FORMAL SPECIFICATION AND VERIFICATION OF XML-BASED BUSINESS DOMAIN MODELS

Wolfgang Schuetzelhofer
IBM Austria, Tullnertalgasse 74/1, A-1230 Vienna, Austria

Karl M. Goeschka
Vienna University of Technology, Gusshausstrasse 27-29/384, A-1040 Vienna, Austria

Keywords: Semantic meta model, Business domain model, Graph theory, Constraint modeling, XML language

Abstract: The rapidly growing use of XML in the development of business to business (B2B) applications requires new approaches in building enterprise application infrastructures. In this field the modeling of business domain semantics, thus focusing on the user's perception of data, in contrast to physical data representation, is gathering more and more importance. It is increasingly important to provide a sound mathematical foundation on modeling business domains, together with a well defined way to map business domain semantics to XML-structures. In our recent work we propose a semantic meta model, built on set- and algebra-theory, considered to serve for the formal definition of operations and transformations and to prove the correctness and completeness of design methods. Based on the mathematical model we propose an XML language to construct domain models and to formally express business domain semantics. The language not only allows to express structural schemas and static constraints but also provides to formulate dynamic business rules, which is considered critical for the quality of a business domain model and which is therefore centrally focused in our work. In addition we provide an XML syntax to encode domain instances and we apply standardized XML technologies to formally verify the validity of domain instances with respect to their specifying domain models. With our paper we contribute to the field of formal software engineering by proposing a business domain modeling language based on XML and founded on a sound mathematical model. The expression of dynamic business rules and the application of XML technologies to formally verify validity of domain instances and of entire domain models are the strength of our approach.

1 INTRODUCTION

The field of research on semantic data models has grown rapidly over the last years (Schmidt 1975, Peckham 1988, Gogolla 1991, Schnase 1993, Chen 1999, Trastour 2002) with a continuous change of focus towards modeling complex business domains. We contribute to this development with our recent work by introducing a semantic meta model based on set- and algebra-theory. It provides a framework for the specification of complex business domains, and it serves as a basis for the formal definition of operations, mappings and transformations and to prove the correctness and completeness of new and extended design methods. Algebraic specifications, by means of algebraic equations (called Σ-equations), serve to formally define validity of business domain models as well as of domain instances. Our special focus is on the seamless integration of business knowledge in form of static and dynamic business rules, which highly influences the expressiveness and quality of a business domain model.

On the other hand XML, as a standardized data description language, is gathering more and more importance in the field of data interchange in B2B applications. XML-based data exchange between different systems requires transformations of XML-structures. These transformations in turn have to be proved for equivalence and soundness.

In our work we propose a formal method to map business domain semantics to XML-structures based on our theoretical model, and we additionally provide an XML-encoding for domain instances. This allows to formally verify validity of XML-based business domain models and of XML-encoded
domain instances and it provides for the formal proof of equivalence and soundness of transformations on XML-structures.

The contribution of our recent work to the field of formal software engineering is
• to provide a sound mathematical foundation in form of a semantic meta model, which builds a framework for the specification of complex business domains,
• to provide a mathematical method which allows to verify validity of business domain models and of domain instances,
• to propose a formal method how to apply domain semantics to XML-structures,
• to outline an approach, which allows to leverage standardized XML-technologies to verify validity of XML-based business domain models as well as of XML-encoded domain instances.

2 A SEMANTIC META MODEL FOR SPECIFYING BUSINESS DOMAINS

As core of our work we introduce a semantic meta model, which allows to formally specify business domains. Business domains are commonly expressed by means of their concepts (e.g. person, car, address, ...) and by means of relationships between these concepts (e.g. ownership, residence, ...). Directed graphs are considered to serve as the basis to describe business domain models. Research in the field of semantic nets (Rada 1990) has successfully proven that directed graphs are well suited to express business domain concepts and relationships between business domain concepts. We call such graphs domain graphs. We furthermore introduce types on nodes and links of directed graphs, so that business domain concepts are mapped to node-types and so that relationships between these business domain concepts are mapped to link-types. Recursive link composition and type hierarchies are proposed as powerful means of abstraction. Structural constraints on types, together with a formalism to describe complex dependencies between model elements, are used to express business knowledge in form of business rules. The consequent separation of structure and content in combination with the proposed method to define business rules, enforces the introduction of a three-layer meta model. We also introduce algebraic specifications to formally define validity of domain graphs as well as of domain instances. A number of simplified examples and graphical views are used to provide an intuitive approach to the underlying mathematical theory.

