MULTIPLE VIEW GEOMETRY ESTIMATION BASED ON FINITE-MULTIPLE EVOLUTIONARY AGENTS FOR MEDICAL IMAGES

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Abstract: In this paper we present a new method for the robust estimation of the trifocal tensor, from a series of medical images, using finite-multiple evolutionary agents. Each agent denotes a subset of matching points for parameter estimation, and the dataset of correspondences is considered as the environment in which the agents inhabit, evolve and execute some evolutionary behavior. Survival-of-finite-fitness rule is employed to keep the dramatic increase of new agents within limits, and reduce the chance of reproducing unfit ones. Experiments show that our approach performs better than the typical methods in terms of accuracy and speed, and is robust to noise and outliers even when a large number of outliers are involved.

1 INTRODUCTION

Within recent years advances in the field of digital imaging have played a key role in medical industry. Medical imaging has progressed significantly throughout the years from X-Ray, CAT and PET scans to now using endoscopic cameras. Three-dimensional reconstruction methods are central to many new applications to medical imaging. In this research, we wish to generate 3D views of an endoscopic procedure, via a head up display unit, in order to enhance features, in particular obscured features, to the surgeon. However, the generation of exact 3D models from uncalibrated endoscopic camera image sequences is a challenging problem.

To generate these three dimensional views we need to know accurately the geometric information of the endoscopic camera. The trifocal tensor is the geometric entity that relates 3D points to three 2D views. In order to determine the trifocal tensor, for exact 3D reconstruction, we must extract interest points from the three images using the corner detector and then match potential features between these images.

In the past years, accurate and robust estimation of trifocal tensor has become an important and productive research area. The well-known robust methods are RANSAC (Random Sample Consensus Paradigm) (Torr, 1995), and its improvement MLESAC (Maximum Likelihood Sample Consensus) (Torr, 1997). Both methods randomly sample a subset of correspondences for geometric parameter estimation. However, the MLESAC method also employs additional statistical measures for the final solution. Both methods can deal with image noise and outliers, which are in gross disagreement with a specific postulated model. However, when a large number of outliers are involved they perform poorly.

Messy genetic algorithm (MGA) has also been used for trifocal tensor estimation (Hu, 2002). This method uses genes to denote triplets of correspondences and employs a genetic mechanism to improve the effectiveness of outlier detection. However, this method does not exploit the intrinsic parallelism between corresponding images and is therefore computational intensive. This is a defect of nearly all GA-based applications.

Recently, the authors proposed a simple evolutionary agent-based approach (SEA) to the problem of trifocal tensor estimation (Hu, 2004). This was found to improve the robustness of parameter estimation and reduce the computational
expense. However, through experimentation it was found that the simplicity of evolutionary operators caused the number of new generated agents to increase almost exponentially at early stages. Moreover, if there is no rule about termination, the method will spend a long time on convergence.

In this paper we present a new method for robust estimation of the trifocal tensor, from a series of medical images, using finite multiple evolutionary agents (FMEA). The dataset of correspondences is viewed as a one-dimensional cellular environment in which the agents inhabit and evolve. Each agent represents a subset for computing a unique trifocal tensor, and will execute some evolutionary behavior e.g. reproduction and diffusion. In this new method, the survival-of-finite-fitnes rule is introduced to limit the increase of new agents. During the diffusion process, after the comparison with their parents, the successful agents are sorted by their costs, and the best set of agents is kept active for evolutionary processing. Experiments show that the new FMEA approach performs better than the original SEA approach in terms of accuracy and robustness. This scheme provides a richer population based on evolutionary agents is presented in detail, including agent definition, cost function and evolutionary behavior. Section 4 deals with the experimental results obtained from synthetic data and real images. Finally, the conclusions are drawn in section 5.

