

AUTONOMOUS GAIT PATTERN FOR A DYNAMIC BIPED WALKING

Christophe Sabourin, Kurosh Madani

*Laboratoire Images, Signaux, et Systèmes Intelligents (LISSI EA / 3956)
Université Paris-XII, IUT de Sénart, Avenue Pierre Point, 77127 Lieusaint, France.*

Olivier Bruneau

*Laboratoire Vision et Robotique - Ecole Nationale Supérieure d'Ingénieurs de Bourges
10 Boulevard Lahitolle 18020 BOURGES, France.*

Keywords: Autonomous gait pattern, biped dynamic walking, Fuzzy-CMAC neural networks.

Abstract: In this paper, we propose an autonomous gait pattern for a dynamic biped walking. Our approach takes simultaneously advantage from a Fuzzy-CMAC based computation of robot's swing leg's desired trajectory and a high level control strategy allowing regulating the robot's average velocity. The main interest of this approach is to proffer to the walking robot autonomy and adaptability involving only one parameter: the average velocity. Furthermore, this approach allows increasing the robustness of the walking robot regarding the forwards pushed force.

1 INTRODUCTION

The design and the control of biped robots are one of the more challenging topics in the field of robotics and were treated by a large number of research works over past decades. The potential applications of this research area are very foremost in the middle and long term. Indeed this can lead firstly to a better comprehension of the human locomotion mechanisms, what can be very helpful for the design of more efficient orthosis. Secondly, the humanoid robots are intended to replace the human for interventions in hostile environments or to help him in the daily tasks. However, in addition to the problems related to autonomy and decision of such humanoid robots, their basic locomotion task is still today a big challenge. If it is true that a number of already constructed prototypes, among which the most remarkable are undoubtedly the robots Asimo (1) and HRP-2P (2), have proved the feasibility of such robots, it is also factual that the performances of these walking machines are still far from equalizing the human's dynamic locomotion process. The design of new control laws allowing real time control for real dynamic walking in unknown environments is thus today fundamental. Moreover, such robots must be able to adapt themselves automatically to indoor and outdoor human environments. Consequently, it is necessary to develop more autonomous biped robots with robust control strategies in order to allow them, on the one hand to adapt their gait to the

real environment and on the other hand, to counteract external perturbations.

In the field of biped locomotion, the control strategies can be classified in two main categories. The first is based on a kinematics and dynamic modeling of the mechanical structure. This implies to identify perfectly the intrinsic parameters of biped robot's mechanical structure, requires a high precision measurement of the joints' angles, velocities and accelerations and needs a precise evaluation of interaction forces between feet and ground. Moreover, the control strategies based on a precise kinematics and dynamic modeling require a lot of computation. For all these reasons, the computing of the on-line trajectories generally are given by using a simplified modeling and the stability is ensured by the control of the Zero Moment Point (ZMP) (3) (4) (5) (6). The second solution consists to use the soft-computing techniques (fuzzy logic, neural networks, genetic algorithm, etc..) and/or pragmatic rules resulting from the expertise of the walking human. Two main advantages distinguish this second class of approaches. Firstly, it is not necessary to know perfectly the characteristics of the mechanical structure. Secondly, this category of techniques takes advantage from learning (off-line and/or on-line learning) capabilities. This last point is very important because generally the learning ability allows increasing the autonomy of the biped robot.

In this paper, we present a control strategy for



Figure 1: Prototype RABBIT.

an under-actuated robot: RABBIT (figure 1) (7) (8). This robot constitutes the central point of a project, within the framework of CNRS ROBEA program (9), concerning the control of walking and running biped robots, involving several French laboratories.

This robot is composed of two legs and a trunk and has no foot as shown on figure 1. If it is true, from design point of view, that RABBIT is simpler compared to a robot with feet, from the control theory point of view, the control of this robot is a more challenging task, particularly because, in phase of single support, the robot is under-actuated. In fact, this kind of robots allows studying real dynamical walking leading to the design of new control laws in order to improve biped robots' current performances. It is pertinent to note that the ZMP approach, generally used for humanoid robots, is not appropriated for the case of a biped without feet, because the contact surface between the foot and the ground is limited to a point.