2.1 Typed Directed Graphs – Foundation of the Meta Model

An extended version of directed graphs serves as the fundamental basis for our approach. In contrast to a common definition, where a directed graph (DG) consists of a set of vertices (nodes) and of a set of edges, we propose an extended definition by introducing the concept of links. Links allow to recursively specify connections between nodes of a directed graph. Every edge of a DG is represented as a link and every connected sequence of links forms a link in turn. This recursive approach serves as a powerful means of abstraction, which especially proves profitable when the goal is to model business domains with the necessity to view and describe those business domains at different levels of abstraction.

By additionally defining mappings of nodes to node-types and of links to link-types, the concept of typed directed graphs (simply called typed graphs) is introduced. Two layers, called type-level and instance-level, provide a clear separation of type and instance. The graph type \( GT \) populates the type-level:

\[
GT = (NT, LT) \quad NT ... a set of node-types, \quad LT ... a set of link-types.
\]

The typed graph \( TG \) populates the instance-level:

\[
TG = (N, L) \quad N ... a set of typed nodes, \quad L ... a set of typed links.
\]

Type mappings are defined:

\[
type: N \rightarrow NT \quad and \quad type: L \rightarrow LT
\]

Additionally nodes are mapped to node-values, so that a node of a typed graph can be written as a pair consisting of a node-value and of a node-type:

\[
n = \langle vnode, tnode \rangle; \quad tnode \in NT
\]

Typed links are defined recursively:

\[
1. \quad l^0 = \langle \langle ns, nt \rangle, tlink \rangle; \quad l^0 \in L, \quad ns, nt \in N, \quad tlink \in LT
\]

... every edge of the graph is represented (encapsulated) by a link. Such a link is called direct link \( (l^0) \).

\[
2. \quad l = \langle l_1, l_2, ..., l_k \rangle; \quad l_1, l_2, ..., l_k \in L;
\]

\[
k \geq 1 \land \forall i, \quad 1 \leq i < k : t(l_i) = s(l_{i+1}), \quad tlink \in LT
\]

... a connected sequence of links is a link in turn and it is called indirect link \( (l) \). \( s(l) \) maps a link to its source node and \( t(l) \) maps a link to its target node.
2.2 Three Layer Meta Model

So far the graph type (GT) simply consists of a set of node-types and of a set of link-types. Business domain concepts are mapped to node-types and relationships between business domain concepts are mapped to link-types. Hence a graph type models a business domain and specifies the domain’s structure. Business rules express structural constraints on domain instances. Consequently they are specified as part of the graph type. In particular, the structural constraints are expressed on link-types and on node-types. Whereas one possibility is to specify constraints in form of structured values of the appropriate node- and link-types, the proposed approach is to express the structural constraints in form of distinct nodes and links as part of a directed graph, moreover, as part of a typed directed graph which is modeled at the type-level. This means, the graph type (GT) itself is extended to form a typed directed graph. The semantic of a specific constraint is then covered by a link of GT, whereas a value for a constraint whenever needed (e.g. a range for a cardinality constraint) is defined by means of a node of GT.

This approach enforces the introduction of a third layer which we call meta-type-level. The layer is introduced, so that nodes and links at the type-level are instances of meta-types. These meta-types are defined at the meta-type-level.

More generally stated, nodes and links at the instance-level are instances of nodes at the type-level, which in turn are instances of meta-node-types. The three layers of the resulting meta model are depicted in Figure 1.