2 BACKGROUND OF MULTIPLE VIEW GEOMETRY ESTIMATION

Consider a single point $M$ in space projected onto 3 views with camera matrices $\mathbf{P}$, $\mathbf{P'}$, $\mathbf{P''}$ with image points $\mathbf{m}$, $\mathbf{m'}$, $\mathbf{m''}$ respectively. Note that $\mathbf{M} = (x, y, 1, \lambda)^T$ for some scalar $\lambda$. Consider $\mathbf{P} = [\mathbf{I} | 0]$ and $\mathbf{P'} = [\mathbf{A} | \mathbf{v}]$ where $\mathbf{A}$ is the $3 \times 3$ principle minor of $\mathbf{P'}$ and $\mathbf{v}$ is the fourth column of $\mathbf{P'}$. Consider $\mathbf{m'} = \mathbf{P'M}$ and eliminate the scale factor:

$$x' = \frac{a_i}{a_i x} \cdot \frac{a_i \mathbf{m} + \lambda \mathbf{v_i}}{a_i x + \lambda \mathbf{v_i}}$$

where $a_i$ is the $i$th row of $\mathbf{A}$. These two equations can be written more compactly as follows:

$$\lambda s' v' + \mathbf{s'}^{\top} \mathbf{Am} = 0$$

$$\lambda s' v' + \mathbf{s'}^{\top} \mathbf{Am} = 0$$

where $s' = (-1, 0, x')$ and $s'' = (0, -1, y')$. Yet in a more compact form consider $s'$, $s''$ as row vectors of the matrix

$$s_j' = [-1, 0, x', 0, -1, y']$$

where $j = 1, 2, 3$ and $\mu = 1, 2$. Therefore, the compact form we obtain is described as follows:

$$\lambda s_j' v^{\mu} + \mathbf{m}^{\mu} s_j' a_i = 0 \quad \text{(1)}$$

where $\mu$ is a free index (i.e., we obtain one equation per range of $\mu$). Similarly, let $\mathbf{P'} = [\mathbf{B} | \mathbf{v}]$ for the third view $\mathbf{m}^3 = \mathbf{P'M}$ and let $r^3_j$ be the matrix,

$$r_j^3 = [-1, 0, x', 0, -1, y']$$

And likewise,

$$\lambda r_j^3 v^{\rho} + \pi r_j^3 b_i = 0 \quad \text{(2)}$$

where $\rho = 1, 2$ is a free index. We can eliminate $\lambda$ from (1) and (2) and obtain a new equation:

$$s_j' \mathbf{r}_j^3 (v^{\mu} b_i - v^{\rho} a_i) = 0$$

and the term in parenthesis is a trivalent tensor we call the trilinear tensor:

$$\mathbf{T}_j^3 = v^{\mu} b_i - v^{\rho} a_i \quad \text{(3)}$$

Hence, we have four trilinear equations (note that $\mu, \rho = 1, 2$). In a more explicit form, these trilinearity look like:

$$\begin{cases}
  x' T_{ij}^3 p' - x' x T_{ij}^3 p' + x' T_{ij}^3 p' - T_{ij}^3 p' = 0 \\
  y' T_{ij}^3 p' - y' y T_{ij}^3 p' + y' T_{ij}^3 p' - T_{ij}^3 p' = 0 \\
  x' T_{ij}^3 p' - x' y T_{ij}^3 p' + y' T_{ij}^3 p' - T_{ij}^3 p' = 0 \\
  y' T_{ij}^3 p' - y' y T_{ij}^3 p' + y' T_{ij}^3 p' - T_{ij}^3 p' = 0
\end{cases} \quad \text{(4)}$$

Equation (4) was first introduced by Shashua in 1995, from where we can see that the trifocal tensor has 27 elements, but only their ratios are significant, leaving 26 coefficients to be specified. And each triplet of matching points can provide four independent linear equations for the elements of the tensor. Therefore the tensor can be computed from a minimum of 7 triplets using Least-Squares methods.
3 MULTIPLE VIEW GEOMETRY ESTIMATION WITH FINITE MULTIPLE EVOLUTIONARY AGENTS

According to the description above, ideally every possible sub-sample (seven correspondences) of all the matching points \( n \) should be considered to obtain the optimal result. However this is usually computationally infeasible for most applications. So we apply finite multiple evolutionary agents to explore large uncertainty-parameter space and avoid getting trapped at a local minimum.