This project has been the subject of many publications concerning the field of control strategies emerging on the one hand from rigorous mathematical modeling, and on the other hand issued from the use of CMAC neural networks. Developed approaches have been subject of experimental validations (10) (11). In this paper, we present an extension of the control strategy using the CMAC neural network. In our previous work (10), the CMAC was used to generate the joint trajectories of the swing leg but these trajectories were fixed. Consequently, the step length could not be changed during the walking. Today, our aim is to develop a control strategy able to generate a fully autonomous biped walking based on a soft-computing approach. In this paper, we show how it is possible to change the walking gait by using the fusion of different trajectories learned by several CMAC neural networks. In fact, our control strategy is based on two stages :

- The first one uses a set of pragmatic rules allowing to stabilize the pitch angle of the trunk and to generate the leg motions (12). This control strategy allows generating a stable dynamic walking with step length and velocity transitions. During this first stage, the robot is supposed to move in an ideal environment (without disturbance). We also assume that frictions are negligible. However, in the case of our intuitive control, it is not possible to counteract external (pushed force) and internal (friction) disturbances. Consequently, we propose to use a neural network allowing to increase the robustness of our control strategy. In fact, in the first stage, the pragmatic rules are used as a reference control to learn, by a set of CMAC neural networks, a set of joint trajectories.
- In the second stage, we use these neural networks to generate and to modulate the trajectory of the swing leg. This trajectory is obtained by fusing outputs of several neural networks. In fact, the data contained in each CMAC represent a reference walking carried out during the first stage. The fusion is realized by using fuzzy logic. Consequently, it is possible to modulate, for example, step length according to average velocity. Furthermore, the fusion allows us to generate an infinity of trajectories only from a limited number of walking references.

This paper is organized as follows. Section 2 presents the characteristics of our virtual under-actuated robot. In Section 3, we explain the method used to train each CMAC neural network. Section 4 presents the control strategy using the Fuzzy-CMAC neural networks. In section 5, we give the main results obtained in simulation. Conclusions and further developments are finally given.

2 VIRTUAL MODELING OF THE ROBOT

The robot RABBIT has only four articulations: one for each knee, one for each hip. Motions are included in the sagittal plane by using a radial bar link fixed at a central column that allows to guide the direction of progression of the robot around a circle. Each articulation is actuated by one servo-motor RS420J. Four encoders make it possible to measure the relative angles between the trunk and the thigh for the hip, and between the thigh and the shin for the knee. Another encoder, installed on the bar link, allows to give the pitch angle of the trunk. Two binary contact sensors detect whether or not the leg is in contact with the ground. Based on the informations given by encoder, it is possible to calculate the step length L_{step} when the two legs are in contact with the ground. The dura-

tion of the step t_{step} is computed by using the contact sensor informations (duration from takeoff to landing of the same leg). Furthermore, it is possible to estimate the average velocity V_M by using (1).

$$V_M = \frac{L_{step}}{t_{step}} \quad (1)$$

The characteristics (masses and lengths of the limbs) are summarized in table 1. Since the contact between the robot and the ground is just one point (passive DOF), the robot is under-actuated during the single support phase: there are only two actuators (at the knee and at the hip of the contacting leg) to control three parameters (vertical and horizontal position of the platform and pitch angle). In fact, this robot represents the minimal system able to generate a biped walking and running gaits.

Table 1: Masses and lengths of the limbs of the robot.

Limb	Weight (Kg)	Length (m)
Trunk	12	0.2
Thigh	6.8	0.4
Shin	3.2	0.4

The numerical model of the robot previously described was designed with the software ADAMS¹ (Fig. 2).

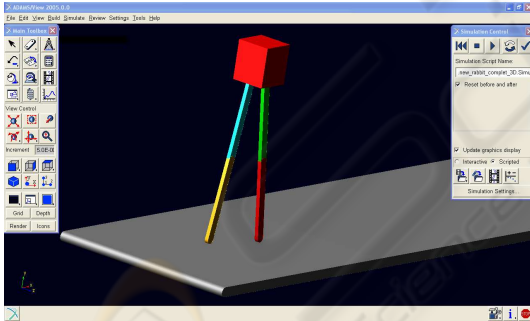


Figure 2: Modeling of the robot with ADAMS.

