

It has already been demonstrated that the static map of the environment required by MCL can be updated during ordinary execution to accommodate changes in the environment (Milstein, 2005). In this article, we demonstrate that it is also possible to update the parameters of the motion model during execution of MCL to provide a more accurate idea of how the robot moves through the environment. In general, a single, simplified, motion model is created that reflects some idea about how a robot moves. This model is necessarily a generalization because the robot's motion is effected by various changing situations, such as the surface it moves on, and possibly the power of the batteries or the inflation and wear on the tires. While all of these situations could be monitored and manually compensated for, it would require an enormous amount of work to create a motion model that reflected all of these different states. It is also impossible to predict all possible circumstances, so such a complex model would be invalidated by any unanticipated change in conditions. By automatically updating the motion model according to the observations, it is possible to optimize the model to any situation, even if that situation has not been predicted in advance. As the model is updated, errors in MCL due to the motion model are reduced, leaving greater tolerance for errors caused by other factors.

2 BACKGROUND

Monte Carlo Localization uses models of various sensors, together with a recursive Bayes filter, to generate the belief state of a robot. In fact, MCL is a specific instance of a POMDP. A standard form of MCL uses a motion model to predict the robot's motion together with a sensor model to evaluate the probability of a sensor reading in a particular location. The sensor model necessarily includes a static map of the environment. The algorithm can be applied to virtually any robot with any sensor system, as long as these two models can be created. One common implementation where MCL is very successful is on a wheeled robot using a range sensor such as a laser rangefinder. One benefit of this combination is that the map and location used by the algorithm are in a human readable format. Although we give the general algorithm in the following sections, which should be applicable to other robots, where application specific details are required, we assume the type of robot as described.

2.1 Recursive Bayes Filter

MCL is an implementation of a recursive Bayes filter. The posterior distribution of robot poses as conditioned by the sensor data is estimated as the robot's belief state. A key detail of the algorithm is the Markovian assumption that the past and future are conditionally independent given the present. For a robot this means that if its current location is known, the future locations do not depend on where the robot has been. In virtually any environment this is the case, so making the assumption is reasonable in general.

To produce a recursive Bayes filter, we represent the belief state of the robot as the probability of the robot's location conditioned by the sensor data, where sensors include odometry.

\[
\text{Bel}(x_t) = p(x_t | z_{1:t}, u_{1:t})
\]

\(x_t\) represents the robot's position at time \(t\), \(z_t\) the robot's sensor readings at time \(t\) and \(u_t\) the motion data at time \(t\). To simplify the subsequent equations we use the notation that \(a^t = a_0, \ldots, a_t\).

While this equation is a good representation of the problem, it is not much use since it can not be calculated as is. By applying a series of probabilistic rules, together with the Markovian assumption, equation 1 is factored into:

\[
\text{Bel}(x_t) = \text{Bel}(x_t | z_{1:t}, u_t) p(x_t | z_{1:t}, u_t) p(z_{1:t}, u_t | x_{1:t})
\]

\(p(x_{1:t} | z_{1:t}, u_t)\) is \(\text{Bel}(x_{1:t})\) giving us the recursive equation necessary for a recursive
Bayes filter. $\eta$ is a normalization constant that can be calculated by normalizing over the state space. $p(z_t | x_t)$ is the sensor model, representing the probability of receiving a particular sensor reading given a robot’s location. Finally, $p(x_t | x_{t-1}, u_t)$ is the motion model. It is the probability that the robot arrives at location $x_t$ given that it started at location $x_{t-1}$ and performed action $u_t$. The sensor and motion model are representations of the physical components of the robot and must be determined experimentally for each robot and sensor device.

### 2.2 Particle Approximation

It would appear that, given the two models, equation 2 is all that is necessary to perform localization with MCL. Unfortunately, a problem occurs with the integral. The equation requires integrating over the entire state space. Although we can evaluate the models at any point in the space, there is no closed form to the integral. Further, the simplest kind of robot moves in a continuous, 3 dimensional state space with an x and y location together with an angle of rotation. Calculating the integral over this space is impossible, especially for a real time algorithm. In order to solve this problem, we approximate the continuous space with a finite number of samples. The integral over the space becomes a sum over the finite number of particles. Of course, approximating the space results in a certain amount of error when low probability locations are not represented. If the robot is really at one of these locations it can never be localized. However, if the number of particles is well chosen MCL works well in most situations.