3.1 Agent definition

Suppose that \( S \) is the dataset of correspondences \( \{(m_i, m'_i, m''_i) | i = 1, \ldots, n\} \). It may be viewed as a one-dimensional grid of triplets of matching points, and also as an environment in which the agents inhabit and evolve. The goal of the evolutionary agents in \( S \) is to select the potential good points and search the preferred optimal subset. The evolutionary agent is defined as follows:

\[
\text{Agent} = \{V, \ a, \ D_{\text{cost}}, \ \text{fml}, \ \text{Rep}, \ \text{Diff}, \ \text{Die}\}
\]

\( V \) denotes the positions of an agent in \( S \), a seven-dimensional position vector, and \( V_k = \{i | i = 1, \ldots, n\} \), \( k = 1, \ldots, 7 \), is just the index number of correspondence lattice \( S \), as shown in Figure 1. In other words, \( V \) stands for the subset of correspondences for geometry estimation. \( a \) denotes the age of an agent, that is, the number of diffusion steps it has taken; \( D_{\text{cost}} \) symbolizes its cost, which indicates the adaptability of an agent and can be computed using the trilinear constraint obtained from the correspondences of \( V \); \( \text{fml} \) represents the family index, which indicates where an agent comes from. \( \text{Rep} \) denotes the reproduction behavior; \( \text{Diff} \) represents the diffusion behavior; while \( \text{Die} \) indicates that an agent has a life span.

3.2 Cost function

In this paper, we employ the seven-point method to get one possible solution of the tensor, although it could be estimated by six-point method (Quan, 1994). The reasons are as follows. Seven-point method is a simple linear approach, while six-point method is much complicated which includes parameterization of matrices, solving cubic constraint and linear equations. Moreover, the advantage of agent-based algorithm is that each agent performs a simple task, but they work together to solve a problem of great complexity by communicating and cooperating with each other. So the trade-off between accuracy and speed is to choose the seven-point method, which does not put a heavy burden on agents.

In order to compare the results of geometry estimation obtained from agents, the cost function is defined based on the residuals of correspondences

\[
R = \sum_{i=1}^{n} R_i = \sum_{i=1}^{n} d(m_i, \hat{m}_i) + d(m'_i, \hat{m}'_i) + d(m''_i, \hat{m}''_i)
\]

i.e., the sum of squared geometric distances between the measurements \( m_i, m'_i, m''_i \) and the corrected data points \( \hat{m}_i, \hat{m}'_i, \hat{m}''_i \), the latter obeying the trilinear constraint (3) for the estimated tensor \( T^o \). It indicates the distinction between the noisy measurements and the geometric elements (the true or equivalently the corrected data points). Then the cost function of an agent is defined by

\[
D_{\text{cost}} = \sum_{i=1}^{n} \alpha_i R_i + \sum_{i=1}^{n} \beta (1 - \alpha_i)
\]

where \( \alpha_i \) satisfies the following equation

\[
\alpha_i = \begin{cases} 1 & \text{if } R_i \leq \beta \quad \text{(inlier)} \\ 0 & \text{otherwise} \quad \text{(outlier)} \end{cases}
\]

\( \beta = 1.96 \sigma \) is the threshold for considering the inliers, and the standard deviation \( \sigma \) can be found as a maximum likelihood estimate using the median.
\[
\sigma = 1.4828 \left(1 + \frac{5}{n-q}\right) \text{median} |R_i|, \quad \text{where} \quad q \text{ is the number of parameters.}
\]

It can be seen that outliers are given a fixed penalty, but inliers are scored on how well they fit the data. In other words, the main consideration is given to the residuals of inliers and the outliers make a little contribution to the cost function.

### 3.3 Evolutionary behavior

Evolutionary agents adapt to their environment mainly by way of two behavioral responses, namely, reproduction and diffusion. Letting \( A^{(g)} \) represent the set of all active agents in generation \( g \), the evolutionary process is detailed in Figure 2.

1. **Reproduction:** In the reproduction process, each active agent \( \alpha^{(g)} \) will breed a finite number \( m_{\alpha} \) of offspring agents. The larger the value of \( m_{\alpha} \), the more offspring agents will be created to search in the large uncertain parameter space. However the computational cost will increase dramatically if no parallel processing is applied. It should be pointed out that the offspring, \( \alpha^{(g+1)} \), are by no means a simple copy of the parent \( \alpha^{(g)} \). The differences between \( \alpha^{(g)} \) and \( \alpha^{(g+1)} \) are mainly in the position vectors \( V^{(g)} \) and \( V^{(g+1)} \). \( m_{\alpha} \) elements of \( V^{(g)} \) are selected and changed into the index number of \( S \) by a random number generator. In other words, \( \alpha^{(g+1)} \) may be viewed as the mutation of his parent \( \alpha^{(g)} \), and new values, randomly selected numbers in \( S \), are introduced to \( V^{(g+1)} \). Therefore the subset of the offspring for computing the tensor \( T^k \) is partly changed.