This software, from the modeling of the mechanical system (masses and geometry of the segments) is able to simulate the dynamic behavior of this system and namely to calculate the absolute motions of the platform and the relative motions of the limbs when torques are applied on the joints by the virtual actuators. Figure 3 shows references for the angles and the torques required for the development of our control strategy. q_{i1} and q_{i2} are respectively the measured angles at the hip and the knee of the leg i . q_0 corresponds

¹ ADAMS is a product of MSC software

to the pitch angle. T_{knee}^{sw} and T_{hip}^{sw} are the torques applied respectively at the knee and at the hip during the swing phase, T_{knee}^{st} and T_{hip}^{st} are the torques applied during the stance phase.

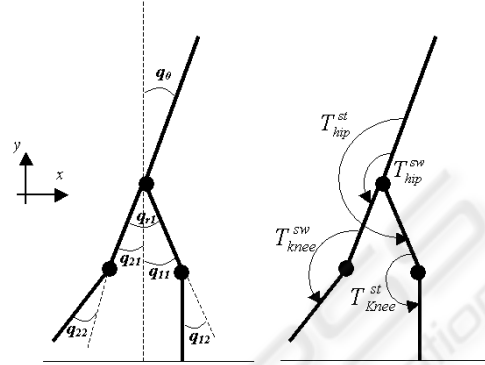


Figure 3: Parameters for angles and torques.

The model used to simulate the interaction between feet and ground is exposed in (13). The normal contact force is given by equation (2):

$$F_c^n = \begin{cases} 0 & \text{if } y > 0 \\ -\lambda_c^n |y| \dot{y} + k_c^n |y| & \text{if } y \leq 0 \end{cases} \quad (2)$$

Where y and \dot{y} are respectively the position and the velocity of the foot (limited to a point) with regard to the ground. k_c^n and λ_c^n are respectively the generalized stiffness and damping of the normal forces. They are chosen in order to avoid the rebound and to limit the penetration of the foot in the ground. The tangential contact forces are computed with the equation (3) in the case of a contact without sliding or with the equation (4) if sliding occurs.

$$F_c^t = \begin{cases} 0 & \text{if } y > 0 \\ -\lambda_c^t \dot{x} + k_c^t (x - x_c) & \text{if } y \leq 0 \end{cases} \quad (3)$$

$$F_c^t = \begin{cases} 0 & \text{if } y > 0 \\ -(sgn(\dot{x})) \lambda_g F_c^n - \mu_g \dot{x} & \text{if } y \leq 0 \end{cases} \quad (4)$$

Where x and \dot{x} are respectively the position and the velocity of the foot with regard to the position of the contact point x_c at the instant of impact with ground. k_c^t and λ_c^t are respectively the generalized stiffness and damping of the tangential forces. λ_g is the coefficient of dynamic friction depending on the nature of surfaces in contact and μ_g a viscous damping coefficient during sliding. After each iteration, the normal and tangential forces are computed from the equations (2) and (3). But, if F_c^t is located outside the cone of friction ($\|F_c^t\| > \mu_s \|F_c^n\|$ with μ_s the static friction coefficient), then the tangential force of contact is computed with equation (4). The interest of this

model is that it is possible to simulate walking with or without phases of sliding allowing us to evaluate the robustness of the control.

Within the framework of a real robot's control, the morphological description of this one is insufficient. It is thus necessary to take into account the technological limits of the actuators in order to implement the control laws used in simulation on the experimental prototype. From the characteristics of servo-motor RS420J used for RABBIT, we thus choose to apply the following limitations :

- when velocity is included in $[0; 2000]rpm$, the torque applied to each actuator is limited to $1.5Nm$ what corresponds to a torque of $75Nm$ at the output of the reducer (ration gear equal to 50),
- when velocity is included in $[2000; 4000]rpm$ the power of each actuator is limited to $315W$,
- when the velocity is bigger than $4000rpm$, the torque is imposed to be equal to zero.

3 TRAINING OF CMAC NEURAL NETWORKS

In this section, we present firstly the CMAC neural network and secondly, the principle which we use to train the CMAC.

3.1 CMAC Neural Networks

The CMAC is a neural network imagined by Albus from the studies on the human cerebellum (14) (15). Despite its biological relevance, its main interest is the reduction of the training and computing times in comparison to other neural networks (16). This is of course a considerable advantage for real time control. Because of these characteristics, the CMAC is thus a neural network relatively well adapted for the control of complex systems with a lot of inputs and outputs and has already been the subject of some researches in the field of the control of biped robots (17) (18).