### 2.3 Algorithm

As the robot moves, it reports its odometry and sensor data to the MCL algorithm. After each move each particle is moved randomly according to the motion model, based on the motion actually reported. The particles are then updated with a weight determined by the sensor model for the particle’s location. Finally, the particles are resampled by repeatedly choosing samples randomly, with replacement, from the current set, according to the weights assigned by the sensor model.

The effect of resampling is to replace the weight of the individual particles with the number of particles at that location. On the robot’s next move the particles at a high probability location will spread out as they are moved randomly according to the motion model, with at least one landing in the robot’s new location. Then the resampling will cause more particles to appear at the correct location, while incorrect locations die out. Assuming that the models and map are accurate, MCL will correctly track the robot’s changing location. Various parameters can be tuned manually to adjust the rate of convergence and the behaviour of the models. Once the belief over the robot’s location is generated, a single location for the robot can be found by looking at the mean of the particles.

### 2.4 Motion Model

The motion model $p(x_t | x_{t-1}, u_t)$ is a critical part of MCL. Unlike the sensor model, which gives the probability of getting a specific sensor reading at a particular location, it is necessary to sample from the motion model. Given a starting location and a reported motion ($x_{t-1}$ and $u_t$), MCL requires that we be able to choose a final location randomly according to the motion model. This requirement precludes us from using any motion model that is very complex. In fact, most motion models are a combination of simple Gaussian distributions. For a holonomic wheeled robot the most common representation is with two kinds of motion leading to three kinds of error. Each movement of the robot is represented as a linear movement followed by a stationary turn. Although a particular robot probably does not follow these exact motions, if we break the robot’s motion into small increments we can use them as an approximation.

Each translation of the robot is approximated by a Gaussian where the mean is the reported distance and the variance is the reported distance multiplied by a parameter. This representation reflects the fact that the range error increases the further the robot travels. Rotation is also represented by a Gaussian. The mean is again the reported angle, but the variance is a parameter multiplied by the angle turned, added to another parameter times the distance moved. The variance takes into account both turn error, which increases as the robot turns, and drift error. Drift error is defined as the robot turning when it tries to go straight. Obviously, it increases the further the robot has travelled. Although it would seem that drift error should be minor, if it occurs at all, this is not in fact the case. Many holonomic wheeled robots use a system where the difference in motion between the drive wheels is used to turn the robot. In such robots, moving forward is accomplished by turning both wheels the same amount, while turning is done by moving the wheels different amounts. It is very likely that, while moving forward, the wheels turn at slightly different rates, causing the robot to rotate. The three parameters involved in the model are often given as
k_r for range error, k_θ for turn error, and k_d for drift error.

These two Normal distributions together represent the motion model for many common robots. However, the algorithms described in this paper should work for any model, provided it is possible to sample from it. In general, some collection of Gaussians works well, since they are often good approximations to a physical system while at the same time being easy to sample from and optimize.

3 DYNAMIC MOTION

The MCL algorithm depends on certain static parameters that must be manually tuned for each implementation. In particular, the sensor model relies on a static map of the environment, while the motion model requires parameters that reflect the specific robot’s motion in the particular environment. Since most interesting problems occur in dynamic environments, or environments with different conditions in different areas, these static parameters are only a broad approximation. Fortunately, MCL is robust to errors in the map and motion model and will successfully localize a robot as long as these parameters are a reasonable representation. However, the more error there is in the static parameters, the less tolerance the algorithm has for errors from other sources. For example, if the environment changes so that the map becomes less accurate, perhaps because of furniture being moved, then an error in the motion model might put the robot in the wrong location. If the changes in the map make an incorrect location look correct to MCL, then there is far less tolerance for the motion model to predict incorrect locations. Either of these errors might be recoverable on their own, but both together could cause a localization failure. If the motion model is correct, then the robot’s next location will be predicted correctly, and the fact that there is a similar location somewhere else won’t matter. Similarly, if the map is accurate, then an incorrect prediction from the motion model will be low probability and will die out in favour of the correct location. As errors in any static parameter build up over time, MCL’s tolerance towards additional errors is reduced until it becomes necessary to manually correct the parameters.

We already know that if MCL is successfully localizing the robot it is possible to automatically correct the map of the environment (Milstein, 2005). When the robot’s location is known, any differences between its sensor readings and the map are probably caused by errors in the map, rather than errors in the sensors. This is especially true if the readings are repeated over time. It is possible to use sensor readings taken when the robot is localized to correct the map. With this modification the static map becomes more accurate over time, instead of less accurate. Of course, it requires several observations to update the map, since a real environment might have transitory objects which should not be in the map, such as people. Thus, even with a dynamic map, there are still errors that will reduce MCL’s tolerance to other problems.