   We should emphasize that after the reproduction process, the position vector of each agent should be checked to ensure the elements are different from each other. If the same value is found, it will be replaced by a randomly generated one.

2. **Diffusion:** The diffusion behavior plays an important role for an agent to search new positions in the correspondence lattice. After the reproduction process, each agent of generation \( g \), \( \alpha^{(g)} \), computes the cost using Eq. (5), and compares it with that of its parent \( \alpha^{(g)} \). If the offspring has the cost advantage, it will survive and be appended to the active agent set \( A \). Its parent, however, will become inactive and be removed from the environment. If \( \alpha^{(g+1)} \) has a worse performance than its parent, it will be deleted at once without any chance to search further in the space. If the offspring of the same parent are all failed, their parent will be kept active in the environment with its age increased by one. Then all the successful agents in data set \( A \) are sorted ascendingly according to their cost, and the first \( n_{\text{out}} \) agents are kept active with the removing of the others from the environment, which
**Input:** A $1 \times n$ grid of correspondences  
**Output:** trifocal tensor

begin  
distribute an initial set of agents $\{\alpha\}^{(0)}$ in the environment, assign the elements of position vector $V$ to the index of $S$ in numerical order $(1, 2, 3, \ldots, n)$, $age(\alpha^{(0)}) \leftarrow 0$, assign the initial agent set to the currently-active agent set: $A \leftarrow \{\alpha\}^{(0)}$, compute the cost of agents in the initial set select the subset template from the agents in $\{\alpha\}^{(0)}$  
while $A \neq \emptyset$ do  
reproduction process, select element $V_i$,  
$V_i \leftarrow \text{random}[\text{Template}]$ or $V_i \leftarrow \text{random}[n]$,  
diffusion process,  
vanishing process,  
update subset template,  
endwhile  
compute tensor using the position vector of the best agent, return trifocal tensor,  
end

could also be called the survival-of-finite-fittest. If the number of successful agents is less than $n_{\text{best}}$, number of active agents, and ends with the same numb then keep all the remaining active. Thus each evolutionary generation will begin with finite or, or fewer offspring of better quality.

### 3.4 Subset template

In order to improve the collaborative ability of the agents, we apply a subset template in the evolutionary process. The subset template is the position vector of the best agent from each generation. In the next generation, the agents will select some elements from the template for reproduction by probability $P_T$, which have a higher possibility to be good matching points. Thus the reproduction behavior of the evolutionary agent has to be partly revised: two elements of $V^{(0)}$ are selected and changed into: (1) an element from the subset template with probability $P_T$, or (2) a random index number of $S$ with probability $1 - P_T$. The larger $P_T$ is, the more entries will be chosen from the template, but the fewer new positions will appear in the offspring, which affects the explorative ability of the agents in some way.

We would also emphasize that after each generation we will check the ages of active agents. If the age of an agent exceeds its life span, it will be removed from the environment, which avoids useless computation. If there is no active agent in the evolutionary environment, the whole process halts.

### 4 EXPERIMENTAL RESULTS

In this part, our novel approach is compared with several typical methods including RANSAC, MLESAC, MGA and SEA. In order to analyze the effectiveness of subset template, we use SEA+T and FMEA+T to denote the methods with templates, this discriminating them from SEA and FMEA methods.

#### 4.1 Experiments with synthetic data

In the experiments with synthetic data, the correspondences are randomly generated by space points in the region of $\mathbb{R}$ visible to three different positions of a synthetic camera: $P = C[I\{0\}]$ (C stands for camera intrinsic matrix), $P' = C[R'\{t'\}]$ and $P'' = C[R''\{t''\}]$, where the camera makes rotations $R'$ and $R''$, and translations $t'$ and $t''$.