The CMAC is an associative memory type neural network which is a set of N detectors regularly distributed on several C layers. The receptive fields of these detectors are distributed on the totality of the limited range of the input signal. On each layer, the receptive fields are shifted of a quantification step q . Consequently, the widths of the receptive field are not always equal. The number of detectors N depends on the one hand of the width of the receptive fields and on the other hand of the quantification step q . When the value of the input signal is included in the receptive fields of a detector, this one is activated. For each value of the input signal, the number of activated detector is equal to the number of layers C (parameter

of generalization). Figure 4 shows a simplified organization of the receptive fields having 14 detectors distributed on 3 layers. Being given that there is an overlapping of the receptive fields, neighboring inputs will activate common detectors. Consequently, this neural network is able to carry out a generalization of the output calculation for inputs close to those presented during learning.

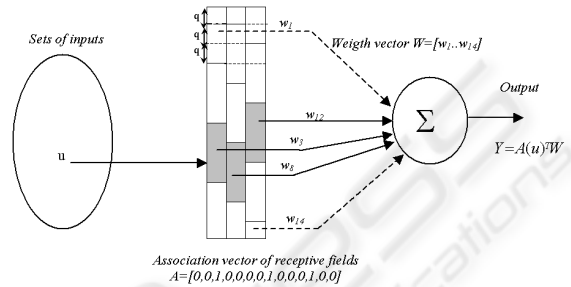


Figure 4: Description of the simplified CMAC with 14 detectors distributed on 3 layers. For each value of the input signal, the number of activated detector is equal to 3. $A = [0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0]$, $Y = A(u)^T W = w_3 + w_8 + w_{12}$.

The output Y of the CMAC is computed by using two mappings. The first mapping projects an input space point u into a binary associative vector $A = [a_1..a_N]$. Each element of A is associated with one detector and N is the number of detector. When one detector is activated, the corresponding element A of this detector is 1 otherwise it is equal to 0. The second mapping computes the output Y of the network as a scalar product of the association vector A and the weight vector $W = [w_1..w_N]$ (equation (5)).

$$Y = A(u)^T W \quad (5)$$

3.2 Learning Phase

During this learning phase, we use an intuitive control allowing us to perform dynamic walking of our virtual under-actuated robot without references trajectories. This intuitive control strategy is based on three points:

- the observation of the relations between joint motions and the evolution of the parameters describing the trajectory of the robot platform,
- an interpretation of the muscular behavior,
- the analysis of the intrinsic dynamics of a biped.

Based on these considerations, it is possible to determine a set of pragmatic rules. The objective of this strategy is to generate the movements of the legs by using a succession of passive and active phase. Also, it is possible to modify step length, average velocity

by an adjustment of several parameters (12). Consequently, this approach allow us to generate several reference trajectories which are learned by several CMAC neural networks.

Figure 5 shows the method used during this training phase. The trajectories of the swing leg (in terms of joint positions and velocities) are learned with four "single-input/single-output" $CMAC_k$ ($k = 1, \dots, 4$) neural networks. Indeed, two CMAC are necessary to memorize the joint angles q_{i1} and q_{i2} and two other CMAC for angular velocities \dot{q}_{i1} and \dot{q}_{i2} . q_{i1} and q_{i2} are respectively the measured angles at the hip and the knee of the leg i ; \dot{q}_{i1} and \dot{q}_{i2} are respectively the measured angular velocities at the hip and the knee of the leg i .

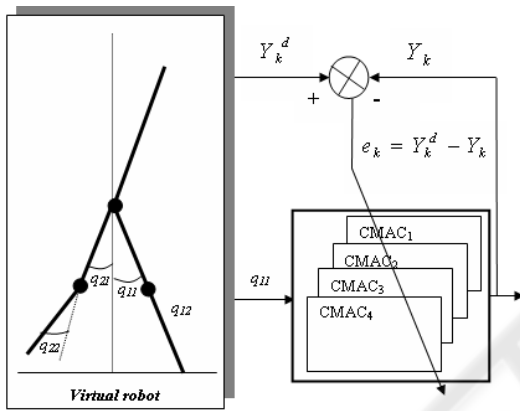


Figure 5: Principle of the learning phase of CMAC neural network ($u = q_{11}$).