<table>
<thead>
<tr>
<th>Level</th>
<th>Elements</th>
<th>Covers / Expresses</th>
</tr>
</thead>
<tbody>
<tr>
<td>meta-type-level</td>
<td>meta-types</td>
<td>Model Semantic</td>
</tr>
<tr>
<td>type-level</td>
<td>instance-of-types</td>
<td>Business Domain Model</td>
</tr>
<tr>
<td>instance-level</td>
<td>instance-of-instanes</td>
<td>Domain Instance</td>
</tr>
</tbody>
</table>

At the instance-level a node of the typed graph represents either:
- an OBJECT i.e. an instance of a business domain concept (e.g. a specific person)
- a PRIMITIVE-VALUE (instance of a primitive data type) (e.g. the integer value 20).

A link at the instance-level represents a RELATION between an OBJECT and/or a PRIMITIVE-VALUE (e.g. a link of type residence may relate a specific person to a certain address, or a link of type birthDate may relate a person to a primitive DATE value).

A simple analogy with E-R modeling concepts can be constructed, so that an OBJECT corresponds to an entity-instance, so that a PRIMITIVE-VALUE corresponds to an attribute-value and so that a RELATION corresponds to either a relationship-instance or to an attribute-name respectively.

At the type-level a node of the typed graph represents either:
- a business domain CONCEPT (e.g. Person), which specifies a type of OBJECTs
- a primitive DATA TYPE (e.g. Integer, Date, ...), which specifies a type of PRIMITIVE-VALUES
- a CONCEPT-RELATIONSHIP, a relationship between business domain concepts (e.g. residence), which is a link-(RELATION-) type
- a CONSTRAINT-VALUE (e.g. a specific range for a cardinality constraint).

A link at the type-level covers constraint semantics (e.g. a distinct super-type relation, a source-node-type constraint, a cardinality constraint, ...), hence it is called a SEMANTIC-RELATION. The graph at the type-level is called Domain Graph (DoG) because it is the means to model business domains.

At the meta-type-level the model semantic is covered by a set of meta-node-types which represent the types of possible nodes for the type-level, and by a set of meta-link-types representing all possible sorts of SEMANTIC-RELATIONS.

2.3 Model Semantic

Figure 2 lists the set of meta-node-types and the set of meta-link-types. Possible links between nodes at the type-level with respect to the nodes’ and links’ meta-types are also shown.
Meta-Node-Types

bd_concept ... Instances represent business domain CONCEPTs (e.g. Person, Address, ...).
p-type ... Instances represent primitive DATA TYPEs (e.g. Integer, String, Date, ...).
bd-relat ... Instances describe relationships between business domain concepts (e.g. residence, ownership, ...).
r-range ... Instances serve to specify valid ranges for cardinality constraints.
condition ... Instances are used to formulate dynamic business rules.
l-t-seq ... Instances constrain the sequence of intermediate links of composed RELATIONS (indirect links at the instance-level).

Meta-Link-Types

Meta-link-types cover the semantic of structural constraints. Instances of meta-link-types are SEMANTIC-RELATIONS at the type-level.

super ... Instances of super relate types to their super-type.
s-type ... Instances constrain the source-node-type of RELATIONS.
t-type ... Instances constrain the target-node-type for RELATIONS.
s-card, t-card ... Instances are used to model cardinality constraints.
composition ... Instances of composition connect CONCEPT-RELATIONSHIPS to lt-seq instances, thus constraining intermediate link sequences of composed RELATIONS.
abstract ... Instances of abstract connect CONCEPTS or CONCEPT-RELATIONSHIPS to condition nodes in order to specify abstract types.
if ... Instances represent if-branches of condition trees.
else ... Instances represent else-branches of condition trees.

