The Cooperative Hunters — Efficient Cooperative Search For Smart Targets Using UAV Swarms *

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Abstract. This work examines the Cooperative Hunters problem, where a swarm of UAVs is used for searching after one or more “smart targets” which are moving in a predefined area, while trying to avoid detection by the swarm. By arranging themselves into an efficient flight configuration, the UAVs optimize their integrated sensing capability, and are thus capable of searching much larger territories than a group of uncooperative UAVs. The problem was introduced in [1], while similar work appears also in [4–7]. This work presents two decentralized cooperative search algorithms which demonstrate major improvements over the algorithm and analysis presented in [1]. The first algorithm uses improved flying patterns which achieve superior search performance. An analytic optimality proof for the algorithm’s performance is presented. The second algorithm is a fault tolerant algorithm which allows the UAVs to search in areas whose shapes and sizes are unknown in advance (unlike the rectangular shapes only, in [1]). Due to space constraints many technical and experimental details were omitted. Such details will appear in a longer version of this work.

1 Introduction

Significant research effort has been invested during the last few years in design, analysis and simulation of multi-agents systems design for searching areas (either known or unknown) [4–7]. While in most works the targets are assumed to be idle, recent works consider dynamic targets, meaning — target which by detecting the searching agents from a long distance, try to avoid detection by evading the agents.

Such problem is presented in [1], where a swarm of UAVs is used for searching after one or more evading “smart targets” (i.e. a platoon of T-72 tanks, a squad of soldiers, etc"). The UAVs’ goal is to find the targets in the shortest time possible. While the swarm comprises relatively simple UAVs which lack prior knowledge of the initial positions of the targets, the targets possess full knowledge of the whereabouts of the swarm’s UAVs. The search strategy suggested in [1] defines flying patterns which the UAVs will follow, which are designed for scanning the (rectangular) area in such a way that the targets cannot re-enter sub-areas which were already scanned by the swarm, without being detected by some UAV. Note that this protocol assumes that the area in

* This research was partly supported by the Ministry of Science Infrastructural Grant No. 3-942
which the targets can move is known to the UAVs in advance, and must be rectangular in shape. Furthermore, the presented algorithm still requires a relatively high amount of explicit cooperation between the UAVs, which can be obtained through the use of a relatively high amount of communication.

This work presents two decentralized cooperative search algorithms which demonstrate major improvements over the algorithm and analysis presented in [1]. The first algorithm, discussed in section 2 uses improved flying patterns which enable the swarm to achieve superior search performance. The optimality of this search scheme is proved in section 2.3. The second algorithm, which is discussed in section 3 assumes no previous knowledge concerning the area to be searched, and uses only a limited communication between the UAVs. The algorithm is also highly fault-tolerant, meaning — even if many UAVs malfunction or be shot down, the swarm will still be able to complete the task, albeit slower.

2 HUNT-I Algorithm — Optimality in Rectangular Shapes

Let \( N, D, S, L \) and \( W \) denote the number of UAVs, the sensor recognition diameter, the line formation’s scan width, the length of the rectangular region and the width of the rectangular region, respectively (note that \( S = N \cdot D \)). Let \( V \) and \( v \) denote the speeds of the UAVs and the targets respectively.

In the algorithm of [1] the UAWs were designed to fly upwards and downwards in line formations parallel to the boundary of the region. In order to ensure that no target escapes into an already clean area, the rectangles formed by consecutive sweeps must overlap. Fig. 2 illustrates the algorithm. W.l.o.g., suppose \( S = 1 \). Since it takes \( \frac{2W + a}{V} \) for the UAVs to go to from one side of the rectangle to the opposite side, shift rightwards \( a \) and return, in order to ensure that the target do not move into an already cleared region while the UAVs are away, the rectangular scan bands need to have overlap of size \( (2W + a) \cdot v \). Since the overlap’s width is at most 1, the algorithm of [1] cannot complete the mission in case \( \frac{V}{v} \leq 2W \).

![Fig. 1. Illustration of the algorithm from Wincent et al. [1] (on the left) and our improved algorithm (on the right).](image-url)
2.1 Description of the Algorithm

Next, we show an algorithm that can guarantee locating the targets even if \( \frac{V}{v} \geq W + 1 \). Similarly to the algorithm of [1] we use upwards and downwards sweeping by a line formation of UAVs (as illustrated in Fig. 2). Again, we assume that \( S = 1 \).

Before each sweeping pass, the UAVs are placed in a line at either top or bottom side of the rectangle. In Fig. 2 we show two sweeping passes. Before the first and after the second pass the planes are at the top side of the rectangle (a light-gray rectangle shows the addition to the clean area after the two passes). The line formation first moves from \( BC \) to \( AD \). Before the stage begins at time \( t = 0 \), the area to the left of line \( BF \), filled with dark gray in Fig. 2, is already clean. Point \( A \) to which the left edge of UAV formation heads is chosen such that \( |AB|_V = |AF|_v \). Denote \( T = |AB|_V = |AF|_v \).