When leg 1 is in support ($q_{12} = 0$), the angle q_{11} is applied to the input of each $CMAC_k$ ($u = q_{11}$) and when leg 2 is in support ($q_{22} = 0$), this is the angle q_{21} which is applied to the input of each $CMAC_k$ ($u = q_{21}$). Consequently, the trajectories learned by the neural networks are not function of time but function of the geometrical pattern of the robot. Furthermore, we consider that the trajectories of each leg in swing phase are identical. This allow on the one hand to divide by two the number of CMAC and on the other hand to reduce the training time. The weights of each $CMAC_k$ are updated by using the error between the desired output Y_k^d of each $CMAC_k$ and the computed output Y_k of each $CMAC_k$.

4 CONTROL STRATEGY USING FUZZY-CMAC

Figure (6) shows the global strategy which is used to control the walking robot. It should be noted that the

architecture of this control can be decomposed into three parts:

- The first is used to compute the trajectory of the swing leg from several output of the $CMAC_k$ neural networks and a Fuzzy Inference System.
- The second allows regulating the average velocity from a modification of the desired pitch angle.
- The third is composed by four PD control in order to ensure the tracking of the reference trajectories at the level of each articulation.

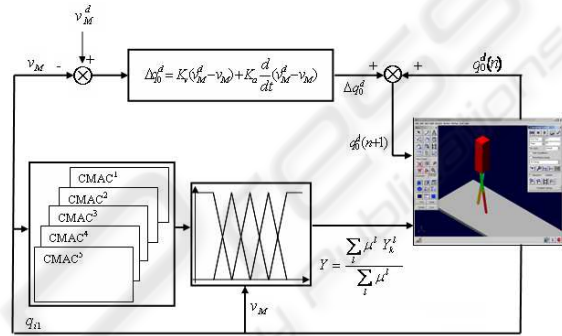


Figure 6: Principle of the control strategy used Fuzzy-CMAC trajectories.

4.1 Reference Trajectories

During the training stage, five trajectories with an average velocity V_M included in $[0.4..0.8]m/s$ have been learned by five $CMAC^l$. Each $CMAC^l$ is composed of four single input/single output $CMAC_k$ (two $CMAC_k$ for the angular positions q_{i1} and q_{i2} and two other $CMAC_k$ for the angular velocities \dot{q}_{i1} and \dot{q}_{i2}). Table 2 gives the main parameters which are used during the learning phase according to the desired average velocity V_M , where V_M is calculated by using (1). q_r^d and q_0^d are respectively the desired relative angle between the two thighs and the desired pitch of the trunk. q_{sw}^d corresponds to the desired angle of the knee at the end of the knee extension of the swing leg just before the double contact phase.

Table 2: Parameters used during the learning stage.

	$V_M(m/s)$	$q_r^d(^{\circ})$	$q_{sw}^d(^{\circ})$	$q_0^d(^{\circ})$
$CMAC^1$	0.4	20	-7	3.5
$CMAC^2$	0.5	25	-10	3
$CMAC^3$	0.6	30	-15	2.5
$CMAC^4$	0.7	35	-20	8
$CMAC^5$	0.8	40	-25	8

It must be pointed out that the step length L_{step} increases when V_M increases. Table (3) gives L_{step} according to V_M .

Table 3: V_M and L_{step} for the five references trajectories.

	$V_M(m/s)$	$L_{step}(m)$
$CMAC^1$	0.4	0.23
$CMAC^2$	0.5	0.28
$CMAC^3$	0.6	0.31
$CMAC^4$	0.7	0.36
$CMAC^5$	0.8	0.4

4.2 Fuzzy-CMAC Trajectories

During the walking, the measured angle q_{11} , if leg 1 is in support, or q_{21} , if leg 2 is in support, is applied at each input of each $CMAC_k^l$. The desired angular position q_{i1}^d and q_{i2}^d , and the desired angular velocity \dot{q}_{i1}^d and \dot{q}_{i2}^d are carried out by using a fusion of the five learned trajectories. This fusion is realized by using a Fuzzy Inference System (FIS). This FIS is composed of five rules:

- IF V_M IS *VerySmall* THEN $Y = Y^1$
- IF V_M IS *Small* THEN $Y = Y^2$
- IF V_M IS *Medium* THEN $Y = Y^3$
- IF V_M IS *Big* THEN $Y = Y^4$
- IF V_M IS *VeryBig* THEN $Y = Y^5$

Where Y^l corresponds at the output of the $CMAC^l$. Figure 7 shows the membership functions. The average velocity is modeled by five fuzzy sets (VerySmall, Small, Medium, Big, VeryBig). Each desired trajectory Y_k is computed by using equation (6).