2.4 Static and Dynamic Business Rules

A major concern of our work is the seamless integration of business rules. In the proposed approach such business rules are defined in form of cardinality constraints which are specified on CONCEPT-RELATIONSHIPS. We distinguish between static and dynamic business rules. Dynamic business rules, in contrast to static ones, depend on the state of distinct domain instances. As an example one can think of a sales transaction which, depending on the age of the customer, allows only certain products to be added as line-items. In DGM such dynamic business rules are expressed in form of conditional cardinality constraints. Figures 3 and 4 provide a simplified example. Whereas Figure 3 shows a UML representation, Figure 4 outlines a graphical view of the appropriate domain graph.
Figure 4: Business rules expressed as conditional cardinality constraints

Figure 4 provides a graphical representation of the set theory based formalism. It is more suitable and easier to read, especially as the presented model is based on graph theory. Note, that the representation in Figure 4 can be unambiguously transformed into the set theory based formalism. However, the used notation is not intended to serve as a graphical modeling language (although possible). Other graphical notations, such as used with UML (UML, 2001), are specifically designed to accomplish this task. Figure 4 demonstrates how a boolean expression is used to formulate a dynamic business rule. Path expressions are the means to select values out of distinct domain instances. These values serve as arguments for the boolean expression. Based on the result of evaluating the boolean expression, the condition tree (encircled in Figure 4) is traversed (if, else branches). The traversal results in a specific range node which specifies the cardinality constraint to be applied. OCL (OCL, 2002), a constraint language, has been adapted to the DGM in order to formulate dynamic business rules.

2.5 Domain Graph Model - Summary

DGM provides a semantic meta-model to formally specify and verify business domains. The meta-model consists of three layers, which are called levels. The topmost layer is named meta-type-level and defines the model semantic. The medium layer is called type-level and hosts typed-directed-graphs, called domain graphs (DoGs), which model distinct business domains. The bottom layer is named instance-level, and it is the layer where instances of specific business domains, again in form of typed-directed-graphs, are constructed.

At the type-level, concepts and concept-relationships describe the basic domain structure, and constraints in combination with boolean OCL-expressions are used to formulate static- and dynamic business rules. At the instance-level, objects, (primitive-)values and relations compose domain instances, and they are constructed, so that they satisfy the structural constraints and business rules defined by their domain graph.

The theory of algebraic specifications is applied to formally define validity. Algebraic specifications are based on algebraic signatures, so that a specification extends a signature with the formal construction of $\Sigma$-equations. A set of such $\Sigma$-equation provides the formal specification of valid domain graphs and of valid domain instances. Figure 5 outlines the basic building blocks of the DGM.

3 XML-ENCODING OF THE DOMAIN GRAPH MODEL

Based on the semantic meta-model we propose an XML-language to specify domain graphs (DoGs), thus modeling business domains. We call this language XDoG. We also provide an XML-
encoding for domain instances, so that instances of a business domain (e.g. specific sales-transactions) can be encoded in form of XML-structures.

The decision to develop a business domain modeling language based on XML is motivated by several reasons. Beside its already leading role in data interchange in business to business (B2B) applications, XML is also gathering more and more importance in the field of semantic data modeling. Based on the foundation of the XML Information Set (W3C, 2004) and on a clear and simple syntax, the extensibility of XML is targeted towards the development of domain specific languages. Grouped around a set of stable and consistent standards, a rapidly growing number of tools and applications are established. This allows new developments to build on mature and well tested technologies and to benefit from a high amount of re-use. This, together with the widespread use of XML, leads to an ever growing number of XML-languages arising in the field of formal software engineering. Recent developments on Web-Ontologies (W3C, 2001) specify XML-languages which aim to define the terms used to describe and represent specific areas of knowledge. DAML+OIL (DAML + OIL, 2001) is an example of such languages.

For our work, interoperability, standards compliance and the possibility to re-use software tools for practical implementations are the major motivations to develop an XML-language for modeling business domains as well as to provide an XML-encoding for business domain instances.