**Lemma 1.** When the formation reaches the lower side of the rectangle at time \( t = T \), the region to the left of line \( DJ \) is clean.

**Proof.** We separate the proof into two parts:

1. − No target can move to the left of line \( AB \). Suppose a target crosses the line at point \( Q \). By the choice of \( A \), if at time \( t = 0 \) the target was in \( Q \in [BF] \) and the UAV at \( B \), they reach location \( Z \), where \( Z \) is such that \( ZQ \) is parallel to axis \( X \), simultaneously and the target will not cross \( AB \) undetected.
   − If the target attempts to cross line \( AB \) at \( Z' \) (or \( Z'' \)), then it will not be able to do this, since even a target located in \( Q' \) (or \( Q'' \)) at \( t = 0 \) is not able to do this despite been nearer to \( Z' \) (or \( Z'' \)), respectively, than \( Z \).
2. A target cannot move into \( ABJD \). Indeed if it waits at line \( JD \) till the UAV formation passes and then heads leftwards, by the choice of point \( A \) the target will reach line \( JD \) at the same time as the formation reaches the bottom side of the area.

When the formation is at the segment \( AD \), it needs to shift rightwards to occupy segment \( EG \) such that the area to the left of \( E \) is clean. Hence \( E \) is chosen such that \( |AE|_V = |ED|_v \). This completes the description of one pass of the algorithm — as before the pass started when the region to the left of \( E \) is clean.

2.2 Analysis of the Algorithm

In this section we shall analyze the behavior of the algorithm for different values of \( V \), \( v \) and \( W \). First, let us see for which ratio \( \frac{V}{v} \), given \( W \), the algorithm succeeds.

**Lemma 2.** If \( \frac{V}{v} \geq W + 1 \) the formation is able to move forward.

**Proof.** In order for the algorithm to be able to move forward by some \( a > 0 \) the UAVs formation must be able to shift from \( AD \) to \( EG \) faster than the “target contaminated front” moving from \( DJ \) to \( KE \). Hence, it must hold that \( \frac{|AF|+a}{V} > \frac{|FD|-a}{v} \), where \( A \) is such that \( \frac{|BA|}{V} = \frac{|FA|}{v} \). That is, for the maximal possible propagation \( A \) we have:

\[
\begin{align*}
W^2 + (vT)^2 &= (VT)^2 \\
\frac{vT^2}{V} &= \frac{1-v-a}{v}
\end{align*}
\]
After some tedious calculations and denoting \( r = \frac{V}{v} \) we get:

\[
a(r, W) = \frac{r}{r+1} - \frac{W}{\sqrt{r^2 - 1}}
\]  

(2)

If \( r \) is such that \( a(r, W) > 0 \), the algorithm is able to complete the mission. Following some more computations we obtain a simpler looking lower bound on propagation after a single pass (Hence, for \( r \geq W + 1 \) the propagation is positive):

\[
a(r, W) > \frac{r}{r+1} \left( 1 - \frac{W}{r-1} \right)
\]  

(3)

Using the original notations, given a sensor recognition diameter \( D \), \( y \geq W + 1 \) is equivalent to the condition on the number of UAVs sufficient to guarantee completion:

\[
N = \frac{W}{(r - 1)D}
\]  

(4)

This can be compared to the bound from Wincent et al. [1]:

\[
N = \frac{2W}{rD}
\]  

(5)

Fig. 2. Illustration of a target attempting to cross into already clean region.

2.3 Lower Bound on the Number of UAVs — Optimality Proof

After we found in the previous section that if \( r \geq W + 1 \), mission completion is guaranteed, we would like to prove the following Lemma.

**Lemma 3.** If \( r < W \), the UAVs will not be able to complete the mission, independently of the algorithm they use.

**Proof.** Given an algorithm, denote with \( C(t) \) the convex hull of the region guaranteed to be clean of targets at time \( t \), by \( S(t) \) denote its area, and let us consider \( \frac{\partial S}{\partial t} \). We show that if \( t \) is such that \( S(t) = \frac{LW}{2} \), \( \frac{\partial S}{\partial t} < 0 \), proving that the algorithm will not be able to complete the mission. Denote with \( P(t) \) the length of the circumference of \( C(t) \) that is not part of the rectangle’s boundary. From geometric considerations, it can be seen that

\[
S(t + \Delta t) - S(t) < \Delta t S \cdot V - \Delta t P(S(t)) \cdot v
\]  

(6)
Recalling our assumption $S = 1$, we have:

$$\frac{\partial S}{\partial t} \leq v \cdot r (r - P(S(t))) \quad (7)$$

If we prove that for $t_0$ s.t. $S(t_0) = \frac{LW}{2}$ it holds that $P(S(t_0)) \geq W$, the claim of the Lemma will follow from the assumption $W > r$. The proof of the later is by consequently applying elementary geometric arguments to the cases of $C(t)$ having common points with 1 to 4 sides of the rectangle and is omitted. For instance, if $C(t_0)$ has common points with one side of the rectangle, then the circumference of $C(t)$ is at most $2P(t_0) \leq 2W$. Since of all shapes with the same area a circle has the greatest area, $S(t_0) \leq \frac{W^2}{\pi} < \frac{W^2}{2}$.