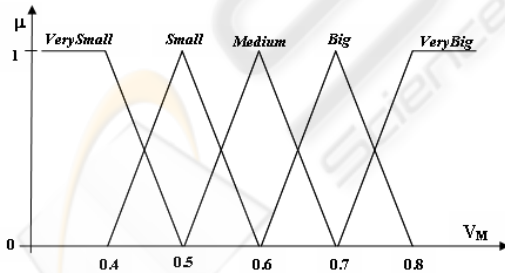


Figure 7: Membership functions used to compute the FuzzyCMAC trajectories.

$$Y_k = \frac{\sum_{l=1}^5 \mu^l Y_k^l}{\sum_{l=1}^5 \mu^l} \quad (6)$$

Consequently, the trajectory depends on the one hand of the geometrical position of the stance leg and on the other hand of the measured average velocity.

4.3 High Level Control

The high level control allows us to regulate the average velocity by adjusting the pitch angle of the trunk at each step by using the error between the average velocity V_M and the desired average velocity V_M^d and of its derivative as described in figure 6.

At each step, Δq_0^d , which is computed by using the error between V_M and V_M^d and of its derivative (equation 7), is then added to the pitch angle of the previous step $q_0^d(n)$ in order to carry out the new desired pitch angle of the following step $q_0^d(n+1)$ as shown in equation (8).

$$\Delta q_0^d = K^p(V_M^d - V_M) + K^v \frac{d}{dt}(V_M^d - V_M) \quad (7)$$

$$q_0^d(n+1) = q_0^d(n) + \Delta q_0^d \quad (8)$$

4.4 PD Control

In order to ensure the tracking of the desired trajectories, the torques T_{knee} and T_{hip} applied respectively at the knee and at the hip are computed by using PD control. During the swing stage, the torques are carried out by using equations (9) and (10). q_{ij}^d and \dot{q}_{ij}^d are respectively the reference trajectories (position and velocity) of the swing leg from the output of the Fuzzy-CMAC ($j = 1$ for the hip, $j = 2$ for the knee).

$$T_{hip}^{sw} = K_{hip}^p(q_{i1}^d - q_{i1}) + K_{hip}^v(\dot{q}_{i1}^d - \dot{q}_{i1}) \quad (9)$$

$$T_{knee}^{sw} = K_{knee}^p(q_{i2}^d - q_{i2}) + K_{knee}^v(\dot{q}_{i2}^d - \dot{q}_{i2}) \quad (10)$$

Secondly, the knee of the stance leg is locked, with $q_{i2}^d = 0$ and $\dot{q}_{i2}^d = 0$ (equation 11), and the torque applied to the hip allows to control the pitch angle of the trunk (equation 12). q_0 and \dot{q}_0 are respectively the measured absolute angle and angular velocity of the trunk. q_0^d is the desired pitch angle.

$$T_{knee}^{st} = -K_{knee}^p q_{i2} - K_{knee}^v \dot{q}_{i2} \quad (11)$$

$$T_{hip}^{st} = K_{trunk}^p(q_0^d - q_0) - K_{trunk}^v \dot{q}_0 \quad (12)$$

5 RESULTS

The control strategy presented in section 4 allows:

- To generate the joint trajectories of the swing leg from the geometrical configuration of the robot and the real average velocity.
- To regulate, at each step, the average velocity thanks to an adjustment of the pitch angle.

The main interest of this approach is that the walking robot is autonomous and is able to adapt, for example, the step length from only one parameter: the average velocity. Furthermore, if the robot is pushed forwards, the average velocity increases and consequently the step length increases too. In this manner, it is easier for the robot to compensate this kind of perturbation.

5.1 Autonomous Walking Gait

Figure 8 shows the stick diagram of the walking of the robot when the desired average velocity increases. It must be noticed that the control strategy allows to adapt automatically the pitch angle and the step length as the human being.

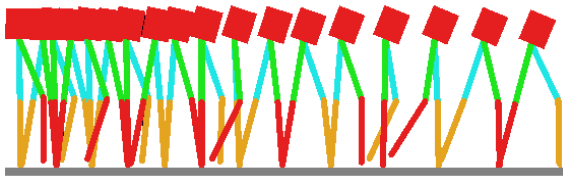


Figure 8: Stick diagram of the walking robot when the average velocity increases.