Rather than providing the complete specification of the domain modeling language XDoG and of the XML-encoding for domain instances as part of this paper, we will focus on how we utilize XML technologies to model XML-based, valid business domains and how we apply standardized XML technologies to verify validity of XML-encoded domain instances.

Figure 6 depicts how formal modeling languages in general and the XDoG language in particular are aligned with the domain graph model (DGM). Expressions of the XDoG language are used to encode a domain graph in XML thus modeling a business domain. The XDoG language itself is specified by means of an XML-Schema, which is derived from SpecDoG and which restricts the XDoG language to describe valid domain graphs (Figure 6 (1)). A domain graph is encoded in XDoG and serves to specify valid domain instances (Figure 6 (2)). Domain instances are XML-encoded in turn. The encoding follows an instance-encoding-specification, which basically defines how OBJECTs, PRIMITIVE VALUES and RELATIONS of a domain instance are represented as XML elements and attributes respectively (Figure 6 (3)).

Just like an XML-schema provides the structural constraints for XML-documents which are instances of that schema, a domain graph or the domain graph’s XML encoding respectively, constrains domain instances. With that relationship in mind, it seems straight forward to derive an XML-schema from a domain graph, or, even better, to directly encode a domain graph in form of an XML-schema. However, the XML-schema-language proves not to be powerful enough to express all constraints specified by a domain graph. Especially dynamic business rules, which play a central role in the DGM theory, but also the composition property of composed RELATIONS cannot be formulated by means of the XML-schema-language. On one hand this is the reason why the XDoG language was developed to provide an appropriate domain graph encoding. On the other hand it is the reason why an XML-schema alone is not sufficient to completely specify domain instances. Nevertheless, the XML-schema-language is not entirely omitted in the specification of the domain instance encoding. Instead, constructs of the XML-schema-language are provided to specify the static constraints on XML-encoded domain instances. This ‘static schema’ is derived from the XML-encoded domain graph. This is done by providing a set of transformation rules in form of an XSL-stylesheet, so that a standard XSL-processor can generate the ‘static schema’ out of the XML-encoded domain graph (Figure 6 (4)).

In order to perform validation of XML-encoded domain instances with respect to dynamic business rules and composed RELATIONS, a different approach
is required. A set of rules in form of another XSL-stylesheet serves to generate the ‘XSL-validation-stylesheet’ (Figure 6 (5)) out of the XML-encoded domain graph. The ‘XSL-validation-stylesheet’ is constructed, so that it contains XPath (W3C, 1999) expressions which properly encode path-expressions (they are part of boolean OCL expressions) which in turn specify dynamic business rules. The XPath expressions serve to select values or value sets out of domain instances. The ‘XSL-validation-stylesheet’ itself is an XSL-stylesheet. Applied to an XML-encoded domain instance it generates a statement about the domain instance’s validity (with respect to dynamic business rules and composed RELATIONS). By performing schema-validation based on the ‘static schema’ and by applying the ‘XSL-validation-stylesheet’ (Figure 6 (6)), we provide validation of XML-encoded domain instances, utilizing standard XML technologies.

4 RELATED WORK

In the field of semantic data modeling a number of publications can be found, which apply set- and graph-theory to map domain semantics to structured hypertext systems and hyperlinked data sets. Our work, providing a semantic meta model together with a proposed XML-encoding, is highly related to this field of research, as the origin of XML can be found in hypertext systems. Moreover, hypertext systems may profitably be viewed as semantic nets (Wang, 1998), which actually provide the basis of our approach on business domain modeling.