3.1 Motion Model Error

On each step of execution, MCL uses the motion model to predict a new location for the robot, and then uses the sensor model to correct that location. Before the resampling step, the mean of the particles represents the location determined by the motion model. After resampling, the mean represents the location of the robot according to the algorithm. This means that a side effect of executing MCL is a list of errors in the motion model. By recording these values, we can dynamically generate a set of errors that can be processed to correct the model. Since each correction comes attached to a particular location, we can even record in what part of the environment the error occurred.

Given a set of errors, it would be quite easy to determine the variance of a Gaussian distribution, however, with the Gaussian motion model we are using it is not quite so simple. The key realization is that we are not trying to calculate the variance, we are trying to find a parameter of the variance. Remember that the motion model for a differential drive robot depends on three parameters, range error, turn error, and drift error, represented as (k_r, k_θ, k_d). If we let r be the distance travelled and θ be the distance turned, while r and θ are the estimations from the motion model, then the distributions become:

\[ r = N(r, k_r) \quad \text{and} \quad θ = N(θ, k_θ) \]

which are both single valued Gaussians. From MCL we are given a set of \{r, θ, r, θ\} values and we wish to optimise the models in the parameters \{k_r, k_θ, k_d\}.

3.2 Variance Parameters

Because we wish to determine parameters to the variance, instead of the variance itself, no standard technique for estimating Normal distributions will work. In fact, the problem is no longer a single distribution, but rather a continuous set of distributions for each value of \{r, θ\}. Fortunately, the problem can be solved if we treat it as a general
equation, instead of specifically as a probabilistic distribution. The Gaussian equation for \( r \) becomes:
\[
p(r) = \frac{1}{k_r \sqrt{2\pi}} e^{-\frac{(r-\mu)^2}{2(k_r \sigma)^2}} \tag{4}
\]
Since we want to have an accurate model, we want the value of \( k_r \) that maximizes the probability. Given the set of data produced by MCL, we would like to maximize the probability obtained over that entire sample space.
\[
\prod \frac{1}{k_r \sqrt{2\pi}} e^{-\frac{(r-\mu)^2}{2(k_r \sigma)^2}} \tag{5}
\]
Of course, (5) is a little unwieldy to calculate, but a standard trick is to notice that if we maximize \( p(r) \) we also maximize \( \log(p(r)) \). Thus we are left with:
\[
\sum - \log\left( \frac{1}{k_r \sqrt{2\pi}} \right) - \frac{(r - \mu)^2}{2(k_r \sigma)^2} \tag{6}
\]
which is quite straightforward to maximize using virtually any nonlinear technique. A similar process for \( \theta \) gives us a slightly more complicated equation which is just as easy to solve.
\[
\sum - \log\left( k_\theta \sqrt{2\pi} \right) - \frac{(\theta - \phi)^2}{2(k_\theta \sigma)^2} \tag{7}
\]
Using an efficient nonlinear optimisation algorithm, we can maximize these equations over the parameters \( k_r, k_\theta, k_d \) for sets of data obtained by MCL in real time. Although the functions are not concave in these parameters, we have good starting parameters available, since MCL is already using a motion model. The current parameters make a good starting point for the optimization. The new parameters can be used immediately, while the data is still collected to further refine them.

### 3.3 Algorithm

Now that we have a method to update the motion model dynamically, we need to integrate it with MCL, hopefully without significantly affecting the runtime. One of the benefits of MCL is that it is a fairly low cost algorithm and it is important that we do not make changes that significantly increase the amount of time it takes to run. Since MCL must run in real time, whatever processing is necessary to update the motion model must not delay localization. With these requirements in mind, our dynamic motion model MCL algorithm provides a minor alteration that allows the parameters of the motion model to be recalculated and used.

At each MCL update step a \( \{ r, \theta, r, \theta \} \) data point is recorded. When enough new data points are recorded to make it worthwhile to calculate new parameters, the equation is maximized in the background, using whatever power is available when localization is finished. When the maximization is complete, the new parameters are reported to the MCL algorithm. In fact, MCL itself is unaware of the changing parameters, since it just runs normally.

In order to reduce the complexity of the calculation, only the most recent set of errors are used. When a predetermined number of corrections are recorded, each subsequent observation causes the oldest observation to be removed. This creates an upper bound for the maximization routine and also allows the dynamic model to update to changing conditions. For example, if the robot’s tires deflate, or water is spilled on the floor, the motion of the robot would change. In that case, after a certain number of updates, all of the old data would be removed and the model would be calculated entirely based on the changed conditions.