Figure 9 shows the desired average velocity V_M^d , the measured velocity V_M (equation 1) and the step length L_{step} . When V_M^d increases from $0.3m/s$ to $0.9m/s$, V_M increases gradually and converges towards the new value of V_M . L_{step} increases automatically from $0.25m$ to $0.4m$ from the measured average velocity at each step.

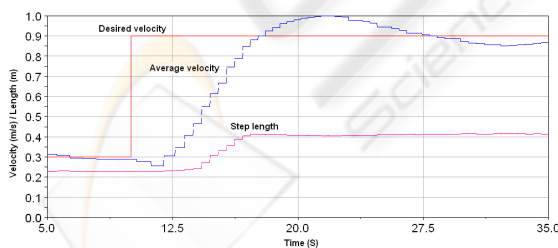


Figure 9: Average velocity and step length when the desired average velocity increase from $0.3m/s$ to $0.9m/s$.

It must be pointed out that the walking gait can depend to the desired average velocity V_M^d . But in this case, the step length transition is abrupt. Furthermore, the fact that the walking gait depends of the measured average velocity allows increasing the robustness of the walking of the robot.

5.2 Evaluation of the Robustness According to a Pushed Force

During walking, a robot moving in real environment can be subjected to external forces involving an imbalance. Consequently, the control strategy must react quickly in order to compensate this perturbation and to avoid the fall of the robot. Generally, when human being is pushed forwards, he increases the step length. In the case of the proposed control strategy, the step length depends of the real average velocity V_M . If the robot is pushed forwards, the duration of the step t_{step} decreases and consequently, V_M increases. In this manner, at the next step after this perturbation, L_{step} is adjusted.

The figure 10 shows the evolution of the average velocity before and after the force perturbation. At $t = 15s$, we applied on the trunk of the robot an impulsive pushed force. The duration and the amplitude of this force are respectively $0.2s$ and $50Nm$. Before this perturbation, the robot walks with an average velocity to $0.7m/s$ which corresponds at the desired average velocity. After this perturbation, V_M increases considerably but our control strategy allow to compensate slowly this perturbation.

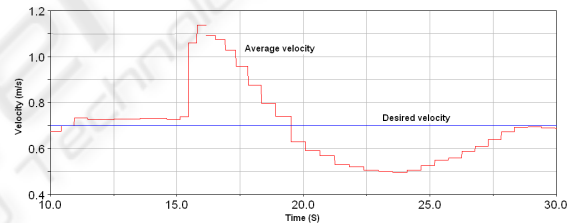


Figure 10: Average velocity V_M when the robot is pushed forwards at $t = 15s$.

The figures 11 and 12 show respectively the evolution of the step length and the pitch angle of the trunk. It must be pointed out that:

- L_{step} is adjusted automatically from the measured average velocity.
- The pitch angle of the trunk q_0^d decreases just after the application of the pushed force in order to slow down the velocity of the progression of the robot.

6 CONCLUSION

In this paper, we have proposed an autonomous gait pattern for a dynamic biped walking. Our approach is based firstly on Fuzzy-CMAC issued computation of robot's swing leg's desired trajectory and secondly on a high level control strategy allowing regulation

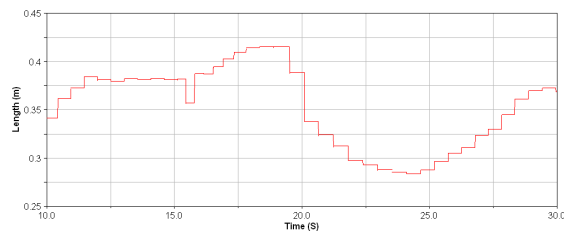


Figure 11: Step length L_{step} when the robot is pushed forwards at $t = 15s$.

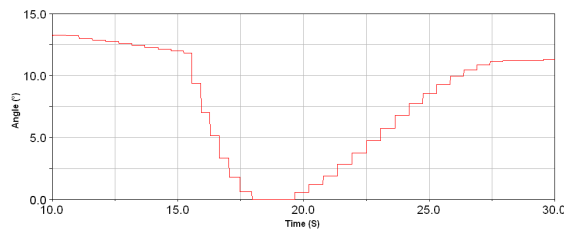


Figure 12: Pitch angle of the trunk when the robot is pushed forwards at $t = 15s$.

of the robot's average velocity. The main interest of this approach is to proffer to the walking robot autonomy and adaptability involving only one parameter: the average velocity. The obtained results show the adaptability of the walking step length and the issued additional robustness of the proposed control strategy. In fact, when the robot is pushed forwards, the average velocity increases and consequently the step length increases too. In this manner, it is easier to compensate this kind of perturbation.