3 HUNT-II Algorithm — Simplicity and Robustness

Although the initial problem is that of searching for hiding targets within a given area, we shall consider an alternative, yet equivalent problem — the dynamic cooperative cleaners problem. The static variant of the cooperative cleaners problem is described and analyzed in [2], while the dynamic variant of the problem appears in [3]. This problem assumes a grid, part of which is ‘dirty’, where the ‘dirty’ part is a connected region of the grid. On this dirty grid region several agents move, each having the ability to ‘clean’ the place it is located in. The dynamic variant involves a deterministic evolution of the environment, simulating a spreading contamination (or fire).

Notice that from a cleaning protocol which is used by agents in order to solve the cooperative cleaners problem, a protocol for the swarm search problem can be derived. This is done by defining the entire area $G$ as ‘contaminated’. A ‘clean’ square (either a square which has not been contaminated yet, or a square which was cleaned by the UAVs) will represent an area which is guaranteed not to contain any target. By using the fact that the contamination is spreading, we simulate the fact that the targets may maneuver around the UAVs, in order to avoid detection — if vertex $v$ is contaminated then it may contain a target, thus, after $\frac{1}{v_{\text{target}}}$ time steps this target could have moved from $v$ to its neighbors, had it been in $v$ (when $v_{\text{target}}$ is the speed of the targets). As a result, after $\frac{1}{v_{\text{target}}}$ time steps all the neighbors of $v$ become contaminated. In other words, the spreading contamination acts as a danger diffusion which simulates the capability of a square to contain a target. The agents’ goal is to eliminate the contaminated area — eliminate the places which the targets may be hiding in. Once there are no longer squares in which the targets may be hiding, the swarm is guaranteed to have detected all evading targets. Note that our demands regarding no prior knowledge of the search area are met, since the cooperative cleaners problem do not assume such knowledge.

3.1 Swarm Search Algorithm

Let each UAV $i$ hold $G_i$ — a bitmap of $G$. Let every $G_i$ be initialized to zeros (e.g. “clean”). Let each UAV $i$ contain a hash table of vertices — $f_i$, which for every vertex can return on or off. The default for all the vertices is off. The list $f_i$ represents the vertices which are known to be within the area to be searched.
Every time a UAV flying over vertex \( v \) identifies \( v \) or one of its neighbors to be a part of the area to be searched, if \( f_i(v) = \text{off} \) it sets the corresponding vertices of \( G_i \) to 1, sets \( f_i(v) \) to be \text{on} and broadcasts this information to the other UAVs. Once a UAV receives a transmission that vertex \( v \) is part of the area to be searched, it sets \( f_i(v) \) to \text{on} and sets the corresponding vertex in \( G_i \) to 1. Every time a UAV moves it broadcasts the direction of its movement to the rest of the UAVs (north, south, west or east).

Notice that every time step each UAV broadcasts the new squares which are parts of \( G \) (which are set to 1 in \( G_i \)), and the squares it “cleaned” by flying over them (which are set to 0). Thus, the \( G_i \) and \( f_i \) of all UAVs are kept synchronized. Since \( v_{\text{target}} \) is known to the UAvs, they can simulate the spreading contamination, by performing \((\forall v \in G_i, \forall u \in \text{Neighbors}(v) : \text{state}(u) = 1)\) every \( \frac{1}{v_{\text{target}}} \) time steps. Thus, the bitmaps \( G_i \) always represent the correct representation of the area still to be cleaned.

The direction of movement and the decision whether or not to clean a vertex are determined using some cleaning protocol (for example, the SWEEP protocol of [3]). Notice that all the analytic bounds over the cleaning time of a cleaning protocol are immediately applicable for our hunting protocol. Whenever a UAV cleans a certain vertex, it sets this vertex in \( G_i \) to be 0, and broadcasts this information. Once a UAV receives such a transmission, it sets the vertex corresponding to the new location of the transmitting UAV to 0.

The UAvs are assumed to be placed on the boundary of the area to be searched. Thus, each \( G_i \) immediately contains at least one vertex whose value is 1. As a result, for \( G_i \) to contains only zeros, the UAvs must have visited all the vertices of \( G \) and had made sure that no target could have escaped and “re-contaminated” a clean square. When \( G_i \) becomes all zeros UAV \( i \) knows that the targets have been found, and stops searching.

Since each time step, each UAV can move in at most 4 directions (i.e. 2 bits of information), clean at most a single vertex (i.e. 1 bit of information), and broadcast the status of 8 neighbor vertices (i.e. 3 bits of information), the communication is limited to 6 bits of information per UAV per time step.

References