Here the total number of correspondences is 100, and there are only 10 agents in $\{\alpha^{(0)}\}$. The number of agents for initialization may be larger than 10, but it will take more time for computation and ten agents has been found in practice to be good enough for real applications. The experiments are divided into two groups:

- (G1): Six different ranges of Gaussian noise are added to the projective correspondences, whose means are 0 and standard deviation vary from 0.5 to 3.0 (in steps of 0.5), as shown in Table 1.
Table 1: Residual error under variable variance of noise

<table>
<thead>
<tr>
<th>Noise level</th>
<th>Method</th>
<th>RANSAC</th>
<th>MLESAC</th>
<th>MGA</th>
<th>SEA</th>
<th>SEA+T</th>
<th>FMEA</th>
<th>FMEA+T</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>1.174</td>
<td>0.865</td>
<td>0.782</td>
<td>0.824</td>
<td>0.817</td>
<td>0.817</td>
<td>0.803</td>
<td></td>
</tr>
<tr>
<td>1.0</td>
<td>2.194</td>
<td>1.389</td>
<td>1.197</td>
<td>1.224</td>
<td>1.185</td>
<td>1.225</td>
<td>1.209</td>
<td></td>
</tr>
<tr>
<td>1.5</td>
<td>3.253</td>
<td>1.546</td>
<td>1.367</td>
<td>1.563</td>
<td>1.489</td>
<td>1.460</td>
<td>1.442</td>
<td></td>
</tr>
<tr>
<td>2.0</td>
<td>4.438</td>
<td>1.790</td>
<td>1.572</td>
<td>1.763</td>
<td>1.712</td>
<td>1.657</td>
<td>1.646</td>
<td></td>
</tr>
<tr>
<td>2.5</td>
<td>5.906</td>
<td>1.923</td>
<td>1.763</td>
<td>1.942</td>
<td>1.825</td>
<td>1.815</td>
<td>1.793</td>
<td></td>
</tr>
<tr>
<td>3.0</td>
<td>7.234</td>
<td>2.341</td>
<td>1.914</td>
<td>2.242</td>
<td>2.026</td>
<td>1.988</td>
<td>1.942</td>
<td></td>
</tr>
</tbody>
</table>

Figure 4: Residual error under noise-perturbation test, (a) results of all the seven methods, (b) results of genetic algorithm and EA-based approaches.

Figure 5: Residual error under outlier-perturbation test, (a) results of all the seven methods, (b) results of genetic algorithm and EA-based approaches.

Table 2: Residual error under different percentage of outliers

<table>
<thead>
<tr>
<th>Outlier percentage</th>
<th>Method</th>
<th>RANSAC</th>
<th>MLESAC</th>
<th>MGA</th>
<th>SEA</th>
<th>SEA+T</th>
<th>FMEA</th>
<th>FMEA+T</th>
</tr>
</thead>
<tbody>
<tr>
<td>10%</td>
<td>3.734</td>
<td>1.426</td>
<td>1.253</td>
<td>1.286</td>
<td>1.237</td>
<td>1.232</td>
<td>1.231</td>
<td></td>
</tr>
<tr>
<td>20%</td>
<td>4.925</td>
<td>1.532</td>
<td>1.314</td>
<td>1.421</td>
<td>1.395</td>
<td>1.310</td>
<td>1.320</td>
<td></td>
</tr>
<tr>
<td>30%</td>
<td>10.83</td>
<td>1.973</td>
<td>1.724</td>
<td>1.895</td>
<td>1.827</td>
<td>1.755</td>
<td>1.710</td>
<td></td>
</tr>
<tr>
<td>40%</td>
<td>15.72</td>
<td>2.272</td>
<td>1.978</td>
<td>2.263</td>
<td>2.211</td>
<td>2.116</td>
<td>2.018</td>
<td></td>
</tr>
<tr>
<td>50%</td>
<td>34.86</td>
<td>2.925</td>
<td>2.226</td>
<td>2.485</td>
<td>2.406</td>
<td>2.421</td>
<td>2.332</td>
<td></td>
</tr>
</tbody>
</table>
Table 3: Average computation time for two groups (Sec.)

<table>
<thead>
<tr>
<th>Method</th>
<th>Group</th>
<th>RANSAC</th>
<th>MLESAC</th>
<th>MGA</th>
<th>SEA</th>
<th>SEA+T</th>
<th>FMEA</th>
<th>FMEA+T</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>G1</td>
<td>3.141</td>
<td>2.735</td>
<td>4.320</td>
<td>2.324</td>
<td>2.418</td>
<td>1.563</td>
<td>1.615</td>
</tr>
<tr>
<td></td>
<td>G2</td>
<td>3.673</td>
<td>3.573</td>
<td>4.456</td>
<td>2.141</td>
<td>2.152</td>
<td>1.325</td>
<td>1.377</td>
</tr>
</tbody>
</table>

Figure 6: Computation time of synthetic data test

(G2): The means and standard deviation of Gaussian noise are fixed to 0, 1, respectively; the percentage of outliers disturbed by the noise and false matches are varied from 10% to 50%, as shown in Table 2.