In order to accommodate different conditions in different areas, data points are not stored globally but are instead recorded by region. Each region of the map has its own collection of data. If there are insufficient points to calculate the parameters then the previous parameters are used. However, once the robot traverses an area enough that it can update the motion model, it calculates the parameters and stores them with the area. When it subsequently enters the same region, it can load the specific parameters. Any reasonable algorithm for defining regions can be used, smaller regions will be more accurate but will take longer to receive enough data, while larger regions will update sooner but may represent multiple conditions.

The results of this dynamic motion model algorithm are a map annotated with the motion model parameters for different regions. Aside from changing the motion model during execution, the map can also be used to provide additional data for planning or analysis. For example, if a region causes a high variance, then it might be better for the robot to avoid that region when path planning. Also, a significant change in variance might indicate some kind of spill that should be dealt with. A robot might also use the different parameters to identify different surfaces in the environment for another machine, perhaps planning a route that avoids certain kinds of surface.

Although creating dynamic motion models uses successful localization to correct errors in the model, it does not preclude using the same data to correct other errors. In particular, it is possible to
dynamically update the map of the environment as in (Milstein, 2005), while simultaneously dynamically updating the motion model. In fact, using both of these together causes them both to work better than either one alone. There is no reason why other parameters could not also be dynamically updated at the same time.

4 RESULTS

The dynamic motion model algorithm was tested using a 2 wheeled Pioneer 3-DX differential drive holonomic robot equipped with a 180 degree SICK laser rangefinder. Data gathered by the robot over a traversal of the environment was processed by both the normal MCL algorithm and various implementations of the dynamic motion model MCL algorithm. The parameters of the motion model were calculated by maximizing the equations as described using Matlab’s ‘fminsearch’ function. Dynamic map MCL (Milstein, 2005) was also used to see if the two dynamic methods could be used simultaneously. The results show a marked improvement using dynamic motion models.

At first, standard MCL was used with some default parameters for this class of robot. Although these parameters work, they are general, high variance parameters that have not been specifically adapted to either the robot or the environment. With these parameters the average error was 1.7% for range and 4.5% for angle.

Figure 1: error vs. range for default parameters.

Figure 1 shows the error in range versus distance moved for standard MCL. Because it is impossible to separate the angle error caused by turning from the angle error caused by range any graph of angle error is not useful.

Next, the dynamic motion model algorithm was used to calculate parameters based on the entire data set and MCL was run with these motion model parameters. The resulting error was 1.0% for range and 2.9% for angle. Of course, in practice this method is impossible, because it involves knowing the observations that will be made before they are actually recorded. In practice, this method can be approximated by using a previous data set on the same environment to calculate the parameters. Figure 2 shows these motion parameters in action.

Figure 2: error vs. range for global optimization.

The third test involved dynamic motion models with global data. The parameters were updated during execution according to the preceding localization corrections. With this method 1.2% range error and 2.6% angle error was recorded.

Finally, the full dynamic motion model algorithm was used. Each region of the map, identified by the small circles, was updated with its own data and produced its own corrections. This technique produced an error of 1.4% for range and 2.8% for angle with characteristics as shown in figure 3.

Figure 3: error vs. range for regional dynamic.
As these results show, dynamic motion models are better able to represent the robot’s motion, and localization becomes more accurate. Table 1 shows a comparison of the various methods. While all of the dynamic methods give similar results, they are far superior to the static motion model method that is the base case. The particular method that is optimal in any given situation depends on the environment, although over the long run, the full dynamic technique should produce the minimum error. However, this convergence may require a large number of traversals in order to get the necessary number of data points for each region. Until execution reaches this point, the other techniques have a temporary advantage, since they require less data.

Table 1: Results of all algorithms.

<table>
<thead>
<tr>
<th>Method</th>
<th>% range error</th>
<th>% angle error</th>
</tr>
</thead>
<tbody>
<tr>
<td>Default static</td>
<td>1.6592%</td>
<td>4.5311%</td>
</tr>
<tr>
<td>Optimal static</td>
<td>1.0428%</td>
<td>2.9509%</td>
</tr>
<tr>
<td>Global dynamic</td>
<td>1.2418%</td>
<td>2.6320%</td>
</tr>
<tr>
<td>Regional dynamic</td>
<td>1.3882%</td>
<td>2.7878%</td>
</tr>
</tbody>
</table>

The technique of calculating the global optimum parameters provides very good results, especially in an environment like this with little change in surface. Range error especially benefits from this technique, since it is relatively constant. However, generating this model requires manual collection and processing of data before execution, which somewhat defeats the purpose of a dynamic algorithm. The benefit is that offline processing can handle a larger number of data points, resulting in more accurate parameters. Of course, any changes, such as tire pressure, will invalidate the model. Although this technique uses part of the dynamic algorithm, it is not truly dynamic nor is it usually a practical method.