Beside publications on formal models for hypertext (Lange, 1990) and on constraining hypertext structures (Chidlovskii, 2000), a lot of related approaches stress the need for our work: Bench-Capon and Dunne (Bench, 1889), in an early approach use a DAG (directed graph) structure and a set of constraints to model electronic documents. Contrasting our approach links are not typed and only represent the containment relationship, providing limited possibilities to express domain semantics. The formal hypertext model described in Tochtermann and Dittrich (Dittrich, 1995) provides some formally defined structural concepts, lacking mechanisms to define more powerful structural and relational constraints. Wang and Rada (Wang, 1998) have developed a semantic data model based on the concept of a semantic net, introducing organizational and relational link types on a DAG. In contrast to our work they do not provide an extensible type system and they also do not provide a mechanism to formulate dynamic constraints. Abiteboul and Hull (Abiteboul, 1987) in their well known approach on formalizing a semantic model recognize the importance of types which are used to model object structures (IFO model), but they do not provide link type hierarchies. E-R modeling, which is very much influenced by the work of P.P.Chen (Chen, 1976, Chen, 1999) provides another field of related work. In contrast to E-R approaches our work is highly built on graph theory and we centrally focus on the possibility to formulate dynamic business rules. H.V.Jagadish et.al. (Jagadish, 2001) provide an algebraic approach for query and transformation of XML tree structures. Whereas they propose a sound mathematical theory, their approach in contrast to our work applies to tree graphs rather than to directed graphs. The OMG with its MOF (Meta-Object-Facility) specification (OMG, 2000), introduces a four layer meta-data architecture in contrast to the three layer model we are proposing in our paper. The Unified Modeling Language (UML) specifies semantics on the level of Meta-Models (UML, 2001, Schleicher, 2001), but does not provide expressing complex business rules as integral part (although the recent integration of OCL as part of UML is targeted in that direction). Recent developments in the field of (Web-) Ontologies (W3C, 2001), such as DAML+OIL, aim to define the terms used to describe and represent specific areas of knowledge. They provide expressing object constraints, but are limited in specifying dynamic constraints which express complex business rules.

Our work is mainly build on a theoretical approach which is inherently complex, especially concerning the integration of dynamic business rules. Whereas most of the related work, discussed in this section, has already successfully proven its applicability and usefulness in many practical implementations, applications, providing a proof of concept for our approach, are currently still under construction.

5 CONCLUSION AND FUTURE WORK

In this paper we have presented the theory of a three-layered semantic meta model for specifying business domains, which we call domain graph model (DGM). We have introduced a Domain Graph (DoG) as a directed graph with typed nodes and typed links which models business domains at the type-level of the DGM. We have outlined, how domain semantics are applied to a DoG and how static and dynamic business rules, playing a central role, are seamlessly integrated by specifying types, structural constraints, and conditions. We have
discussed how construction rules for DoGs are specified at the meta-type-level, how business domains are modeled at the type-level and how valid domain instances are provided at the instance-level. This leads to a clear separation of structure and content and is proposed as a flexible way to deliver semantic data. The concept of type hierarchies as well as the approach of recursive link composition were introduced as powerful means of abstraction.

We have based the domain graph model (DGM) on set- and algebra- theories, providing a sound mathematical foundation for the formal definition of operations and transformations and to prove the correctness and completeness of design methods. The formal verification of valid domain graphs and of valid domain instances, by use of algebraic specifications, satisfies the requirement for robustness of semantic data. It was outlined, that by proposing an XML-encoding for domain graphs and for domain instances we provide an approach to apply domain semantics to XML-structures. This allows to utilize DGM theories for interchange of semantic data in XML-based B2B applications.

We have discussed structural constraints, the specification of static and dynamic business rules and different abstraction mechanisms. The definition of operations, built on the mathematical basis of the DGM, is considered to specify additional dynamic aspects as part of future work. Manipulating a domain instance by inserting, deleting or updating nodes and links, thereby maintaining consistency and validity of the domain instance are such dynamic aspects to be specified. New and extended design methods, which can be formally specified and verified, are seen to be another profitable output of future work based on this paper.

REFERENCES

W3C, XML Information Set http://www.w3.org/TR/xml-infoset/
W3C, Web-Ontology http://www.w3.org/2001/sw/WebOnt/
UML, Meta-Model Specification (v1.4) http://www.rational.com/uml
W3C, DAML + OIL http://www.w3.org/TR/daml+oil-reference