Tables 1 and 2 show the experimental results of (G1) and (G2) respectively, and Figures 4 and 5 also illustrate them. Table 3 shows the average computation time taken by these methods, which is also illustrated in Figure 6. From these tables and figures, it can be noticed that the EA-based approaches perform better than other typical methods, and almost as well as genetic algorithm in terms of accuracy. In the four EA-based methods, FMEA turns out to be the quickest followed by FMEA+T. The residual error of FMEA is smaller than that of SEA, and the computation time decreased by 48.69% in the noise-perturbation test, and 61.58% in the outlier-perturbation test. This strongly suggests that the survival-of-finite-fitness rule efficiently relieves the computational burden by removing a large number of unfit agents. It can also be seen that FMEA +T and SEA+T obtain better results than FMEA and SEA, which confirms that the subset template improves the communication among all the agents in the population and helps offspring inherit good resources.

4.2 Experiments with medical images

The performance of our approach is also demonstrated by using a variety of image triplets. Three different triplets of medical images are taken from a laparoscopic operation. Figure 7 illustrates the first triplet of images we utilized. The white circles denote the feature points obtained with corner detector, and the white arrow lines illustrate the movement of matching points between the images.

Table 4 shows the residual error of the medical image testing. We can see that FMEA method also perform best in real image experiments. The mean residual error of RANSAC, MLESAC, MGA and SEA are 7.240, 1.132, 0.886 and 1.070 times as much as that of FMEA. As to the computational efficiency, FMEA works so fast that the computation time for FMEA is 0.4158, 0.6832 as much as those of SEA and MGA, respectively.

From the experiments it can be concluded that the novel evolutionary strategy of FMEA helps agents search for a fit parameter set in the uncertain solution space, and allows them to move more efficiently toward the global optimum by gradually reducing the chance of reproducing an unfit dataset.

Figure 7: The medical images from three viewpoints
Table 4: Residual error of different pairs of medical images

<table>
<thead>
<tr>
<th>Method Group</th>
<th>RANSAC</th>
<th>MLESAC</th>
<th>MGA</th>
<th>SEA</th>
<th>SEA+T</th>
<th>FMEA</th>
<th>FMEA+T</th>
</tr>
</thead>
<tbody>
<tr>
<td>MG1</td>
<td>6.537</td>
<td>1.664</td>
<td>1.584</td>
<td>1.702</td>
<td>1.887</td>
<td>1.637</td>
<td>1.621</td>
</tr>
<tr>
<td>MG2</td>
<td>8.025</td>
<td>2.124</td>
<td>1.621</td>
<td>2.116</td>
<td>2.075</td>
<td>1.936</td>
<td>1.907</td>
</tr>
<tr>
<td>MG3</td>
<td>29.06</td>
<td>3.032</td>
<td>2.135</td>
<td>2.626</td>
<td>2.651</td>
<td>2.452</td>
<td>2.276</td>
</tr>
</tbody>
</table>

5 CONCLUSION

In this paper, we described a novel competitive evolutionary agent-based approach to trifocal tensor estimation, which employs a new competitive strategy to control the breeding number of new agents and reduce the chance of reproducing unfit ones. It focuses on the reproduction behavior to reduce the computation time, and produces results commensurate with, or superior to, that of SEA. The experimental results indicate that the proposed method attains a high level of performance in terms of accuracy and computational efficiency. It can obtain an optimal (or near optimal) result in the solution space and is robust to outliers, even when a large number of outliers are involved.

By accurately estimating the trifocal tensor, it will now be possible to generate 3D views of the sequence of 2D images. This brings the authors closer to their ultimate goal, the real time generation of 3D views during a laparoscopic procedure in order to enhance features, in particular obscured features, to the surgeon. This requires that the geometric data are estimated as fast and accurately as possible. The novel finite multiple evolutionary agent-based approach presented here allows us to do this.

REFERENCES