The choice between the two dynamic techniques depends on the circumstances. If the environment has different surfaces then having the parameters change with the region provides a benefit. If, on the other hand, the surfaces are constant but the robot changes conditions, a globally dynamic technique will update more quickly, since the data points are all processed into the same model. A situation where this is useful might be when the robot changes its behaviour as its battery drains. The global technique could adapt faster to changing robot conditions, but it cannot recognize different surfaces. Note that the regional algorithm will eventually adapt to global conditions, but it will require more data since each region must be updated. The choice depends strongly on the environment, although the regional method is more adaptable.

These results demonstrate that adding dynamic motion models to MCL provides a benefit to localization. Although slightly different dynamic techniques provide different advantages, they are all superior to the static technique. Aside from the tests described above, several other data sets in different environments were examined, with similar results. One such test involved a similar robot in a different building where the floor was carpeted instead of concrete. The map of the environment incorporated a serious error that caused localization to fail for most techniques. One corridor was actually much shorter than it appears in the map, causing motion along part of that corridor to have a large bias. Because of this, the range error in the dynamic techniques actually increases, as they increase the variance to handle the error. Only the regionally dynamic technique was able to successfully localize in this environment.

Table 2: Results of all algorithms for high error data.

<table>
<thead>
<tr>
<th>Method</th>
<th>% range error</th>
<th>% angle error</th>
</tr>
</thead>
<tbody>
<tr>
<td>Default static</td>
<td>7.2343%</td>
<td>5.9671%</td>
</tr>
<tr>
<td>Optimal static</td>
<td>8.6733%</td>
<td>1.3428%</td>
</tr>
<tr>
<td>Global dynamic</td>
<td>9.5313%</td>
<td>1.4835%</td>
</tr>
<tr>
<td>Regional dynamic</td>
<td>10.9178%</td>
<td>1.7166%</td>
</tr>
</tbody>
</table>

5 CONCLUSION

We have derived and implemented a technique for dynamically calculating the parameters of the Monte Carlo Localization motion model during ordinary execution of the algorithm. Our technique requires very little overhead and provides a strong benefit over the ordinary technique of using a static model determined experimentally from a similar robot. In fact, the most common current technique is to estimate the model and modify it using trial and
error until localization is successful. The problem is that performing experiments to determine the parameters is a difficult and laborious process. Since the parameters of a real environment change over time, it is usually not worthwhile to develop an accurate model when an approximate one will still allow MCL to function. Our dynamic motion model technique provides a viable alternative to both these methods, allowing an accurate model to be created and maintained without requiring skilled user input. Since the frequency and size of the updates can be modified to suit the platform, there is no reason not to use a dynamic model. Because MCL is running properly when the dynamic algorithm is active, there is no urgency in processing the error data into new parameters. Thus the additional run time required can be limited to what is available on the particular platform. Allocating more time will result in more frequent updates, but since the alternative is no updates there is no reason not to use even the slowest possible rate. In fact, very good results can be obtained by using offline processing to determine a new model whenever conditions change. Although the offline method does not provide all the benefits of our full regional dynamic algorithm, it provides a great improvement over the default method.

Another benefit of having dynamic motion models is that they can be used to automatically optimize a robot to different conditions in the environment. This may be an important feature for a robot that runs autonomously between different areas. It is impractical to perform laborious experiments to determine an optimal model for different regions, but a general model can be automatically refined into specific models for many different conditions.

By reducing the error due to the motion model in MCL, our technique provides localization with greater resilience to errors from other causes. The more accurate the various models are, the more tolerance MCL has towards random events that might otherwise cause it to fail. In some circumstances this may be a major benefit, but even if ordinary MCL is successful in an environment, a more accurate model cannot harm its execution.

Since dynamic motion model MCL provides an annotated map which includes motion model parameters, it may be possible to use those parameters in order to determine information about the environment. For example, by discovering the parameters caused by various types of surface, the robot might be able to identify those same surfaces if it encountered them again. Also, the motion models might be taken into account in path planning in order to give the robot a preference for stable surfaces.

Finally, a robot might detect a change in its parameters and use them to identify a malfunction, such as deflated tires. These uses for dynamic motion models would provide additional benefits to the algorithm, above the improvements it makes to localization.

**REFERENCES**