Future works will focus firstly on the extension of the Fuzzy-CMAC approach in order to increase the autonomy of the walking robot according to the nature of the environment (get up and down stairs for instance), avoidance and dynamic crossing obstacles and secondly on the experimental validation of our approach.

REFERENCES

- Y. Sakagami, R. Watanabe, C. Aoyama, S. Matsunaga, N. Higaki, K. Fujimura. The intelligent ASIMO: system overview and integration. *Proc. IEEE Conf. on Intelligent Robots and Systems*, 2002, 2478–2483.
- K. Kaneko, F. Kanehiro, S. Kajita, H. Hirukawa, T. Kawasaki, M. Hirata, K. Akachi, T. Isozumi. Humanoid robot HRP-2. *Proc. IEEE Conf. on Robotics and Automation*, 2004, 1083–1090.
- M. Vukobratovic, B. Borovac. Zero moment point - thirty five years of its live. *International Journal of Humanoid Robotics*, 2004, Vol.1 N°1, 157–173.
- S. Kajita, F. Kanehiro, K. Kaneko, K. Fujiwara, K. Harada, K. Yokoi and H. Hirukawa. Biped walking pattern generation by using preview control of Zero-Moment Point. *IEEE Conf. on Robotics and Automation*, 2003, 1620–1626.
- Q. Huang, K. Yokoi, S. Kajita, K. Kaneko, H. Arai, N. Koyachi, K. Tanie. Planning walking patterns for a biped robot. *IEEE Transactions on Robotics and Automation*, 2001, Vol.17, N°3, 280–289.
- K. Hirai, M. Hirose, Y. Haikawa, T. Takenaka. The development of honda humanoid robot. *Proc. IEEE Conf. on Robotics and Automation*, 1998, 1321–1326.
- C. Chevallereau, G. Abba, Y. Aoustin, F. Plestan, E.R. Westervelt, C. Canudas-de-Wit, J.W. Grizzle. RABBIT: A testbed for advanced control theory. *IEEE Control Systems Magazine*, 2003, Vol.23, N°5, 57–79.
- <http://robot-rabbit.lag.ensieg.inpg.fr/>
- <http://www.laas.fr/robea/>
- C. Sabourin, O. Bruneau. Robustness of the dynamic walk of a biped robot subjected to disturbing external forces by using CMAC neural networks. *Robotics and Autonomous Systems*, 2005, Vol.23, 81–99.
- E.R. Westervelt, Gabriel Buche, J.W. Grizzle. Experimental validation of a framework for the design of controllers that induce stable walking in planar bipeds. *The International Journal of Robotics Research*, 2004, Vol.23 N°6, 559–582.
- C. Sabourin, O. Bruneau, J-G. Fontaine. Start, stop and transition of velocities on an underactuated bipedal robot without reference trajectories. *International Journal of Humanoid Robotics*, 2004, Vol.1, N°2, 349–374.
- O. Bruneau, F.B. Ouezdou. Distributed ground/walking robot interactions. *Robotica, Cambridge University Press*, 1999, Vol.17, N°3, 313–323.
- J. S. Albus. A new approach to manipulator control: the cerebellar model articulation controller (CMAC). *Journal of Dynamic Systems, Measurement and Control*, (1975), 220–227.
- J. S. Albus. Data storage in the cerebellar model articulation controller (CMAC). *Journal of Dynamic Systems, Measurement and Control*, 1975, 228–233.
- W. T. Miller, F. H. Glanz, L. G. Kraft. CMAC: An associative neural network alternative to backpropagation. *Proceedings of the IEEE, Special Issue on Neural Networks*, vol.78, N°10, 1990, 1561–1567.
- A. L. Kun, T. Miller. The design process of the unified walking controller for the UNH biped. *Proc. IEEE Conf. on Humanoid Robots*, 2000.
- A. Brenbrahim, J. Franklin. Biped dynamic walking using reinforcement learning. *Robotics and Autonomous Systems*, 1997, Vol.22, 283–302.